

## **Conjunctive Queries: Fast Evaluation**

(Chapter 18 of DBT)

[DBT] Database Theory, https://github.com/pdm-book/community

## Complexity of Query Evaluation

Theorem: CQ-Evaluation is NP-complete, and in PTIME in data complexity

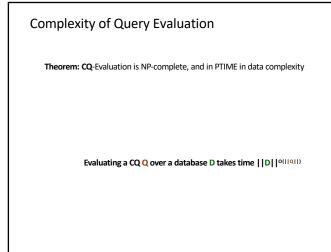
## Proof:

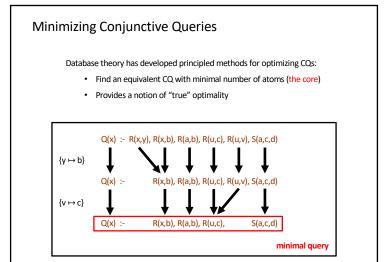
## (NP-membership) Guess-and-check:

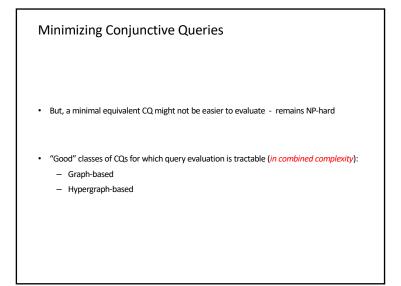
- Consider a database D, a CQ Q(x<sub>1</sub>,...,x<sub>k</sub>) :- body, and a tuple (a<sub>1</sub>,...,a<sub>k</sub>) of values
- Guess a substitution h : terms(body) → terms(D)
- Verify that h is a match of Q in D, i.e.,  $h(body) \subseteq D$  and  $(h(x_1),...,h(x_k)) = (a_1,...,a_k)$

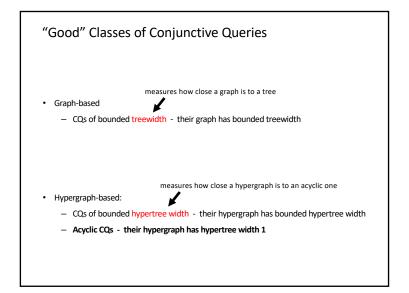
(NP-hardness) Reduction from 3-colorability

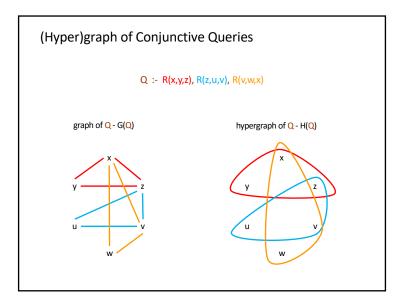
(in PTIME) For every substitution  $h : terms(body) \rightarrow terms(D)$ , check if  $h(body) \subseteq D$ and  $(h(x_1),...,h(x_k)) = (a_1,...,a_k)$ 

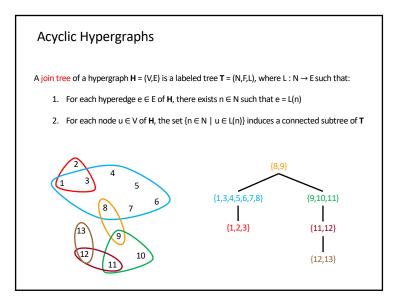


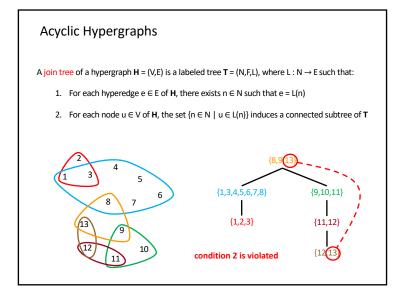


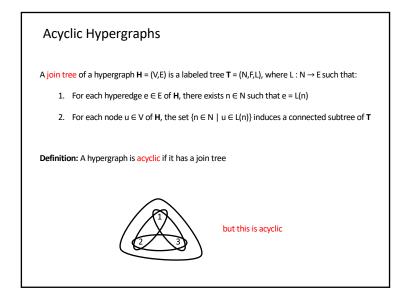


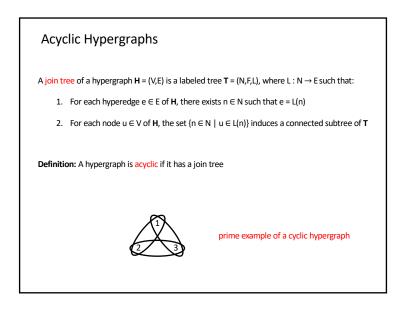


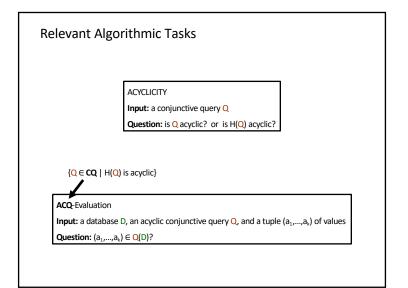


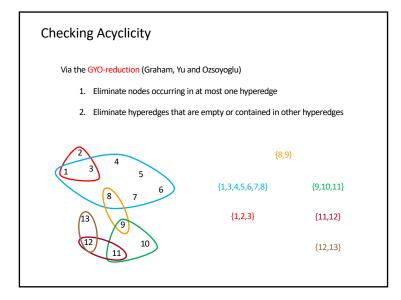


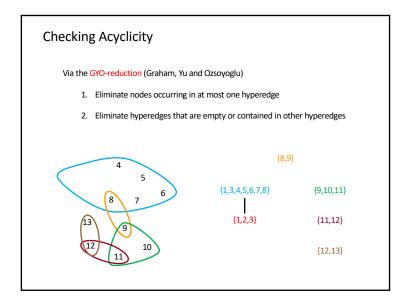


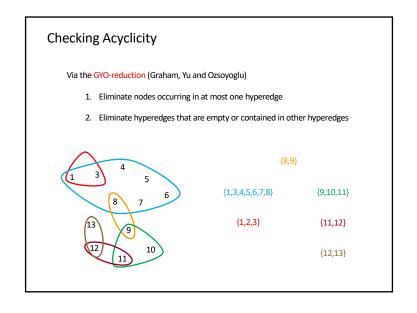


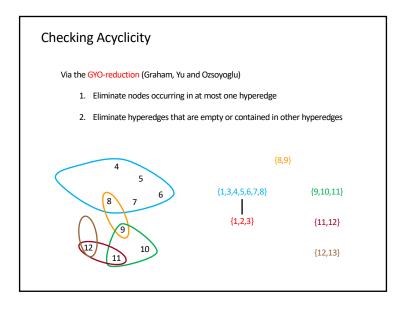


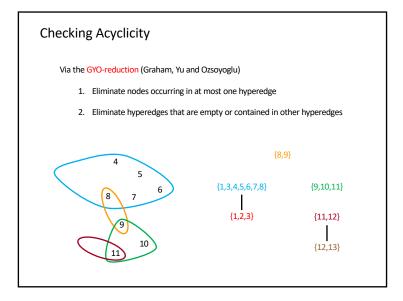


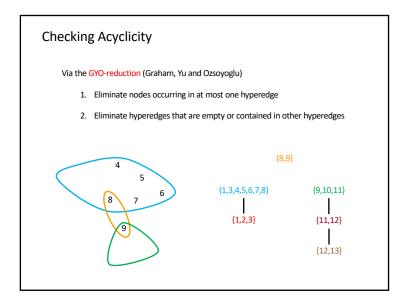


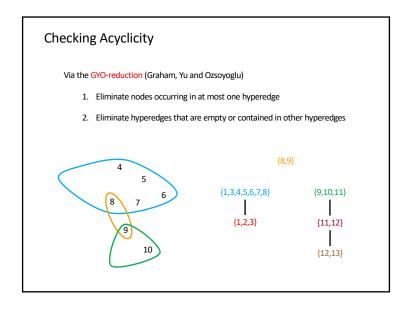


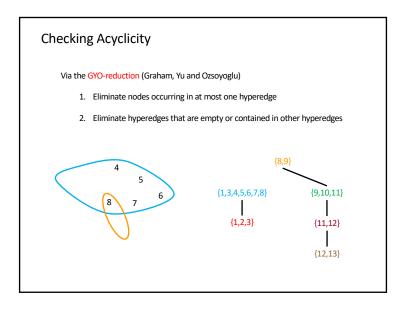


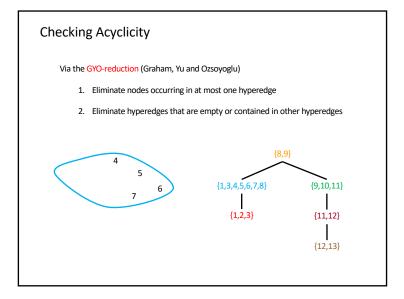


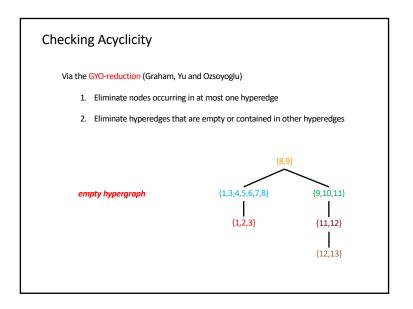


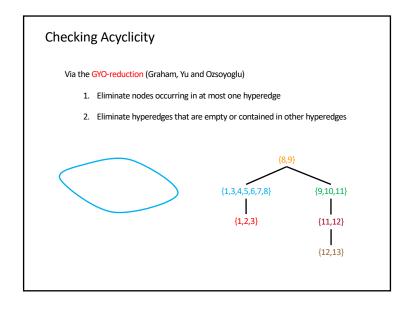


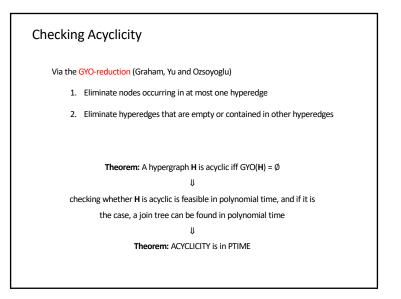


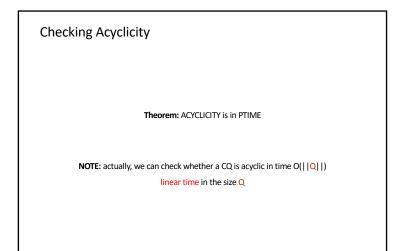












 Evaluating Acyclic CQs

 Theorem: ACQ-Evaluation is in PTIME

 NOTE: actually, if H(Q) is acyclic, then Q can be evaluated in time O(||D|| · ||Q||)

 Linear time in the size of D and Q

