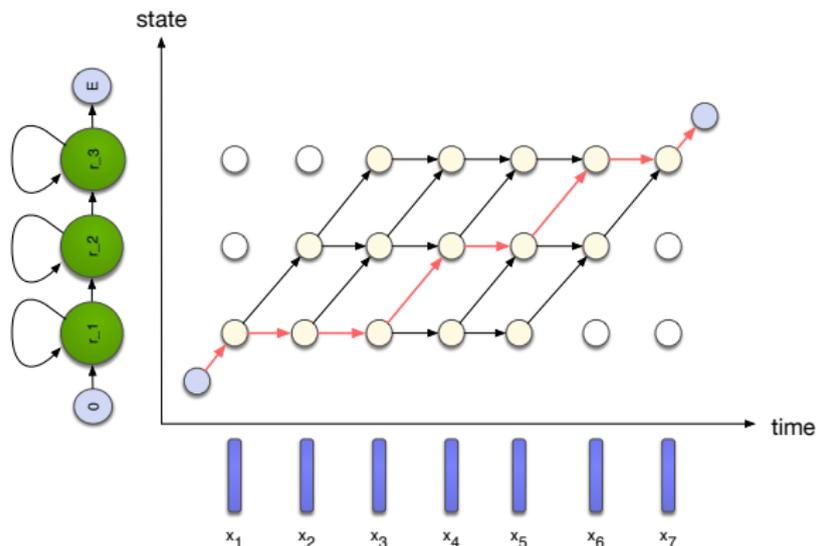


# Neural Networks for Acoustic Modelling: Hybrid HMM/DNN systems

Peter Bell

Automatic Speech Recognition – ASR Lecture 10  
12 February 2026

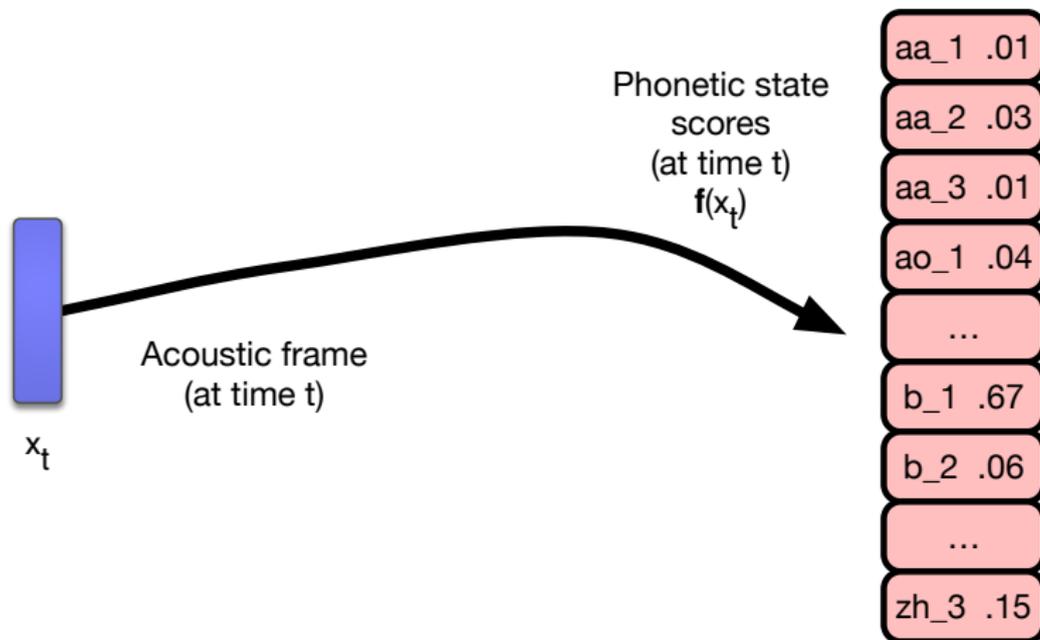
# Local phonetic scores and sequence modelling



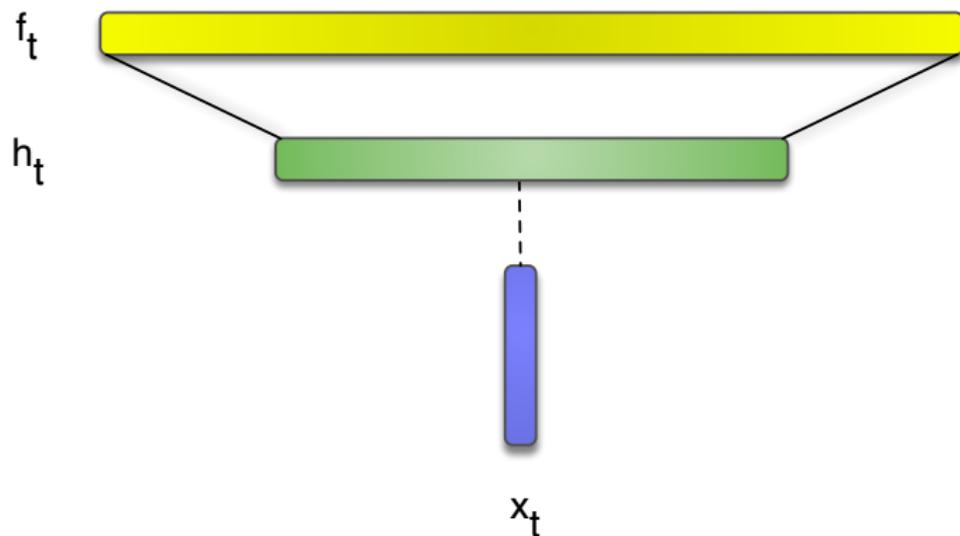
- Compute state observation scores (acoustic-frame, phone-model) – this does the detailed matching at the frame-level
- Chain observation scores together in a sequence – HMM

# HMM state scores

Output a score for each phone state



# Extracting features using a neural network



- Our network that predicts phonetic scores is a *classifier* – at training time each frame of data has a correct label (target output of 1), other labels have a target output of 0
- We can design an output layer which forces the output values to act like probabilities
  - Each output will be between 0 and 1
  - The  $J$  outputs will sum to 1
- A way to do this is using the *Softmax* activation function:

$$y_j = \frac{\exp(f_j)}{\sum_{k=1}^J \exp(f_k)}$$

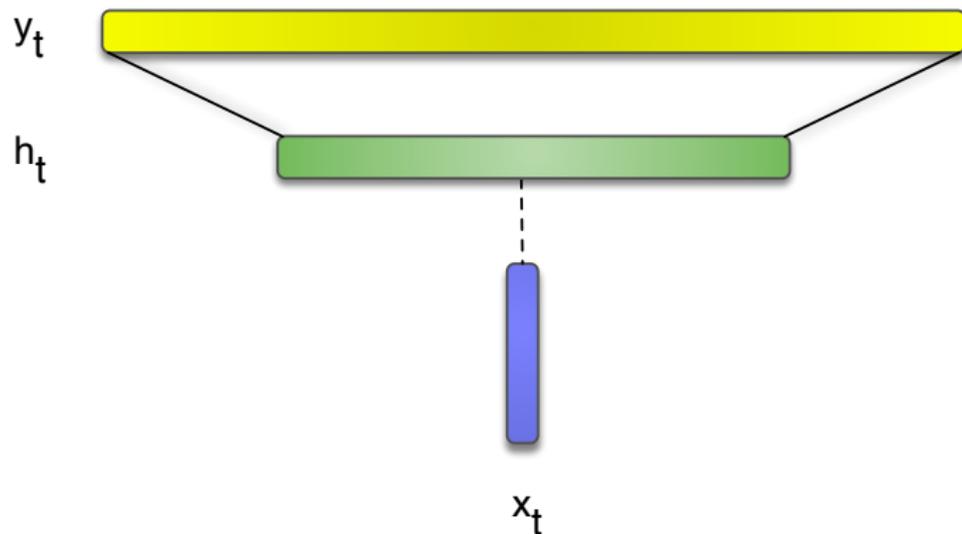
# Cross-entropy error function

- Since we are interpreting the network outputs as probabilities, we can write an error function for the network which aims to maximise the log probability of the correct label.
- If  $r_t^j$  is the 1/0 target of the the  $j$ th label for the  $t$ th frame, and  $y_t^j$  is the network output, then the cross-entropy (CE) error function is:

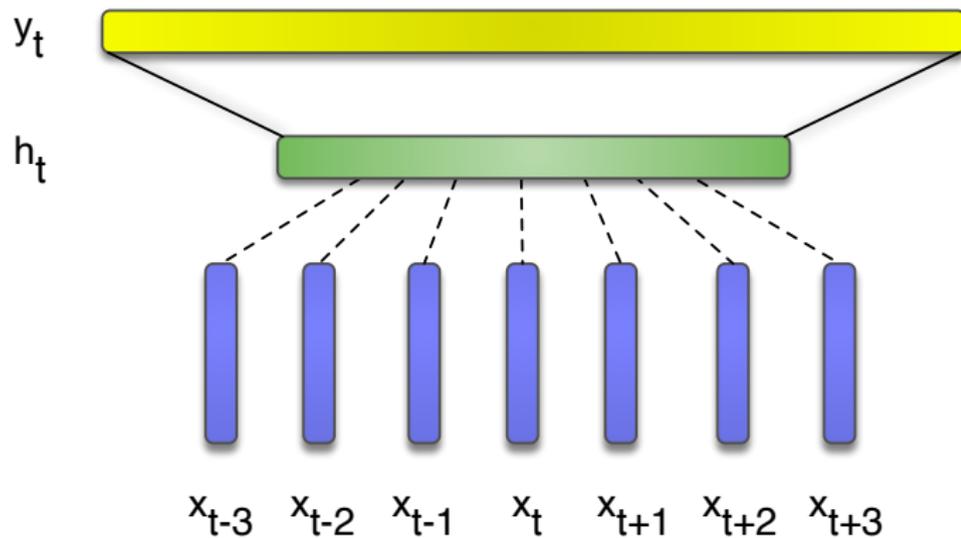
$$E^t = - \sum_{j=1}^J r_t^j \ln y_t^j$$

- Note that if the targets are 1/0 then the only the term corresponding to the correct label is non-zero in this summation.

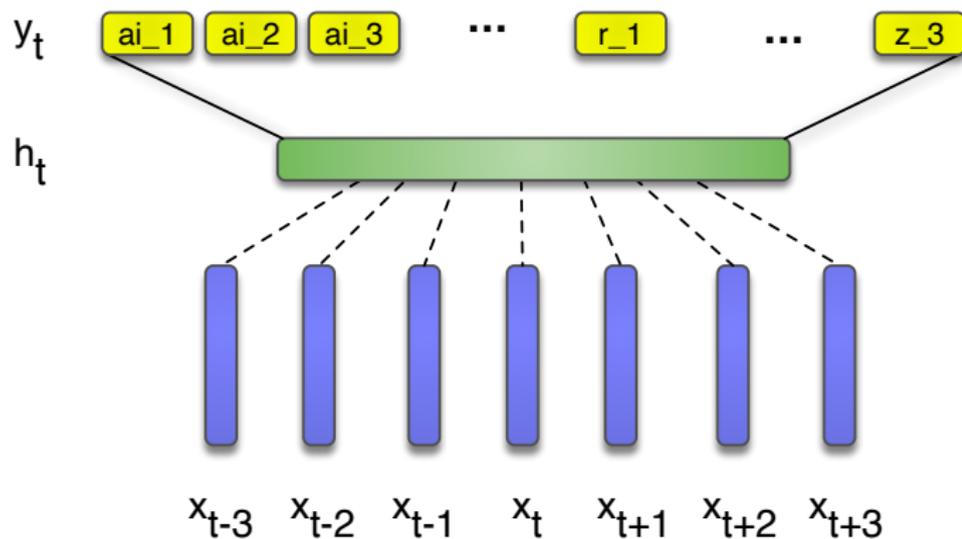
# Extracting features using a neural network



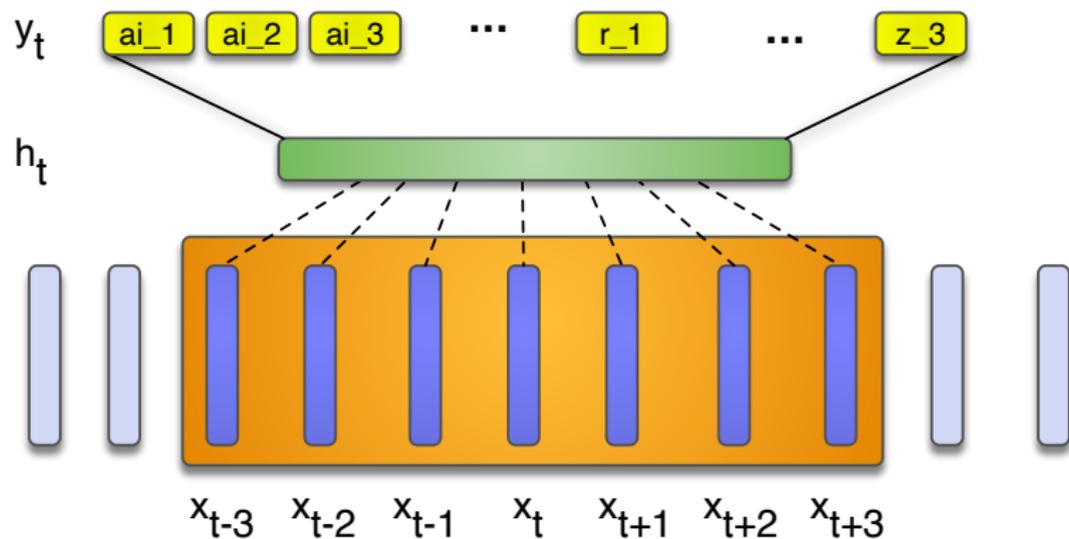
# Incorporate acoustic context



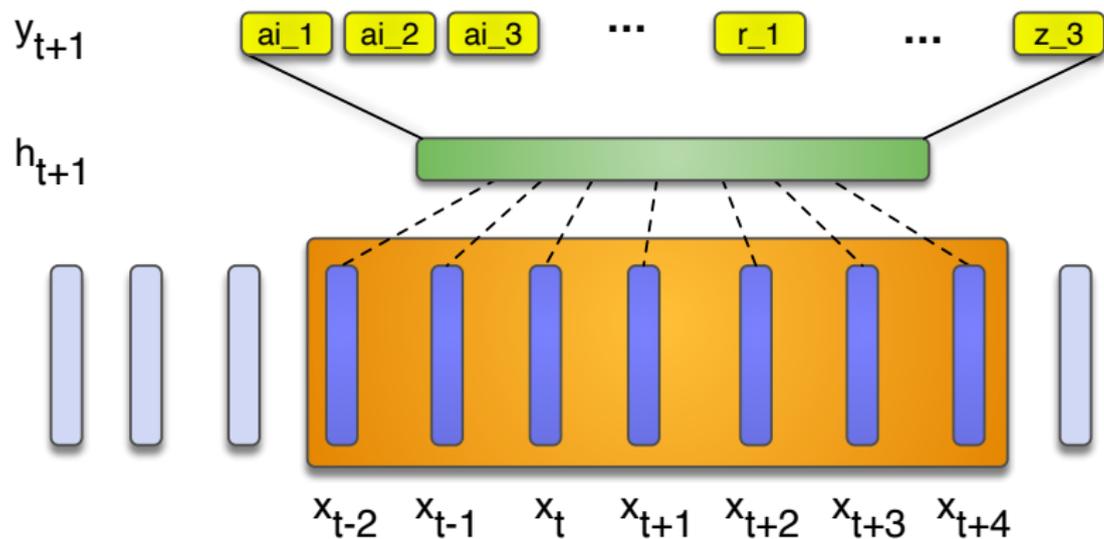
# Incorporate acoustic context



# Use a sliding window over time



# Use a sliding window over time



# Neural networks for large vocabulary recognition

- So far the networks are trained to *classify* each frame of observations
- In full speech recognition *recognition*, we need to obtain the best word sequence
- **Hybrid NN/HMM systems:** in an HMM, replace the GMMs used to estimate output pdfs with the outputs of neural networks
- Train a neural network to associate a HMM-state label with a frame of acoustic data (+ context)
- Can interpret the output of the network as  $P(\text{HMM-state} \mid \text{acoustic-frame})$
- Use NN to obtain output probabilities in Viterbi algorithm to find most probable sequence of phones

## Posterior probability estimation

- Consider a neural network trained as a classifier – each output corresponds to a class.
- When applying a trained network to test data, it can be shown that the value of output corresponding to class  $j$  given an input  $x_t$ , is an estimate of the posterior probability  $P(q_t = j|x_t)$ . (This is because we have softmax outputs and use a cross-entropy loss function)
- Using Bayes Rule we can relate the posterior  $P(q_t = j|x_t)$  to the likelihood  $p(x_t|q_t = j)$  used as an output probability in an HMM:

$$P(q_t|x_t) = \frac{p(x_t|q_t = j)P(q_t = j)}{p(x_t)}$$

# Scaled likelihoods

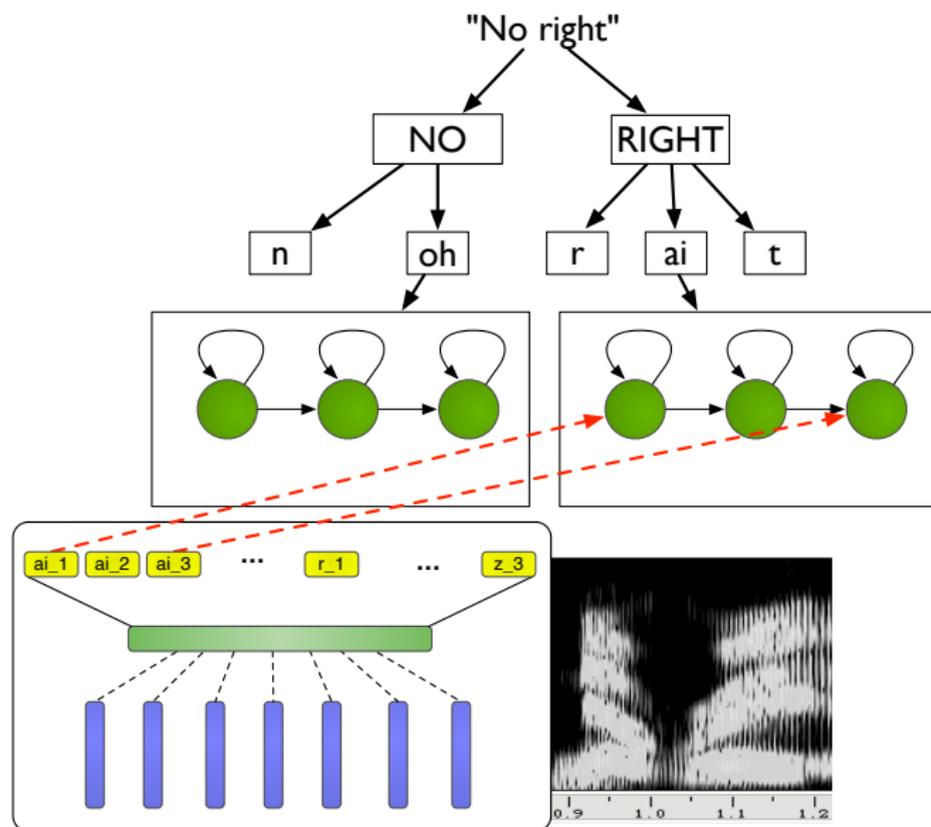
- If we would like to use NN outputs as output probabilities in an HMM, then we would like probabilities (or densities) of the form  $p(x|q)$  – likelihoods.

We can write *scaled likelihoods* as:

$$\frac{P(q_t = j|x_t)}{P(q_t = j)} = \frac{p(x_t|q_t = j)}{p(x_t)}$$

- Scaled likelihoods can be obtained by “dividing by the priors” – divide each network output  $P(q_t = j|x_t)$  by  $P(q_t = j)$ , the relative frequency of class  $j$  in the training data
- Using  $p(x_t|q_t = j)/p(x_t)$  rather than  $p(x_t|q_t = j)$  is OK since  $p(x_t)$  does not depend on the class  $j$
- Computing the scaled likelihoods can be interpreted as factoring out the prior estimates for each phone based on the acoustic training data. The HMM can then integrate better prior estimates based on the language model and lexicon

# Hybrid NN/HMM



# Modelling phonetic context (1)

- NNs can naturally model *acoustic* context, but how can we model *phonetic* context?
- Early solution (Bourlard et al, 1992) – separate the modelling of the primary class,  $y$ , and its context,  $c$ , with two neural networks:

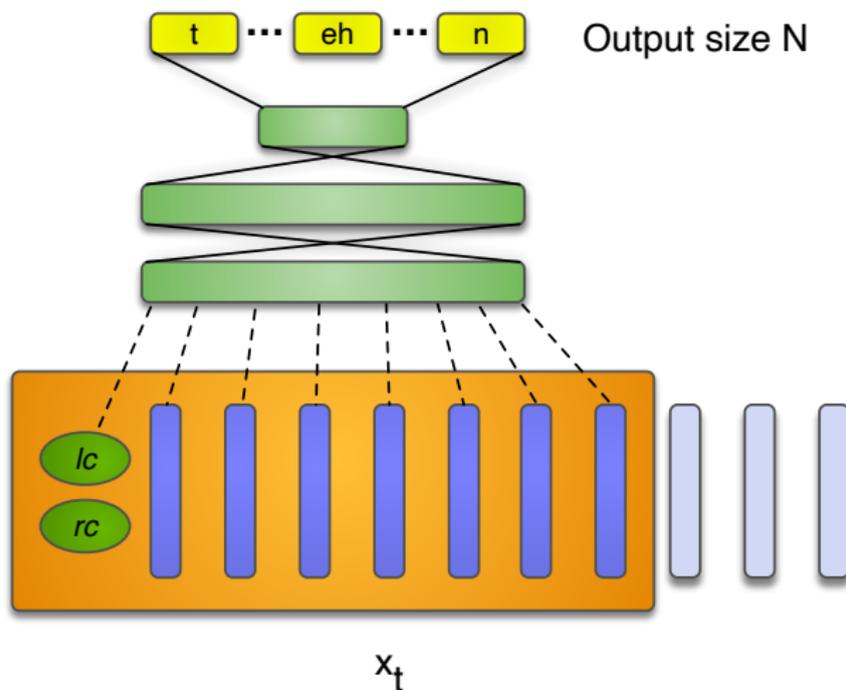
$$p(y, c|x) = p(c|y, x)p(y|x)$$

or

$$p(y, c|x) = p(y|c, x)p(c|x)$$

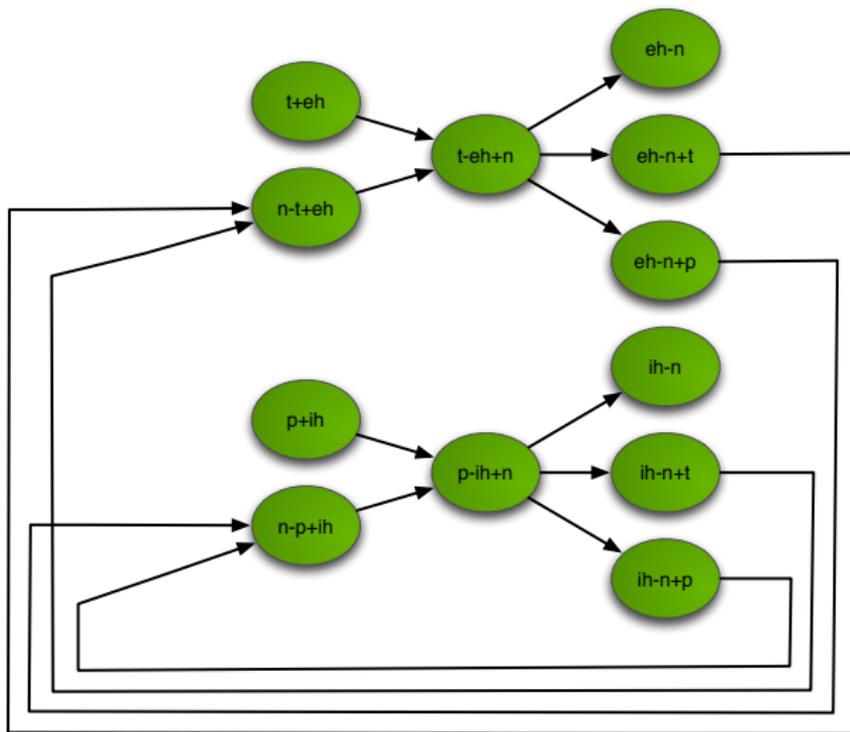
During decoding, we need separate forward passes for each context

# Using context as input for $p(y|c, x)$

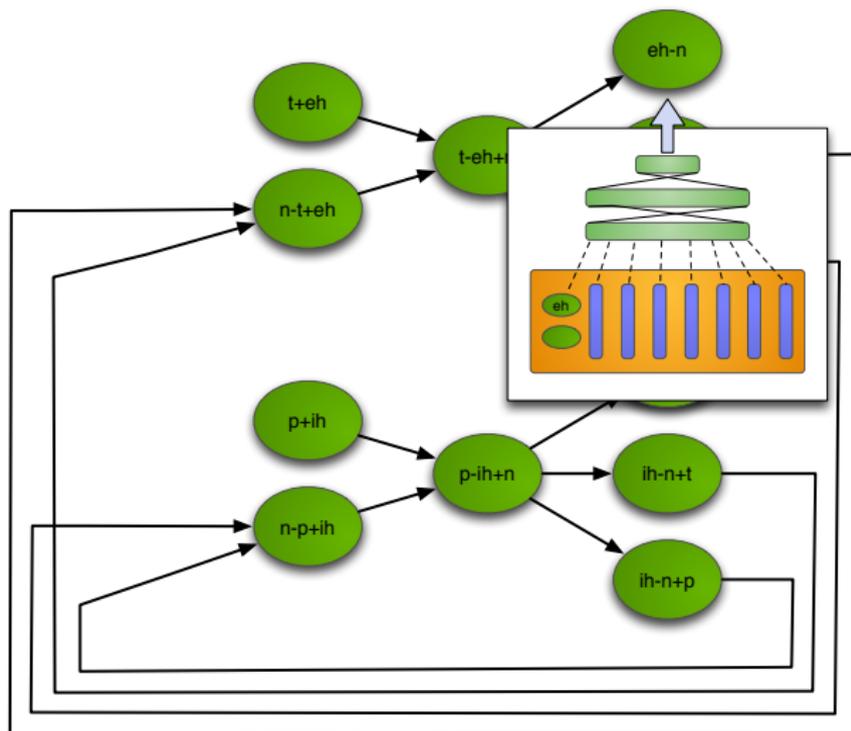


Showing just one HMM state per phone for simplicity

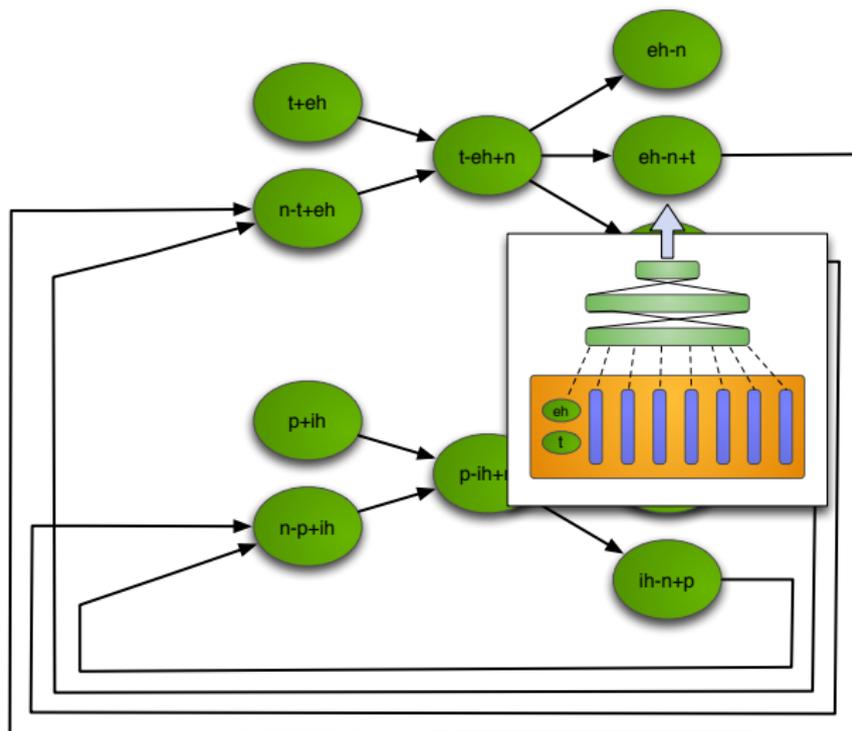
# Context-dependent decoding



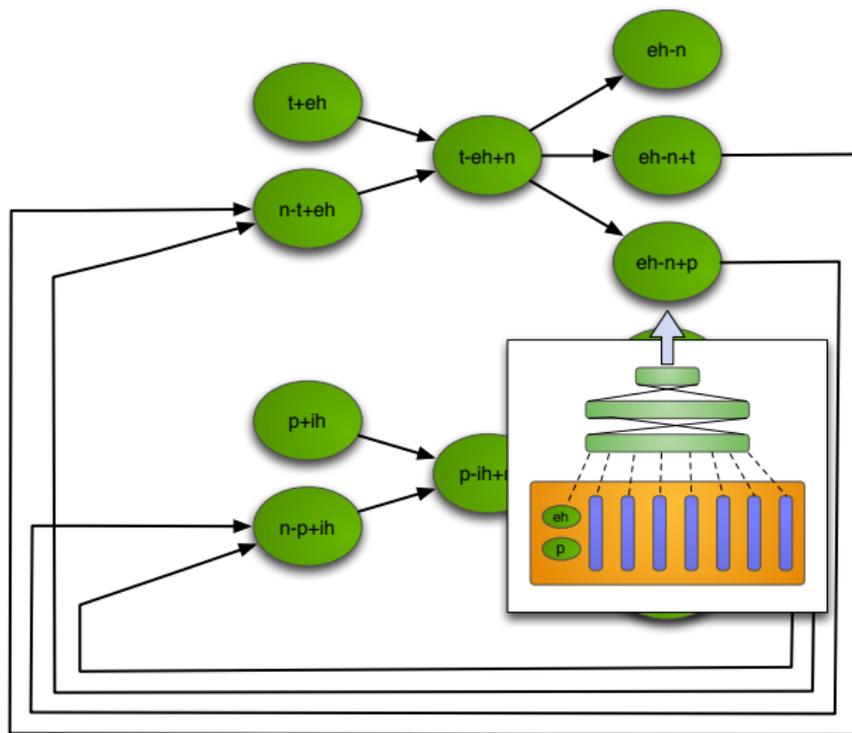
# Context-dependent decoding



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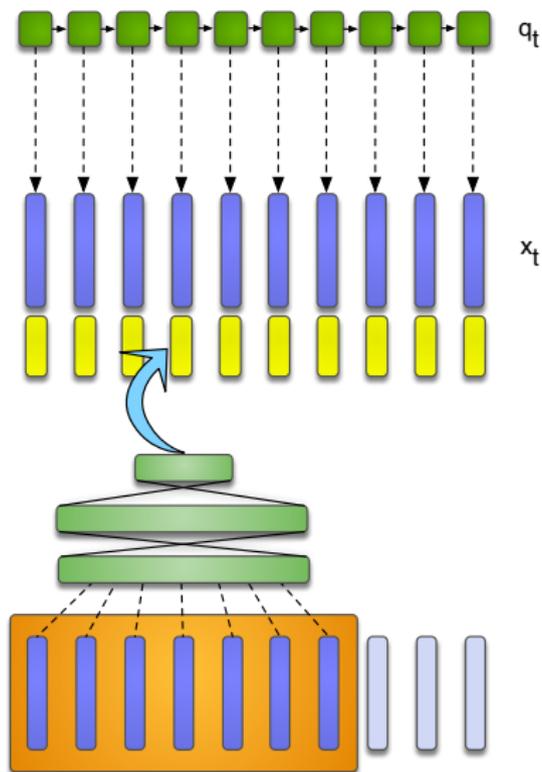


## Modelling phonetic context (2)

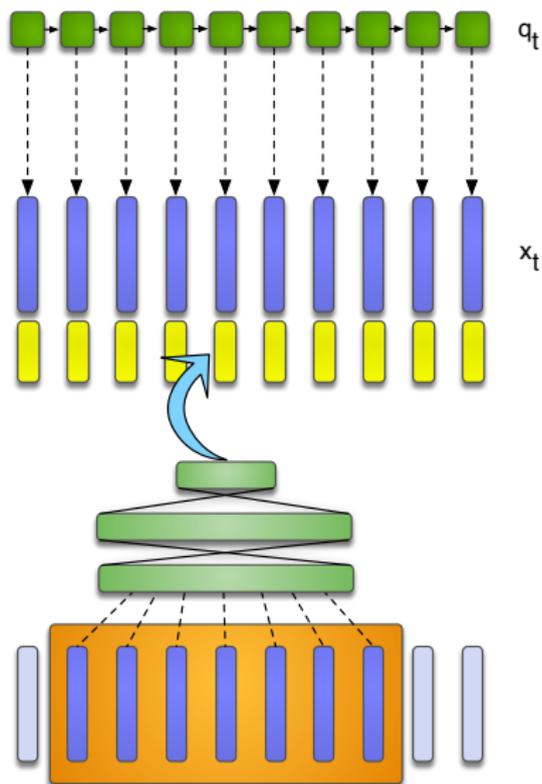
Tandem scheme:

- Basic idea: use the output probabilities from the NN as input features to standard CD-HMM-GMM system
- Combines the benefits of both:
  - NNs good at modelling wide acoustic contexts, correlated input features
  - HMM-GMMs good for speaker adaptation, modelling phonetic context, sequence-training
- NN output probabilities are *Gaussianised* by taking logs and decorrelating with PCA
- Early variants used purely NN features; later variants augmented the feature vector with standard acoustic features
- Can also use “bottleneck features” (narrow, intermediate NN layers)

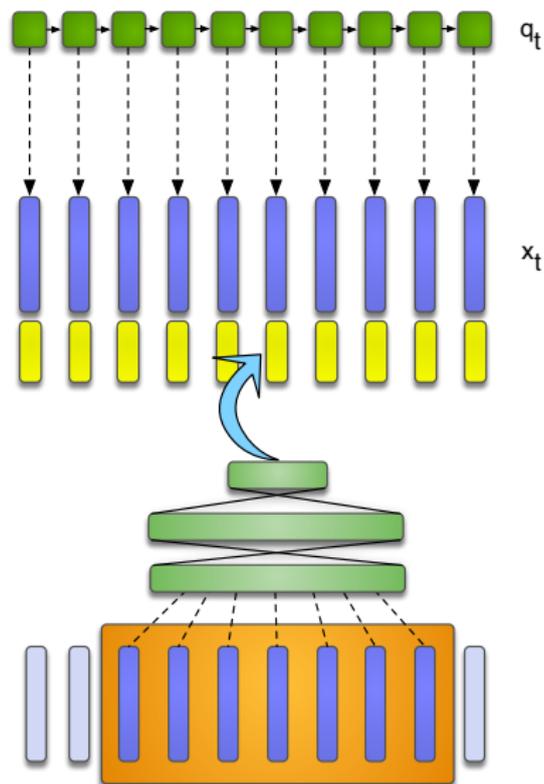
# Tandem scheme



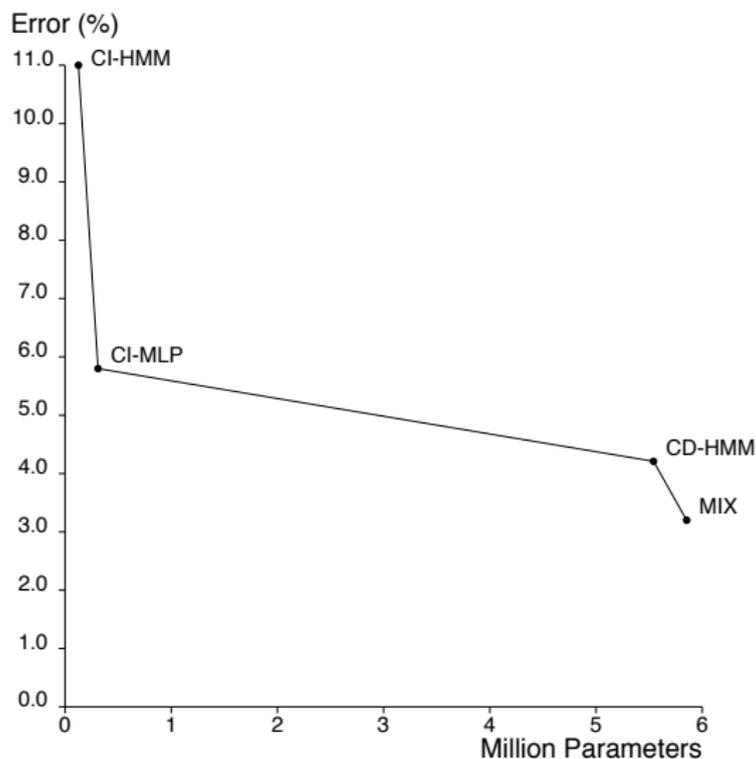
# Tandem scheme



# Tandem scheme

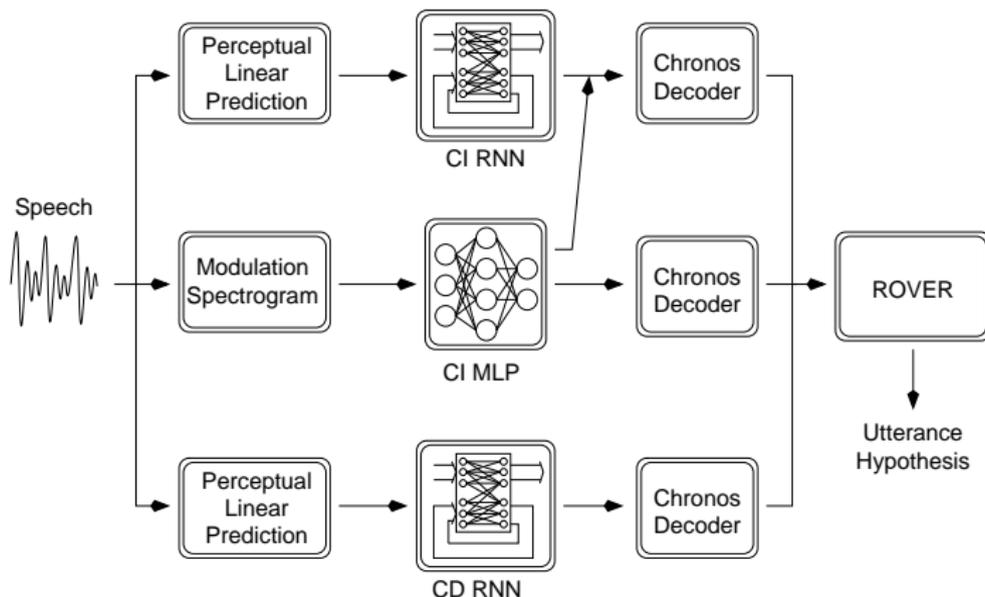


# Monophone HMM/NN hybrid system (1993)



Renals, Morgan, Cohen & Franco, ICASSP 1992

# Monophone HMM/NN hybrid system (1998)



- Broadcast news transcription (1998) – 20.8% WER
- (best GMM-based system, 13.5%)
- Cook et al, DARPA, 1999

# HMM/NN vs HMM/GMM

- Advantages of NN:
  - Can easily model **correlated features**
    - Correlated feature vector components (eg spectral features)
    - Input context – multiple frames of data at input
  - **More flexible** than GMMs – not made of (nearly) local components); GMMs inefficient for non-linear class boundaries

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  - **More flexible** than GMMs – not made of (nearly) local components); GMMs inefficient for non-linear class boundaries
- Disadvantages of NNs in the 1990s:
  - Context-independent (monophone) models, weak speaker adaptation algorithms
  - NN systems less complex than GMMs (fewer parameters):  
RNN –  $< 100k$  parameters, MLP –  $\sim 1M$  parameters
  - Computationally expensive - more difficult to parallelise training than GMM systems



# Features of the Cambridge system

	CU-HTK 2000
Base model	HMM-GMM
Acoustic context	$\Delta$ , $\Delta\Delta$ features, HLDA projection
Phonetic context	Tied state triphones & quinphones
Speaker adaptation	Gender-dependent models, VTLN, MLLR
Training criterion	ML + MMI sequence training
System architecture	6-pass system
Other features	Multi-system combination
Hub 2000 WER	<b>19.3%</b>

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No neural networks!

## Conversational Speech Transcription Using Context-Dependent Deep Neural Networks

Frank Seide<sup>1</sup>, Gang Li,<sup>1</sup> and Dong Yu<sup>2</sup>

<sup>1</sup>Microsoft Research Asia, Beijing, P.R.C.

<sup>2</sup>Microsoft Research, Redmond, USA  
{fseide, ganl, dongyu}@microsoft.com

### Abstract

We apply the recently proposed Context-Dependent Deep-Neural-Network HMMs, or CD-DNN-HMMs, to speech-to-text transcription. For single-pass speaker-independent recognition on the RT03S Fisher portion of phone-call transcription benchmark (Switchboard), the word-error rate is reduced from 27.4%, obtained by discriminatively trained Gaussian-mixture HMMs, to 18.5%—a 33% relative improvement.

CD-DNN-HMMs combine classic artificial-neural-network HMMs with traditional tied-state triphones and deep-belief-network pre-training. They had previously been shown to reduce errors by 16% relatively when trained on tens of hours of data using hundreds of tied states. This paper takes CD-DNN-

Table 3: Comparing different by HMM accuracy. 'nz' means 'non' for Hub5 '00 SWB.

acoustic model	#params	WER (r. chg.)
GMM 40 mix, BMMI	29.4M	27.6
CD-DNN 1 layer×4634 nodes	43.6M	26.0 (+10%)
+ 2×5 neighbor frames	45.1M	25.4 (-14%)
CD-DNN 7 layers×2048 nodes	45.1M	16.1 (-24%)
+ updated state alignment	45.1M	16.4 (-23%)
+ sparsification 66%	15.2M	16.1 (-24%)

16.1%

ception (MLP) and DNN and previous work on understanding which factors contribute most to the accuracy improvements achieved by the CD-DNN-HMMs.

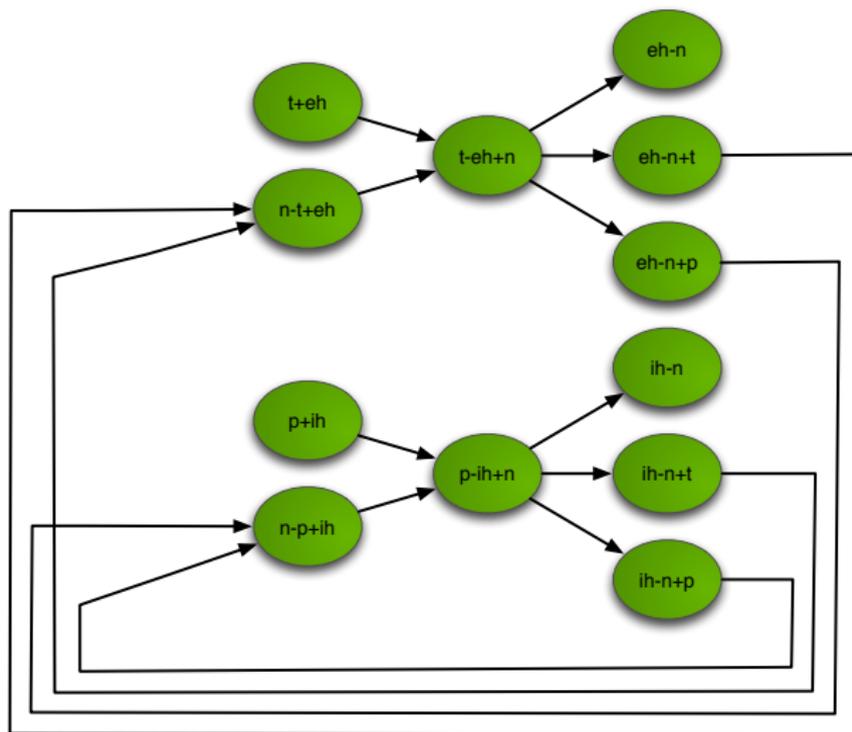
# Features of the Microsoft NN system

	Microsoft 2011
Base model	HMM-DNN
Acoustic context	11 frames directly modelled
Phonetic context	Tied state triphones
Speaker adaptation	None
Training criteria	Frame-level cross-entropy
System architecture	Single pass
Other features	Deep network architecture
Hub 2000 WER	<b>16.1%</b>

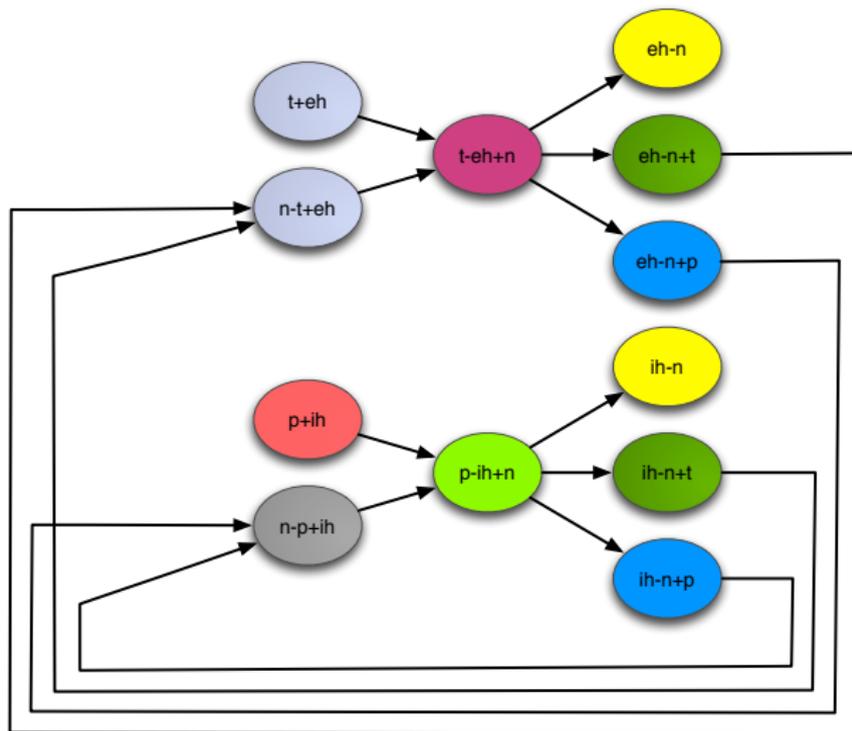
# Acoustic features for NN acoustic models

- GMMs: filter bank features (spectral domain) not used as they are strongly correlated with each other – would either require
  - full covariance matrix Gaussians
  - many diagonal covariance Gaussians
- DNNs do not require the components of the feature vector to be uncorrelated
  - Can directly use multiple frames of input context (this has been done in NN/HMM systems since 1990, and is crucial to make them work well)
  - Can potentially use feature vectors with correlated components (e.g. filter banks)
- Mel-scaled filter bank features (FBANK) found to result in greater accuracy than standard MFCCs, though higher resolution MFCCs are now used

# Recap: context-dependent units



# Recap: tied context-dependent units



## Modelling phonetic context (3)

- In the 1990s, this was considered hard (see earlier slides)
- But in 2011, a simple solution emerged: use state-tying from a GMM system

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### Context-Dependent Pre-Trained Deep Neural Networks for Large-Vocabulary Speech Recognition

George E. Dahl, Dong Yu, *Senior Member, IEEE*, Li Deng, *Fellow, IEEE*, and Alex Acero, *Fellow, IEEE*

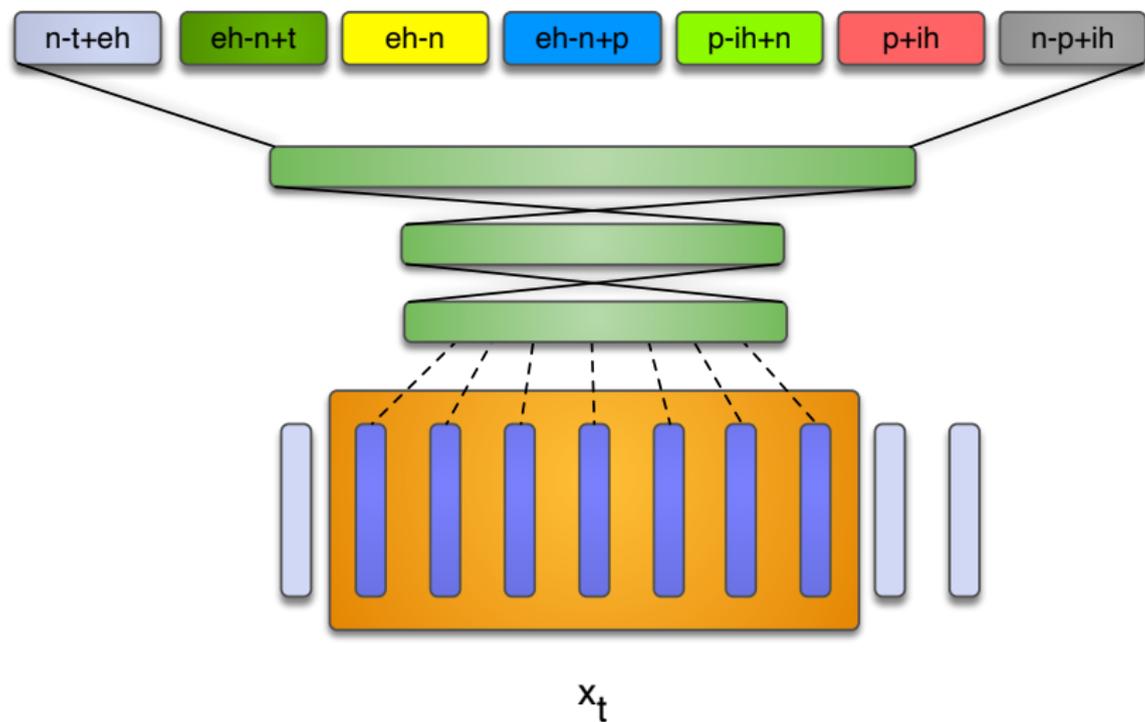
**Abstract**—We propose a novel context-dependent (CD) model for large-vocabulary speech recognition (LVSR) that leverages recent advances in using deep belief networks for phone recognition. We describe a pre-trained deep neural network hidden Markov model (DNN-HMM) hybrid architecture that trains the DNN to produce a distribution over senones (tied triphone states) as its output. The deep belief network pre-training algorithm is a robust and often helpful way to initialize deep neural networks generatively that

fields (CRFs) [18]–[20], hidden CRFs [21], [22], and segmental CRFs [23]). Despite these advances, the elusive goal of human level accuracy in real-world conditions requires continued, vibrant research.

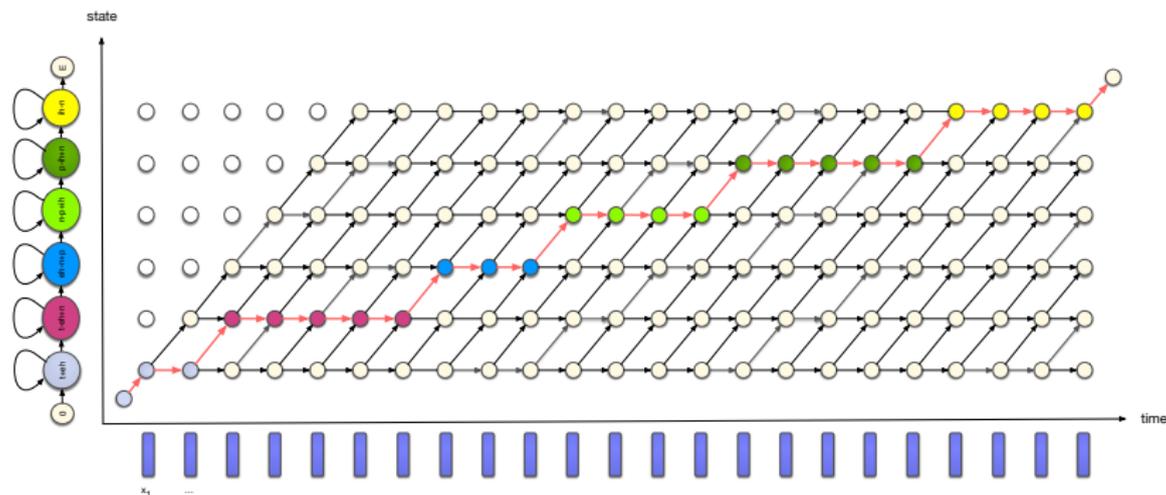
Recently, a major advance has been made in training densely connected, directed belief nets with many hidden layers. The resulting deep belief nets learn a hierarchy of nonlinear feature

# Context-dependent hybrid HMM/DNN

- First train a context-dependent HMM/GMM system on the same data, using a phonetic decision tree to determine the HMM tied states
- Perform Viterbi alignment using the trained HMM/GMM and the training data
- Train a neural network to map the input speech features to a label representing a context-dependent tied HMM state
  - So the size of the label set is thousands (number of context-dependent tied states) rather than tens (number of context-independent phones) or tens of thousands (number of full set of context-dependent phones)
  - Each frame is labelled with the Viterbi aligned tied state
- Train the neural network using gradient descent as usual
- Use the context-dependent scaled likelihoods obtained from the neural network when decoding



# Obtain labels with the Viterbi algorithm



# Summary

- DNN/HMM systems (hybrid systems) gave a significant improvement over GMM/HMM systems
- Compared with 1990s NN/HMM systems, DNN/HMM systems
  - model context-dependent tied states with a much wider output layer
  - are deeper – more hidden layers
  - can use correlated features (e.g. FBANK) or higher resolution MFCCs
- Background reading:
  - N Morgan and H Bourlard (May 1995). “Continuous speech recognition: Introduction to the hybrid HMM/connectionist approach”, *IEEE Signal Processing Mag.*, **12**(3), 24–42.  
<http://ieeexplore.ieee.org/document/382443>
  - A Mohamed et al (2012). “Understanding how deep belief networks perform acoustic modelling”, Proc ICASSP-2012.  
[http://www.cs.toronto.edu/~asamir/papers/icassp12\\_dbn.pdf](http://www.cs.toronto.edu/~asamir/papers/icassp12_dbn.pdf)