

## **Conjunctive Queries: Fast Evaluation**

(Chapter 18 of DBT)

[DBT] Database Theory, https://github.com/pdm-book/community

Complexity of Query Evaluation

Theorem: CQ-Evaluation is NP-complete and in PTIME in data complexity

## Proof:

(NP-membership) Guess-and-check:

- Consider a database D, a CQ Q(x<sub>1</sub>,...,x<sub>k</sub>) :- body, and a tuple (a<sub>1</sub>,...,a<sub>k</sub>) of values
- Guess a substitution h : terms(body) → terms(D)
- Verify that h is a match of Q in D, i.e.,  $h(body) \subseteq D$  and  $(h(x_1),...,h(x_k)) = (a_1,...,a_k)$

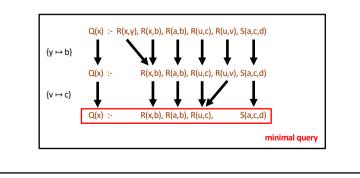
(NP-hardness) Reduction from 3-colorability

(in PTIME) For every substitution  $h : terms(body) \rightarrow terms(D)$ , check if  $h(body) \subseteq D$ and  $(h(x_1),...,h(x_k)) = (a_1,...,a_k)$ 

Complexity of Query Evaluation Theorem: CQ-Evaluation is NP-complete and in PTIME in data complexity Evaluating a CQ Q over a database D takes time ||D||<sup>o(||Q||)</sup>



Provides a notion of "true" optimality



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