

Conjunctive Queries: Fast Evaluation

(Chapter 18 of DBT)

[DBT] Database Theory, https://github.com/pdm-book/community

Complexity of Query Evaluation

Theorem: CQ-Evaluation is NP-complete, and in PTIME in data complexity

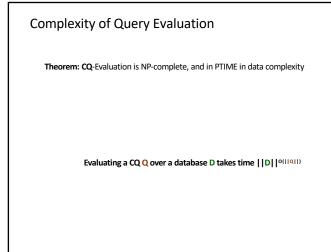
Proof:

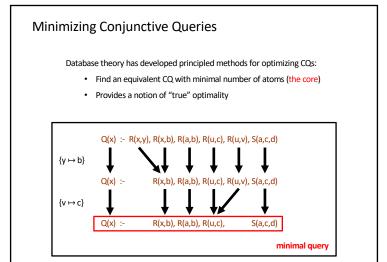
(NP-membership) Guess-and-check:

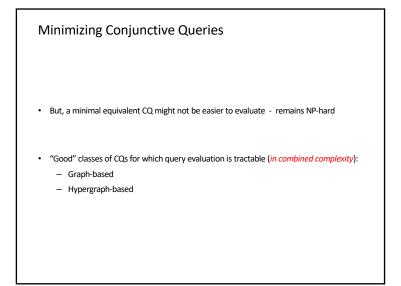
- Consider a database D, a CQ Q(x₁,...,x_k) :- body, and a tuple (a₁,...,a_k) of values
- Guess a substitution h : terms(body) → terms(D)
- Verify that h is a match of Q in D, i.e., $h(body) \subseteq D$ and $(h(x_1),...,h(x_k)) = (a_1,...,a_k)$

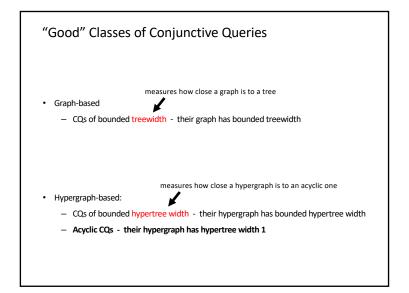
(NP-hardness) Reduction from 3-colorability

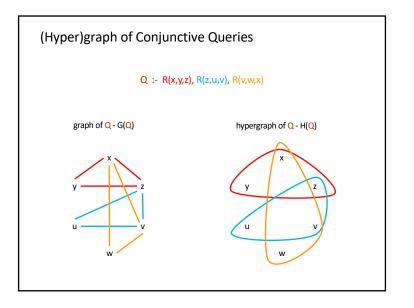
(in PTIME) For every substitution $h : terms(body) \rightarrow terms(D)$, check if $h(body) \subseteq D$ and $(h(x_1),...,h(x_k)) = (a_1,...,a_k)$

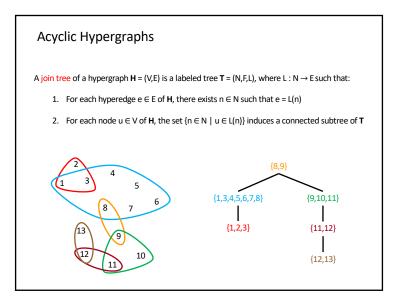


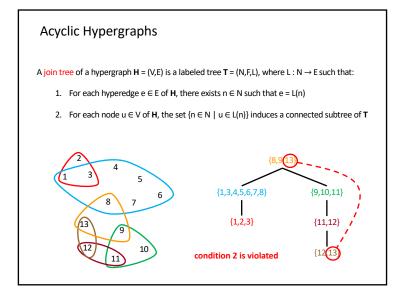


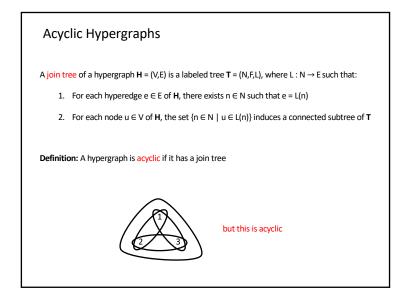


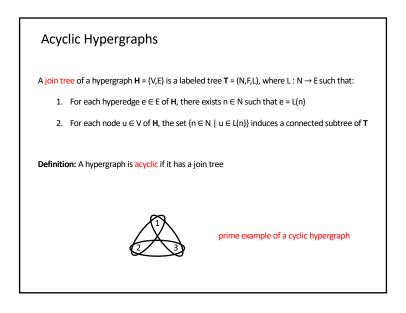


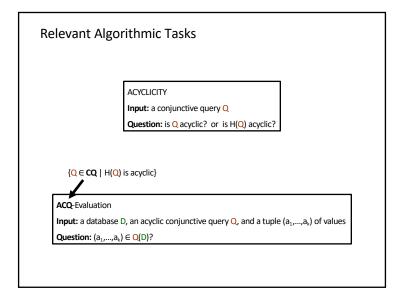


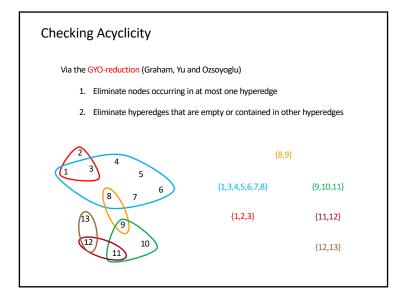


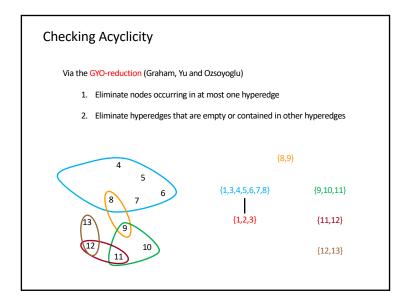


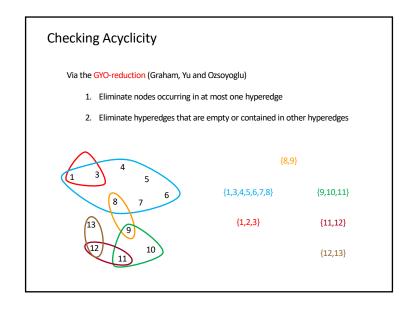


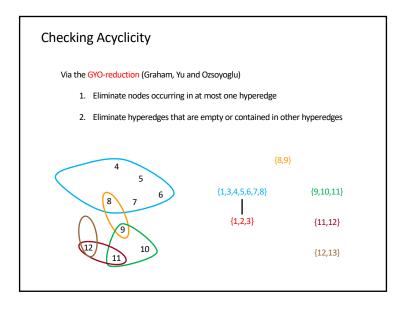


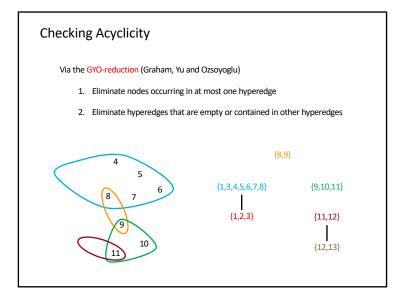


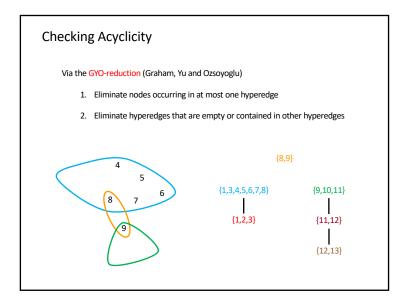


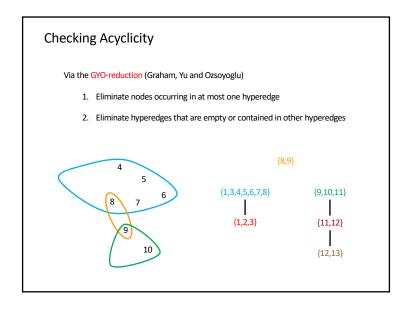


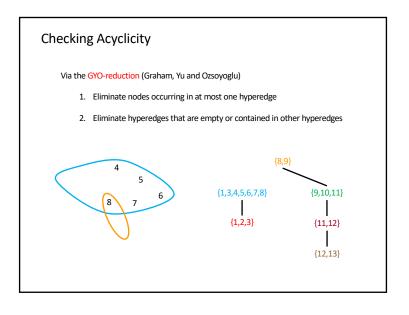


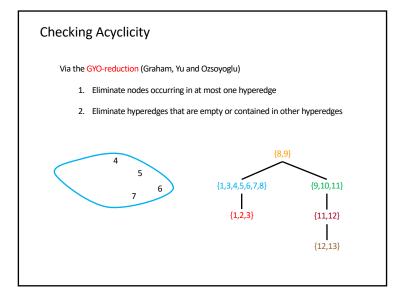


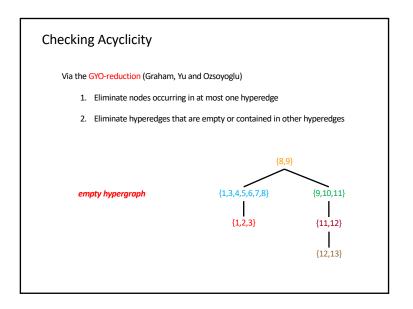


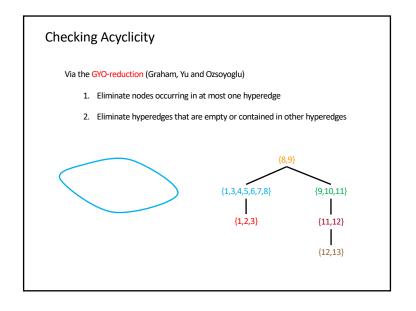


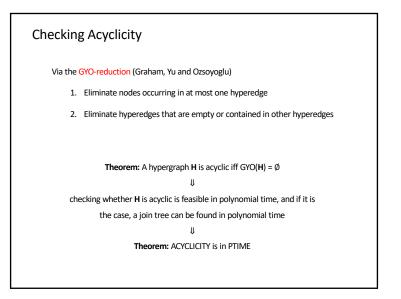


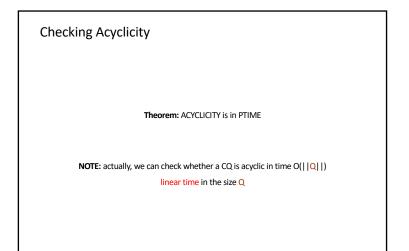












 Evaluating Acyclic CQs

 Theorem: ACQ-Evaluation is in PTIME

 NOTE: actually, if H(Q) is acyclic, then Q can be evaluated in time O(||D|| · ||Q||)

 Linear time in the size of D and Q

