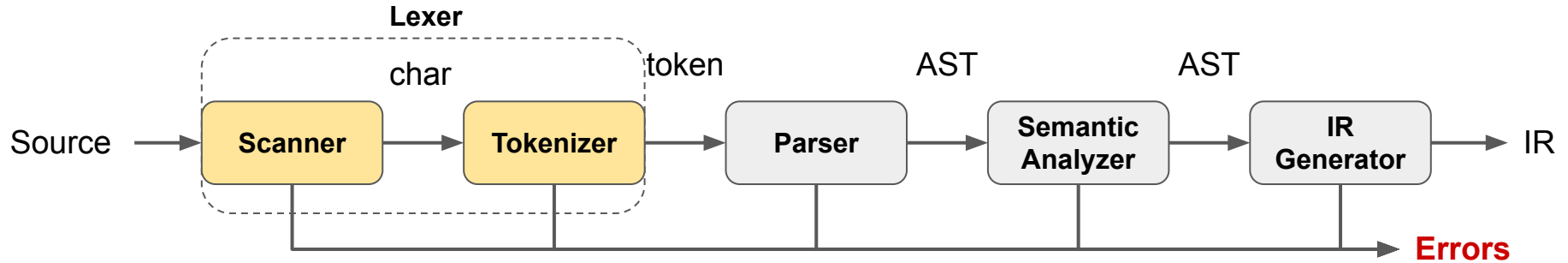


Compiling Techniques

Lecture 3: Lexical Analysis

The Lexer



- Maps character stream into words — the basic unit of syntax
- Assign a syntactic category to each work (part of speech)
 - $x = x + y$; becomes ID(x) EQ ID(x) PLUS ID(y) SC
 - word \sim lexeme
 - syntactic category \sim part of speech
 - In casual speech, we call the pair a token
- Typical tokens: number, identifier, +, -, new, while, if, . . .
- Scanner eliminates white space (including comments)

Context-free Language

Context-free syntax is specified with a grammar

- SheepNoise \rightarrow SheepNoise baa | baa
- This grammar defines the set of noises that a sheep makes under normal circumstances

It is written in a variant of Backus Naur Form (BNF)

Formally, a grammar $G = (S, N, T, P)$

- S is the start symbol
- N is a set of non-terminal symbols
- T is a set of terminal symbols or words
- P is a set of productions or rewrite rules ($P: N \rightarrow N \cup T$)

Simple Expression Grammar

goal \rightarrow expr

expr \rightarrow expr op term | term

term \rightarrow number | id

op \rightarrow + | -

S = goal

T = { number, id , +, - }

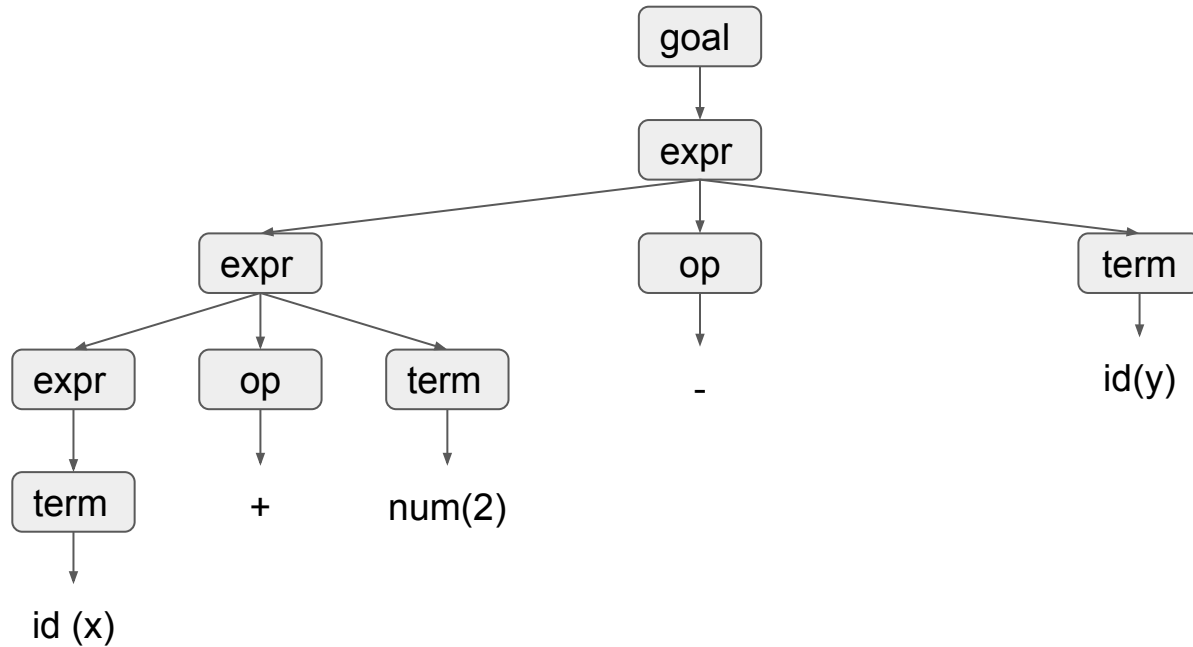
N = { goal , expr , term , op }

P = { 1, 2, 3, 4, 5, 6, 7 }

- This grammar defines simple expressions with addition & subtraction over “number” and “id”
- This grammar, like many, falls in a class called “context-free grammars”, abbreviated CFG

Parse Tree

$x + 2 - y$



Regular Expression

Grammars can often be simplified and shortened using an augmented BNF notation where:

- x^* is the Kleene closure : zero or more occurrences of x
- x^+ is the positive closure : one or more occurrences of x
- $[x]$ is an option: zero or one occurrence of x

Example: identifier syntax

```
identifier ::= letter ( letter | digit)*  
digit ::= "0" | ... | "9"  
letter ::= "a" | ... | "z" | "A" | ... | "Z"
```

Exercise: Signed Numbers

Task: Write the grammar of signed integers

Use pen and paper to write down such a grammar!

Regular Language

Definition

A language is regular if it can be expressed with a single regular expression or with multiple non-recursive regular expressions.

- Regular languages can be used to specify the words to be translated to tokens by the lexer.
- Regular languages can be recognised with finite state machine.
- Using results from automata theory and theory of algorithms, we can automatically build recognisers from regular expressions.

Regular Language to Program

Given the following:

- `c` is a lookahead character;
- `next()` consumes the next character;
- `error ()` quits with an error message; and
- `first (exp)` is the set of initial characters of `exp`.

Regular Language to Program

RE	pr(RE)
"x"	<pre>if c == x: next() else: error()</pre>
(exp)	<pre>pr(exp)</pre>
[exp]	<pre>if c in first(exp): pr(exp)</pre>
exp*	<pre>while c in first(exp): pr(exp)</pre>

Regular Language to Program

RE	pr(RE)
exp+	<pre>pr(exp) while c in first(exp): pr(exp)</pre>
fact_1 ... fact_n	<pre>pr(fact_1); ... ; pr(fact_n)</pre>
term_1 ... term_n	<pre>if c in first(term_1): pr(term_1) elif elif c in first(term_n): pr(term_n) else error()</pre>

Left Parsable

Definition: left-parsable

A grammar is left-parsable if:

<code>term_1 ... term_n</code>		The terms do not share any initial symbols.
<code>fact_1 ... fact_n</code>		If <code>fact_i</code> contains the empty symbol then <code>fact_i</code> and <code>fact_i + 1</code> do not share any common initial symbols.
<code>[exp], exp*</code>		The initial symbols of <code>exp</code> cannot contain a symbol which belong to the first set of an expression following <code>exp</code> .

Example: Recognising identifiers

```
void ident ( ) {
    if (c is in [ a-zA-Z ] )
        letter();
    else
        error();

    while (c is in [ a-zA-Z0-9]) {
        switch (c) {
            case c is in [ a-zA-Z ] : letter();

            case c is in [0 -9] : digit();

            default : error();
        }
    }
}

void letter( ) { ... }

void digit() { ... }
```

Example: Simplified Python Version

```
void ident () {  
    if (Character.isLetter(c))  
        next();  
    else  
        error();  
    while (Character.isLetterOrDigit(c))  
        next();  
}
```

Role of Lexical Analyser

The main role of the lexical analyser (or lexer) is to read a bit of the input and return a lexeme (or token).

```
def Lexer:  
    def nextToken(self) {  
        // return the next token, ignoring whitespaces  
    }  
    ...  
}
```

White spaces are usually ignored by the lexer. White spaces are:

- white characters (tabulation, newline, . . .)
- comments (any character following “//” or enclosed between “/*” and “*/”

What is a token?

A token consists of a token class and other additional information.

Example: some token classes

IDENTIFIER	→	foo , main , cnt , ...
NUMBER	→	0 , -12, 1000 , ...
STRING_LITERAL	→	"Hello world!" , "a" , ...
EQ	→	==
ASSIGN	→	=
PLUS	→	+
LPAR	→	(
...	→	...

```
class Token:  
    Kind: TokenKind  
    Value: Any = None
```


Example

Given the following Python program:

```
def foo (i):  
    return i+2
```

the lexer will return:

```
DEF IDENTIFIER("foo") LPAR IDENTIFIER ("i") RPAR COLON  
    RETURN IDENTIFIER("i") PLUS NUMBER("2")
```

A Lexer for Simple Arithmetic Expressions

Example: BNF syntax

```
identifier ::= letter ( letter | digit )*
digit      ::= "0" | . . . | "9"
letter     ::= "a " | . . . | " z " | "A" | . . . | "Z"
number     ::= digit+
plus       ::= "+"
minus      ::= "-"
```

Example: token definition

```
from enum import Enum
from dataclasses import dataclass
```

```
class TokenClass(Enum):
    IDENTIFIER = 0
    NUMBER     = 1
    PLUS       = 2
    MINUS      = 3
```

```
@dataclass
class Token:
    type: TokenClass
    value: any = None

    def __repr__(self):
        return self.type.name + (":" + str(self.value)) if self.value else ""
```

Example: scanner implementation

```
class Scanner:
    def __init__(self, stream):
        self.stream = stream
        self.buffer = None

    def peek(self):
        if not self.buffer:
            self.buffer = self.next()
        return self.buffer

    def next(self):
        if self.buffer:
            c = self.buffer
            self.buffer = None
            return c

        return self.stream.read(1)
```

Example: Tokenizer implementation

```
class Tokenizer:
    def __init__(self, scanner):
        self.scanner = scanner
        self.buffer = None

    def peek(self):
        if not self.buffer:
            self.buffer = self.next()
        return self.buffer

    def next(self):
        if self.buffer:
            c = self.buffer
            self.buffer = None
            return c
        c = self.scanner.next()

        if c.isspace():
            return self.next()

        if c == "+":
            return Token(TokenClass.PLUS)

        if c == "-":
            return Token(TokenClass.MINUS)
```

Example: Tokenizer implementation (continued)

```
if c.isalpha():
    name = c
    c = self.scanner.peek()
    while c.isalpha() or c.isdigit():
        name += c
        self.scanner.next()
        c = self.scanner.peek()

    return Token(TokenClass.IDENTIFIER, name)
```

Example: Tokenizer implementation (continued)

```
if c.isdigit():
    digits = c
    c = self.scanner.peek()
    while c.isdigit():
        digits += c
        self.scanner.next()
        c = self.scanner.peek()
    value = int(digits)
    return Token(TokenClass.NUMBER, value)
```

Next Lecture

- Automatic Lexer Generation