

Reinforcement Learning in the Brain (Overview)

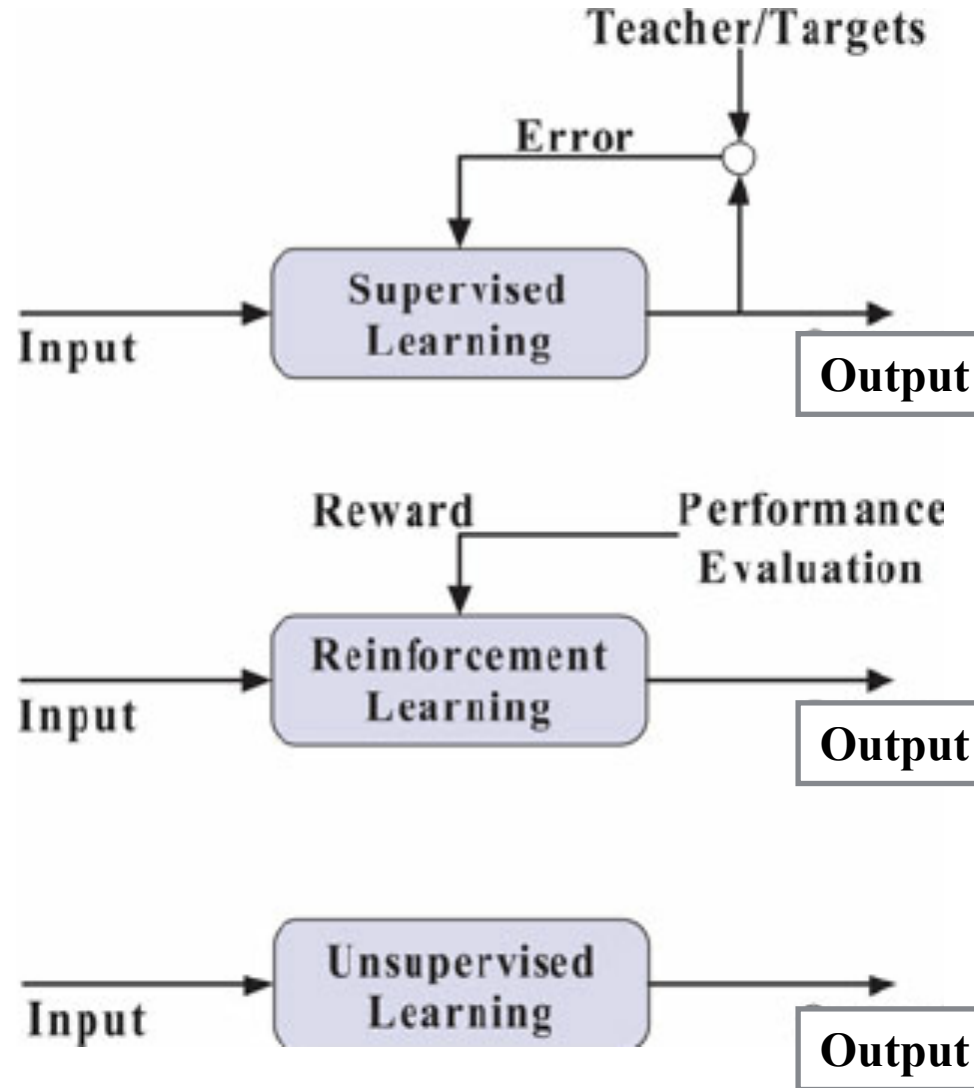
Peggy Seriès, IANC
Informatics, University of Edinburgh, UK

pseries@inf.ed.ac.uk

CCN Lecture 9

Reinforcement learning (RL):

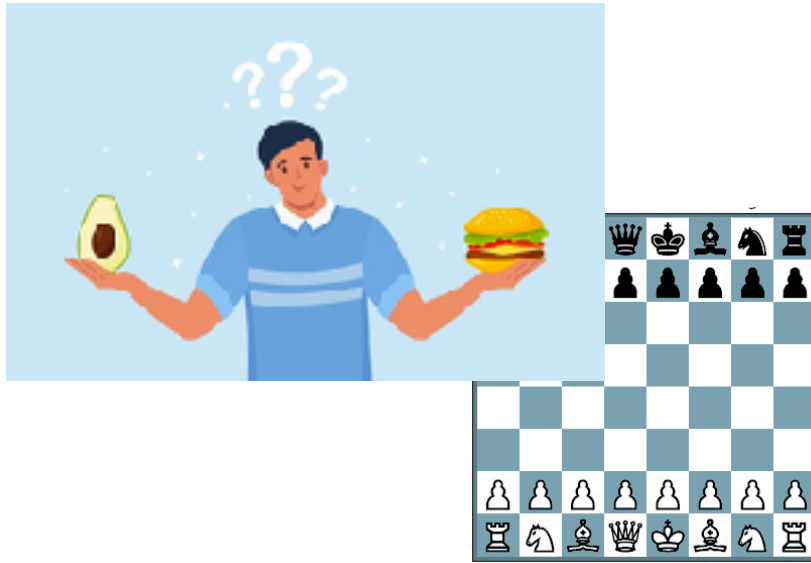
- an area of machine learning inspired by behaviorist psychology, concerned with how software agents ought to take actions in an environment so as to maximize some notion of cumulative reward.
- thought to be a good model of how learning is occurring in the brain.



Contrasted with Supervised, and Unsupervised learning

Maximizing Reward as a guide to decision-making

- Key to decision making at all levels
- Reinforcement learning : **maximize reward** and **minimize punishments**; Sutton 1978; Sutton & Barto, 1990, 1998.
- Why is this hard? (1) rewards/ punishment may be **delayed**; (2) outcome may depend on **series of actions** (credit assignment problem)
- Needs learning of **predictions** of events and actions

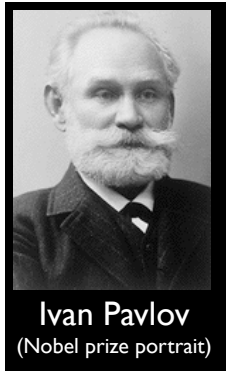


SCHOOL IS HELL
BUT
IT BEATS WORKING

SHOULD YOU GO
TO GRAD SCHOOL?
A WEE TEST

- | T | F | |
|--------------------------|--------------------------|--|
| <input type="checkbox"/> | <input type="checkbox"/> | I AM A COMPULSIVE NEUROTIC. |
| <input type="checkbox"/> | <input type="checkbox"/> | I LIKE MY IMAGINATION CRUSHED INTO DUST. |
| <input type="checkbox"/> | <input type="checkbox"/> | I ENJOY BEING A PROFESSOR'S SLAVE. |
| <input type="checkbox"/> | <input type="checkbox"/> | MY IDEA OF A GOOD TIME IS USING JARGON AND CITING AUTHORITIES. |
| <input type="checkbox"/> | <input type="checkbox"/> | I FEEL A DEEP NEED TO CONTINUE THE PROCESS OF AVOIDING LIFE. |

Animals learn predictions -- Pavlovian conditioning



1849-1936



- Animals learn predictions
- **Classical (aka “Pavlovian”) conditioning**: pairing of a conditioned stimulus (bell, CS) with a unconditioned stimulus (food, US)
- conditioned suppression, freezing to tone paired with punishment

<http://www.youtube.com/watch?v=ZlZekx1P1g4>

- autoshaping, bird pecking on light that has been paired with food

<http://www.youtube.com/watch?v=cacwAvvg8EA>

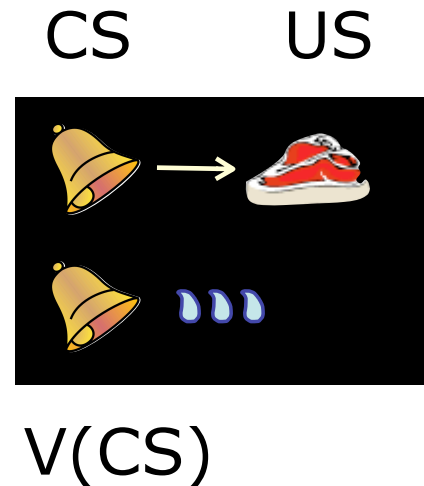
Behaviorism: John Watson (1913) proposed that the process of classical conditioning (based on Pavlov’s observations) was able to explain all aspects of human psychology.

Rescorla & Wagner Model of Classical Conditioning (1972)

In 1972, Rescorla & Wagner proposed mathematical model to explain amount of learning that occurs on each trial of Pavlovian learning, when a signal (conditioned stimulus: CS) is paired with a subsequent stimulus (unconditioned stimulus: US).

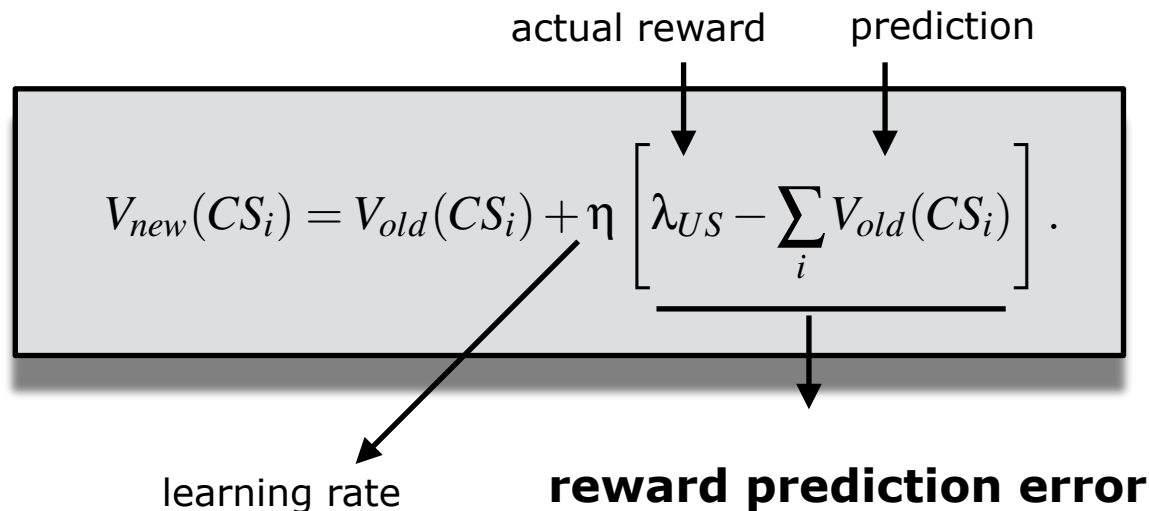
Describes development of **associative strength V** between objects or events and reward or punishment, recognising that:

1. **Learning** will occur if what happens on the trial **does not match the expectation** of the organism (**surprise !**),
2. The expectation on any given trial is based on the predictive value of **all of the stimuli** present.



Rescorla & Wagner model of classical conditioning (1972)

- Change in value of **associative strength** $V(\text{CS})$ is proportional to the difference between actual outcome λ_{US} and predicted outcome $\sum_i V_{old}(\text{CS}_i)$.
- The idea: **error-driven learning**: Learning occurs only when events violate expectations.



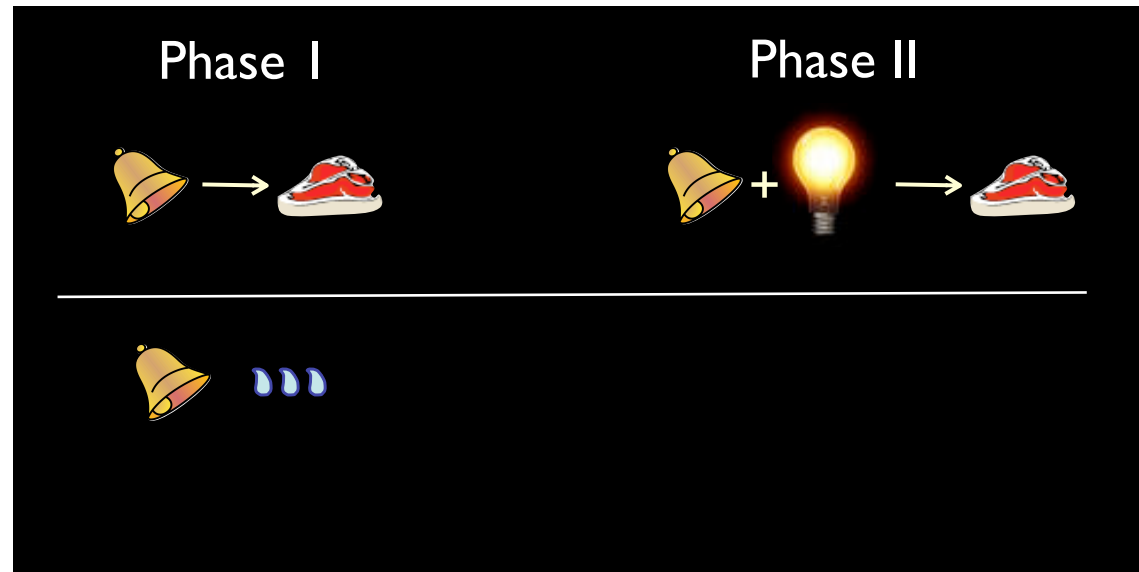
- **Most influential model of animal learning**, explains puzzling behavioural phenomena such as blocking, overshadowing and conditioned inhibition.

How do we know that animals use an error-correcting rule ?



Leon Kamin
(1917-2017)

- (Kamin) Blocking: Adding a second stimulus

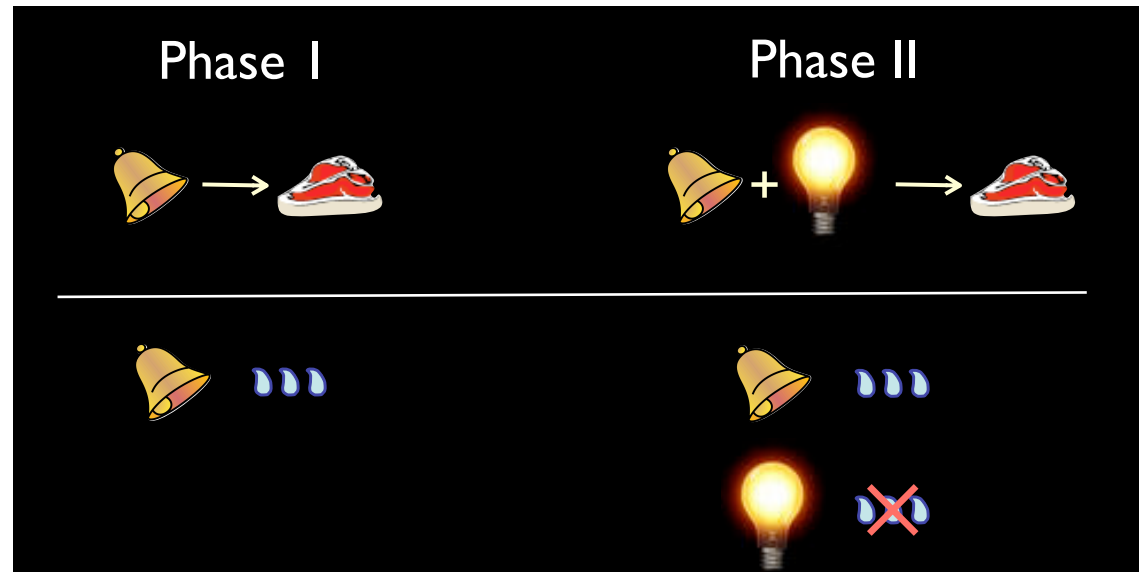


How do we know that animals use an error-correcting rule ?



Leon Kamin
(1917-2017)

- (Kamin) Blocking: Why does the light not make the animal salivate?



- Interpretation: the bell fully predicts the food and the presence of the light adds no new predictive information -- therefore no association develops to the light.

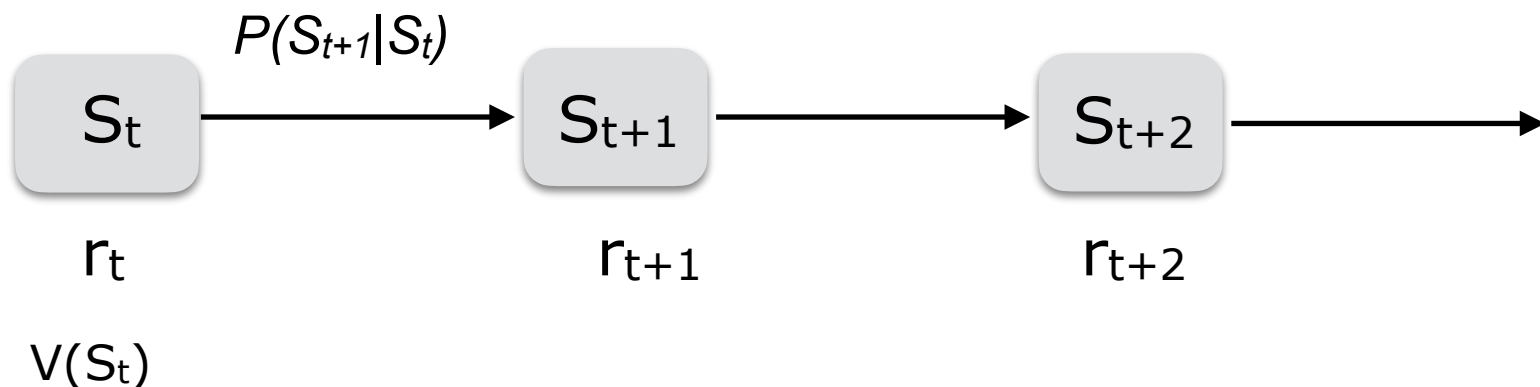
Limitations of the Rescorla & Wagner Model

- Does not extend to **2d order conditioning**, i.e. $A \rightarrow B \rightarrow \text{reward}$; where A gains reward predictive value
 - Basic unit of learning = conditioning trial as **discrete** temporal object
This fails to account for the temporal relations between CS and US stimuli within a trial
- **Temporal Difference (TD) learning**, first described by Sutton (1988)
- a means to overcome these limitations
 - extension of Rescorla-Wagner to take into account timing of events.

Richard Sutton



Temporal Difference (TD) learning (1)



- Consider a succession of **states** S , following each other with $P(S_{t+1}|S_t)$
- **Rewards** observed in each state with probability $P(r|S_t)$

(This is a *Markov Decision Process*)

- Useful quantity to predict is the **expected sum of all future rewards**, given current state S_t , = value of state S , **$V(S_t)$**

$$V(S_t) = E \left[r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots \mid S_t \right] = E \left[\sum_{i=t}^{\infty} \gamma^{i-t} r_i \mid S_t \right]$$

where E denotes expected value (or mean) and gamma the discount factor

Temporal Difference (TD) learning (1)

$$V(S_t) = E [r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots | S_t] = E \left[\sum_{i=t}^{\infty} \gamma^{i-t} r_i \middle| S_t \right]$$

- **Discount factor** introduced to make sure that the sum is finite, but also humans and animals prefer earlier rewards to later ones
- Incorporating probabilities $P(S_{t+1}|S_t)$ and $P(r|S_t)$, we get **recursive form**

$$\begin{aligned} V(S_t) &= E[r_t | S_t] + \gamma E[r_{t+1} | S_t] + \gamma^2 E[r_{t+2} | S_t] + \dots = \\ &= E[r_t | S_t] + \gamma \sum_{S_{t+1}} P(S_{t+1} | S_t) (E[r_{t+1} | S_{t+1}] + \gamma E[r_{t+2} | S_{t+1}] + \dots) = \\ &= P(r | S_t) + \gamma \sum P(S_{t+1} | S_t) V(S_{t+1}) \end{aligned}$$

- Goal of TD learning = learn the values $V(S_t)$.

Temporal Difference (TD) learning (2)

- When estimated values are incorrect, there is a discrepancy between 2 sides of equation: **prediction error**:

$$\delta_t = P(r|S_t) + \gamma \sum_{S_{t+1}} P(S_{t+1}|S_t) V(S_{t+1}) - V(S_t).$$

- prediction error is a natural signal for improving estimates $V(S_t)$, giving:

$$V(S_t)_{new} = V(S_t)_{old} + \eta \cdot \delta_t,$$

- = Optimal learning rule, basis of “**dynamic programming**”.
- One problem: assumes knowledge of $P(S_{t+1}|S_t)$ and $P(r|S_t)$ which is unreasonable in basic learning situations.
- **Model-free Approximation** which can be formally justified (sampling):

$$\delta_t = r_t + \gamma V(S_{t+1}) - V(S_t)$$

~ **current reward+next prediction - current prediction**

Temporal Difference (TD) learning (3)

- Resulting learning rule:

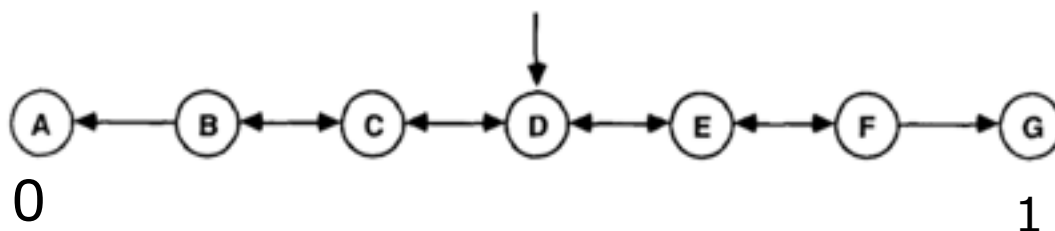
$$V_{new}(S_t) = V_{old}(S_t) + \eta(r_t + \gamma V_{old}(S_{t+1}) - V_{old}(S_t)).$$

current reward+next prediction - current prediction

- This is **TD(0) learning rule** as proposed by Sutton & Barton (1990).
- reduces to **Rescorla-Wagner model** if only one step i.e. $V(S_{t+1})=0$.

$$V_{new}(S_t) = V_{old}(S_t) + \eta(r_t - V_{old}(S_t)).$$

TD in practice



e.g. π = random walk, at each state go left or right with 50% chance

Input: the policy π to be evaluated

Initialize $V(s)$ arbitrarily (e.g., $V(s) = 0, \forall s \in \mathcal{S}^+$)

Repeat (for each episode):

 Initialize S

 Repeat (for each step of episode):

$A \leftarrow$ action given by π for S

 Take action A ; observe reward, R , and next state, S'

$V(S) \leftarrow V(S) + \alpha[R + \gamma V(S') - V(S)]$

$S \leftarrow S'$

 until S is terminal

Figure 6.1: Tabular TD(0) for estimating v_π .

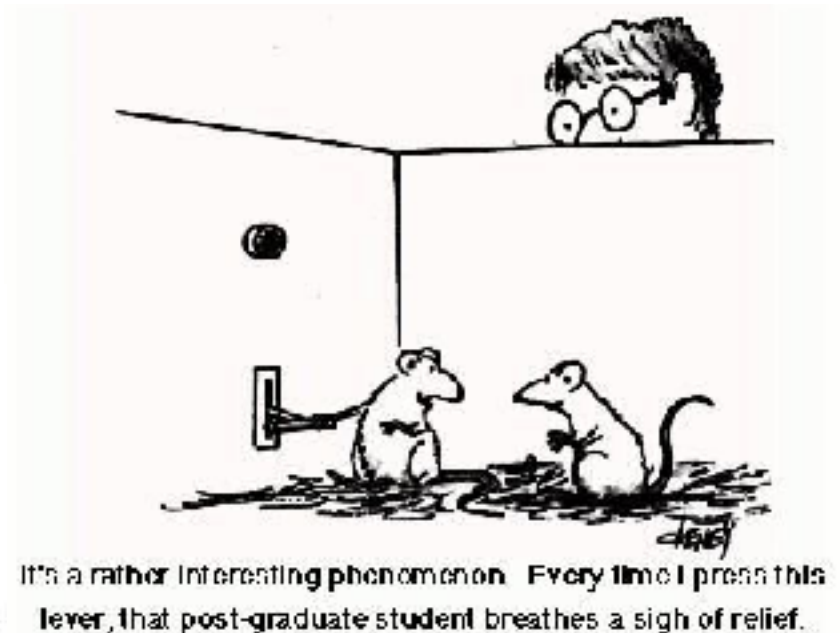
Sutton & Barton (1990).

Instrumental conditioning: adding control

- Animals not only learn associations between stimuli and reward but also between **actions and reward**
- Learning to select actions that will increase the probability of rewarding events and decrease the probability of aversive events.
- Rat lever pressing in boxes -- **operant conditioning** (Skinner)



Skinner
1904-1990



Actor/Critic Methods

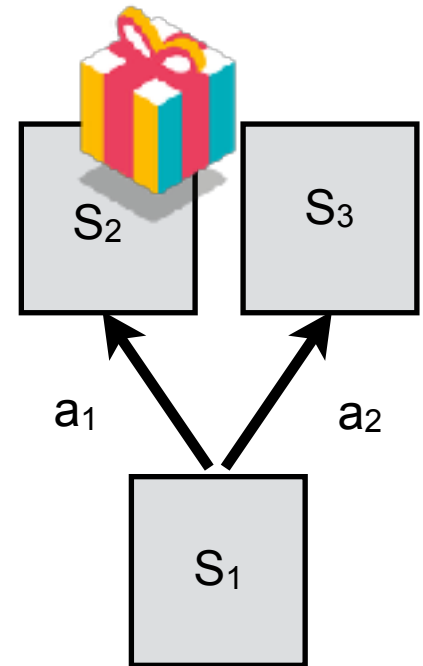
- How can such action selection be learned?
- Barto (1983): credit assignment problem can be solved by a learning system comprised of 2 neurons-like elements:
 - the **critic**, uses TD learning to construct **values of states**
 - the **actor**, learn to select **actions** at each state using prediction error.

Idea: if positive prediction error is encountered, current action should be repeated.

Learning of **policies**

$$\pi(S, a) = p(a|S),$$

$$\pi(S, a)_{new} = \pi(S, a)_{old} + \eta_{\pi} \delta_t$$



Q-learning

- Watkins (1989)
- Alternative: explicitly learn the predictive value (future expected rewards) of **taking an action at each state** = learn the value of **state-action pairs** $Q(S,a)$
- Learning rule:

$$Q(S_t, a_t)_{new} = Q(S_t, a_t)_{old} + \eta \delta_t$$

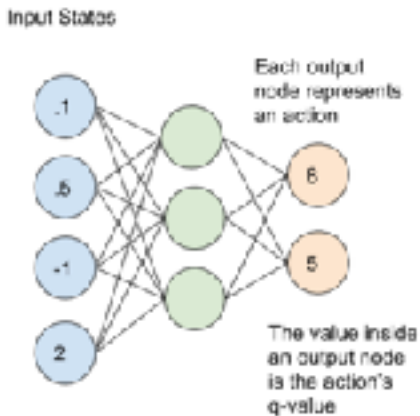
- Q prediction error:

$$\delta_t = r_t + \max_a \gamma Q(S_{t+1}, a) - Q(S_t, a_t)$$

~ **current reward+ prediction of next best action- current prediction**

- SARSA algorithm a slightly different version

Machine learning applications of Q learning (deep Q learning)



LETTER

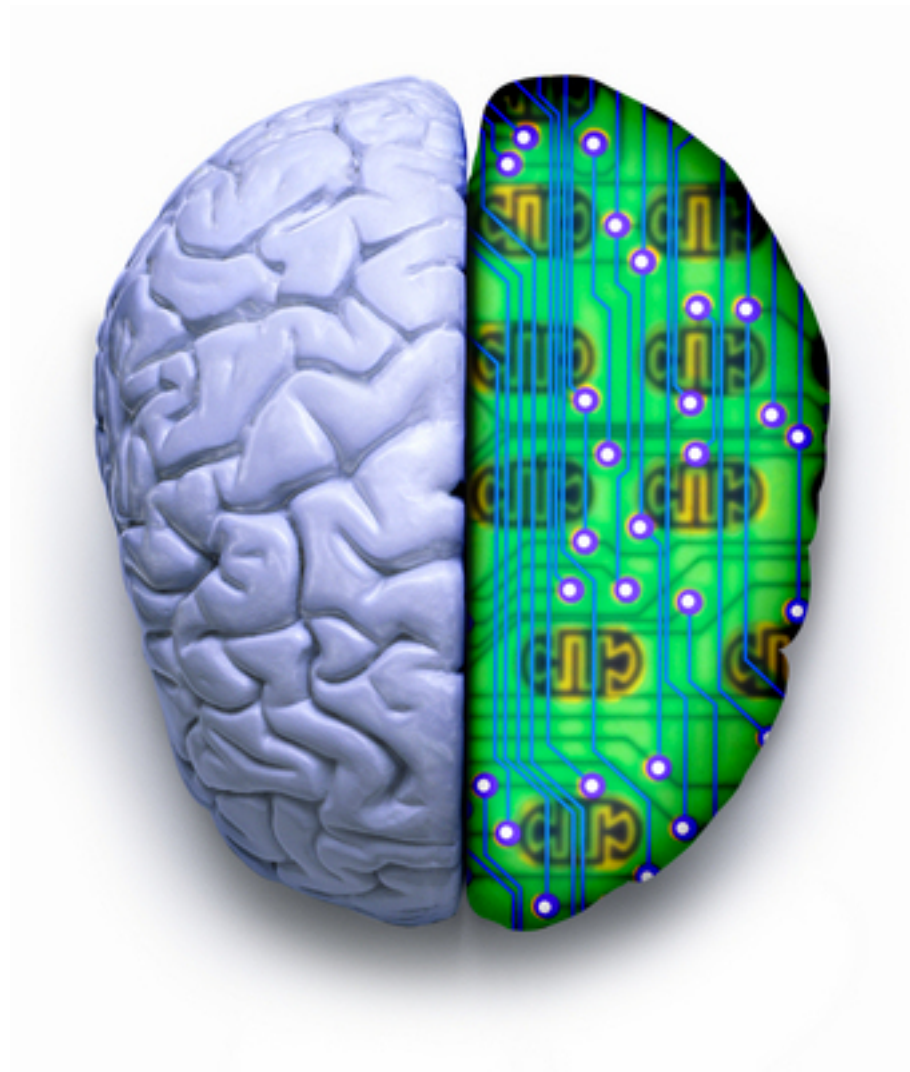
doi:10.1038/nature14235

Human-level control through deep reinforcement learning

Volodymyr Mnih¹*, Koray Kavukcuoglu¹*, David Silver¹*, Andrej A. Rusu¹, Joel Veness¹, Marc G. Bellemare¹, Alex Graves¹, Martin Riedmiller¹, Andreas K. Bjorck¹, Georg Ostrovski¹, Stig Petersen¹, Charles Beattie¹, Amir Sadik¹, Ioannis Antonoglou¹, Helen King¹, Dharmash Kumar¹, Duan Wierstra¹, Shane Legg¹ & Demis Hassabis¹

<https://www.youtube.com/watch?v=V1eYniJ0Rnk>

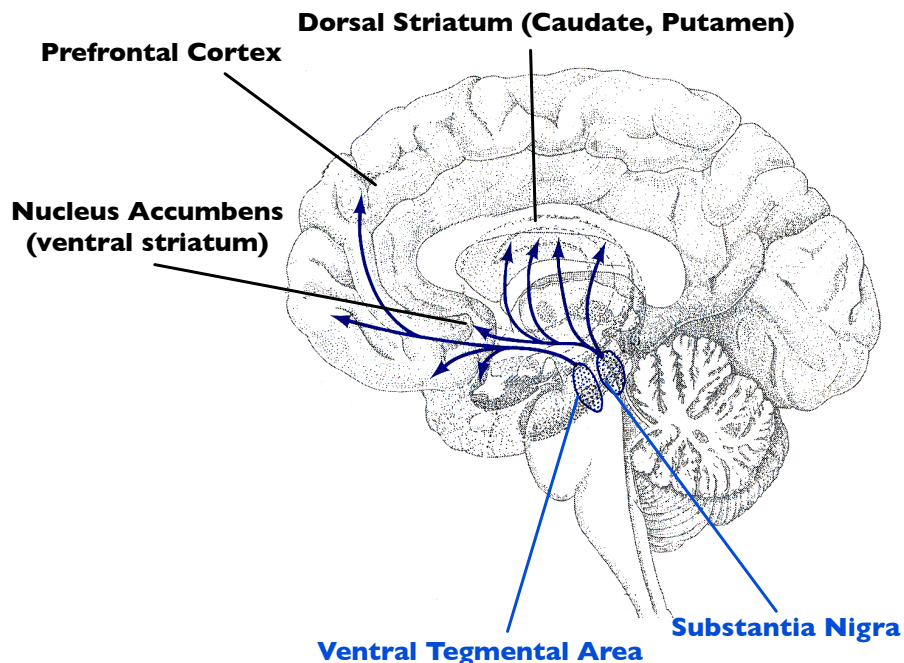
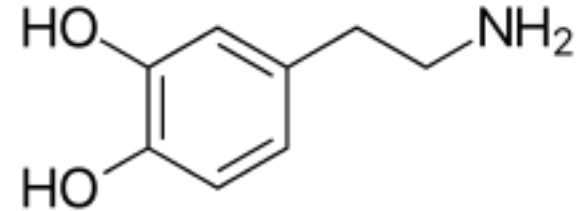
A recent application of Q-learning to deep learning, by Google DeepMind has been successful at playing some Atari 2600 games at expert human levels.



Does the brain do anything like that ?

- “the largest success of computational neuroscience”,
dopamine and prediction error

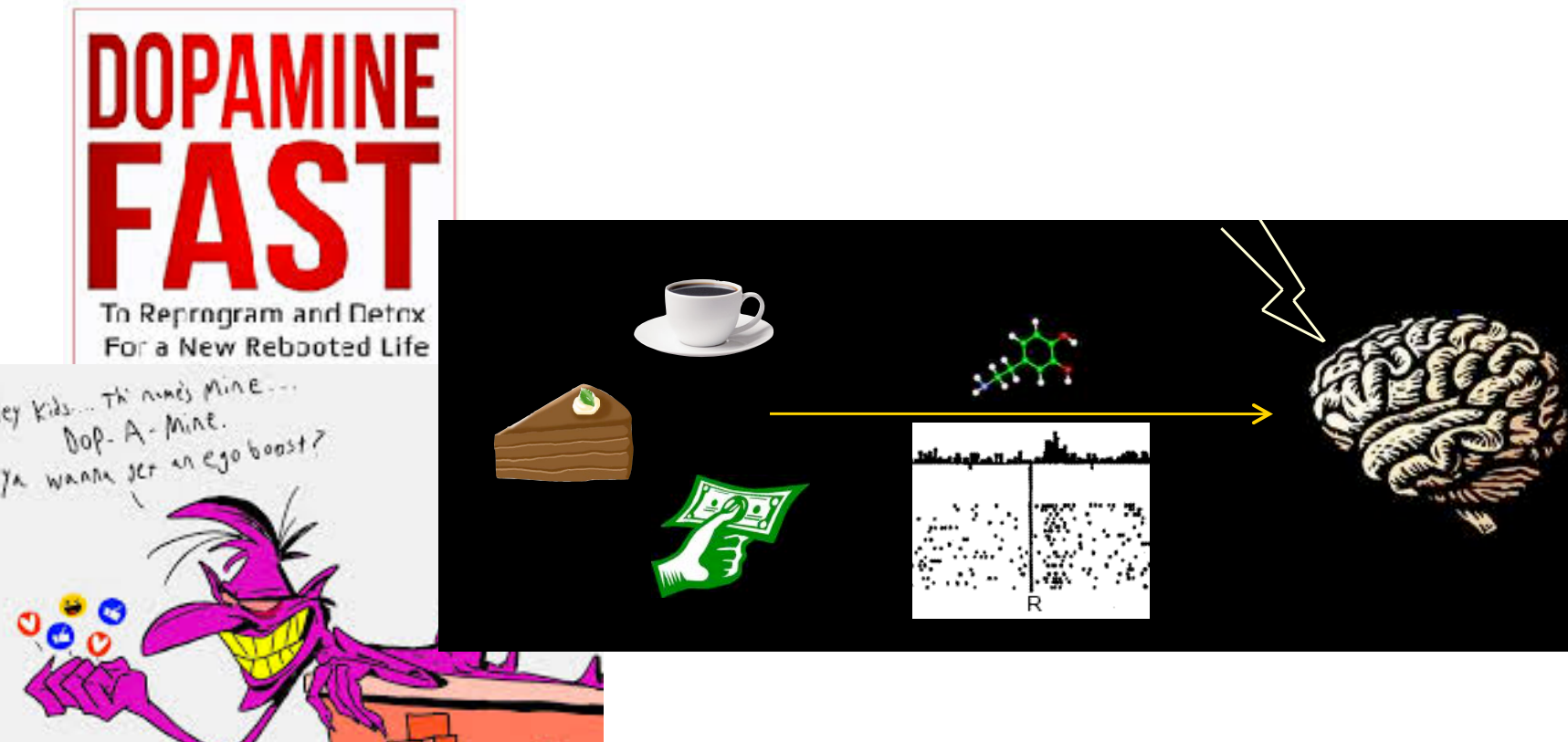
What is Dopamine ?



- A neurotransmitter
- Dopaminergic neurons in Ventral Tegmental Area (**VTA**) and Substantia Nigra (**SN**), both in the midbrain
- **Parkinson's** Disease : motor control/ initiation
- **Addiction**, gambling, natural rewards
- also involved in : working memory, novel situations, ADHD, schizophrenia, Tourette.

Former idea: Dopamine signals Reward (Wise, '80s)

- Initial idea: dopamine represent **reward signals**
- brain self stimulation by rats <http://www.youtube.com/watch?v=7HbAFYiejvo>
- antipsychotic drugs (dopamine antagonists) cause anhedonia
- 'wanting' more than 'liking'
- dopamine important for reward mediated conditioning



New idea: Phasic Dopamine signals Prediction Error

A Neural Substrate of Prediction and Reward

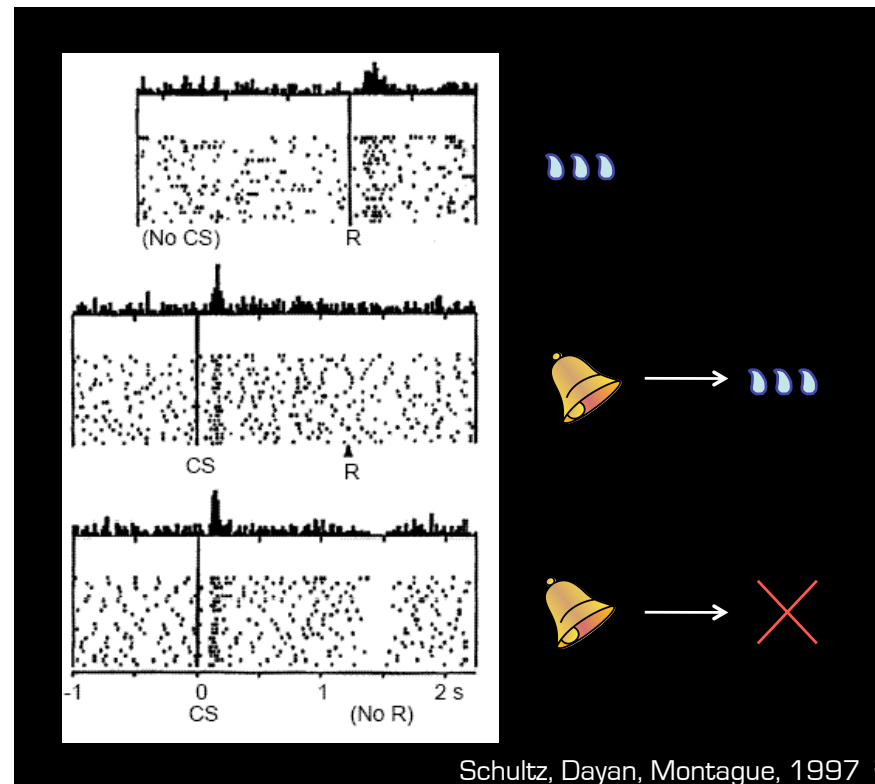
Wolfram Schultz, Peter Dayan, P. Read Montague*

The capacity to predict future events permits a creature to detect, model, and manipulate the causal structure of its interactions with its environment. Behavioral experiments suggest that learning is driven by changes in the expectations about future salient events such as rewards and punishments. Physiological work has recently complemented these studies by identifying dopaminergic neurons in the primate whose fluctuating output apparently signals changes or errors in the predictions of future salient and rewarding events. Taken together, these findings can be understood through quantitative theories of adaptive optimizing control.

- Schultz et al 90s
- Monkeys underwent simple instrumental or pavlovian conditioning
- Disappearance of dopaminergic response at reward delivery after learning
- If reward is not presented, response depression below basal firing at expected time of reward.

Dopamine Response

= $\text{Reward Occurred} - \text{Reward Predicted}$
= prediction error



Schultz, Dayan, Montague, 1997



PETER DAYAN

RAY DOLAN

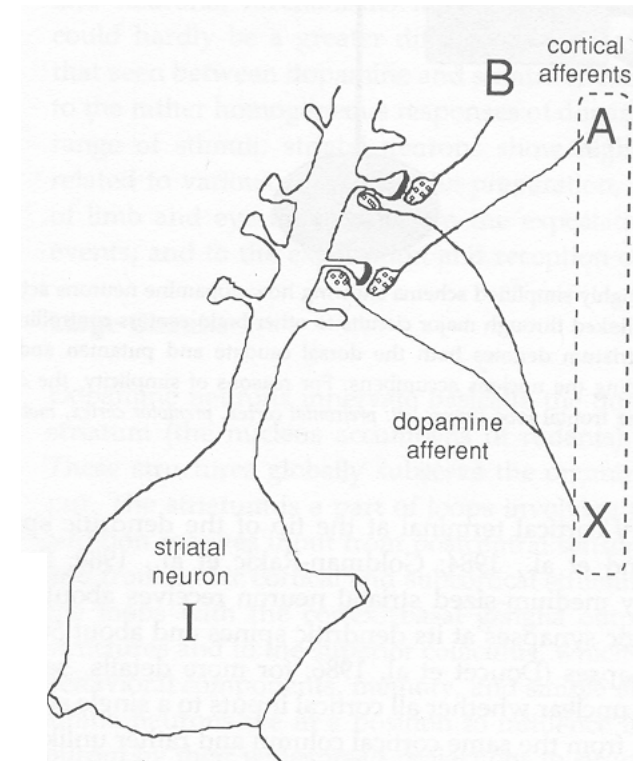
WOLFRAM SCHULTZ

THE BRAIN PRIZE 2017

<https://speakingofresearch.com/2017/03/06/winners-of-2017-brain-prize-announced-peter-dayan-ray-dolan-and-wolfram-schultz/>

Dopamine and Prediction

- The idea: dopamine encodes **prediction error** (Montague, Dayan, Barto, 1996)
Teaching signal, crucial for learning
- Provided **normative basis** for understanding not only when dopamine neurons fire when they do, but also why, and what the **function** of these firing might be.
- Evidence for **dopamine-dependent, or dopamine-gated plasticity** in synapses between cortex and striatum.



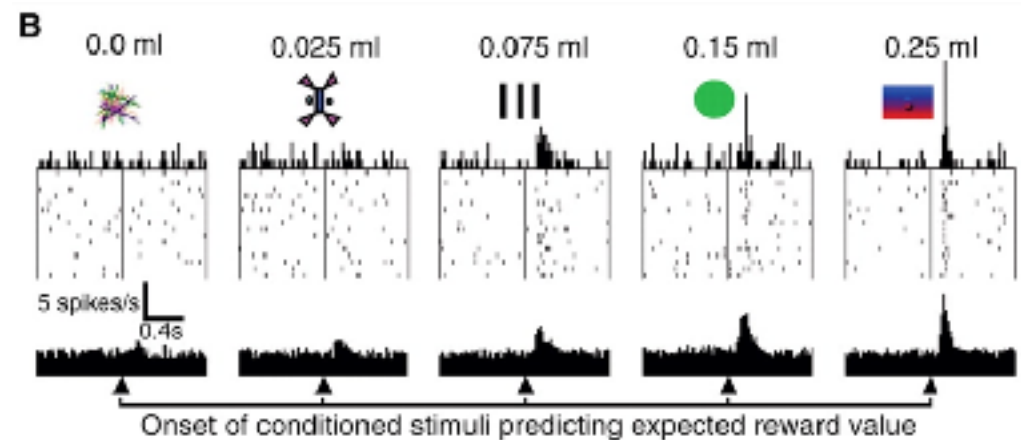
Testing that dopamine signals prediction error

- Is the size of response at onset of CS proportional to reward size?
- Recording of midbrain dopaminergic neurons in 2 macaque monkeys, different visual stimuli predict different amount of juice reward (Tobler et al, *Science* 2005).

Adaptive Coding of Reward Value by Dopamine Neurons

Philippe N. Tobler, Christopher D. Fiorillo,* Wolfram Schultz†

It is important for animals to estimate the value of rewards as accurately as possible. Because the number of potential reward values is very large, it is necessary that the brain's limited resources be allocated so as to discriminate better among more likely reward outcomes at the expense of less likely outcomes. We found that midbrain dopamine neurons rapidly adapted to the information provided by reward-predicting stimuli. Responses shifted relative to the expected reward value, and the gain adjusted to the variance of reward value. In this way, dopamine neurons maintained their reward sensitivity over a large range of reward values.



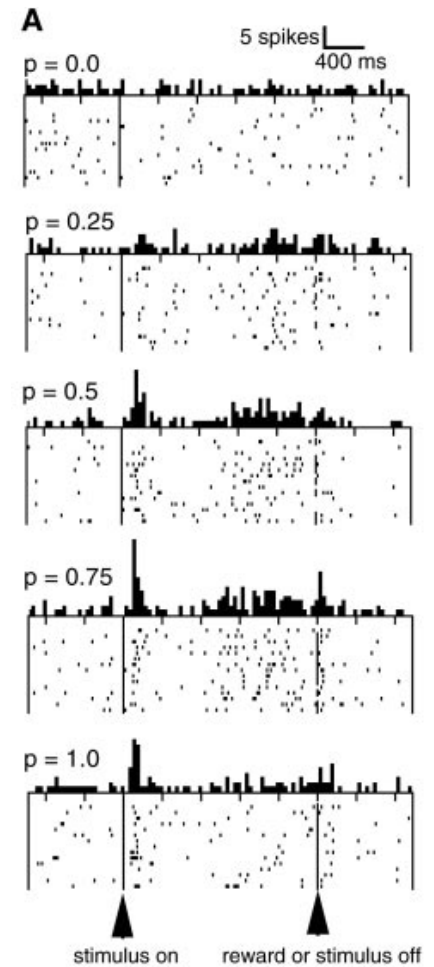
Testing that dopamine signals prediction error

- checking that size of response at onset of CS is proportional to **reward probability** (Fiorillo et al, Science 2003)

Discrete Coding of Reward Probability and Uncertainty by Dopamine Neurons

Christopher D. Fiorillo,* Philippe N. Tobler, Wolfram Schultz

Uncertainty is critical in the measure of information and in assessing the accuracy of predictions. It is determined by probability P , being maximal at $P = 0.5$ and decreasing at higher and lower probabilities. Using distinct stimuli to indicate the probability of reward, we found that the phasic activation of dopamine neurons varied monotonically across the full range of probabilities, supporting past claims that this response codes the discrepancy between predicted and actual reward. In contrast, a previously unobserved response co-varied with uncertainty and consisted of a gradual increase in activity until the potential time of reward. The coding of uncertainty suggests a possible role for dopamine signals in attention-based learning and risk-taking behavior.



Using fMRI to visualise prediction errors in humans

- **Model-driven analysis** -- search the brain for predicted **hidden variables** that should control learning:
- 1) collect behavioural data in fMRI scanner
- 2) fit a model, e.g. TD or Rescorla Wagner, to subjects' performance;
- 3) Once best-fitting model parameters have been found, then the different model components (time series, e.g. values and prediction error) can be regressed against the fMRI data.

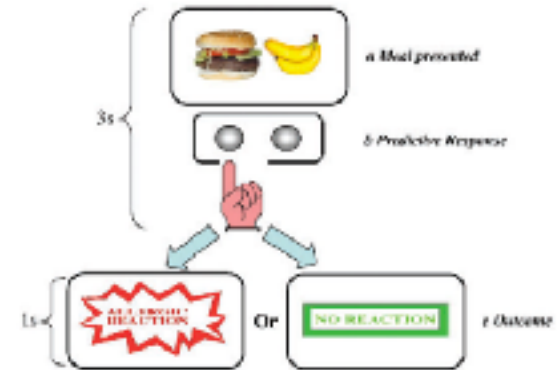
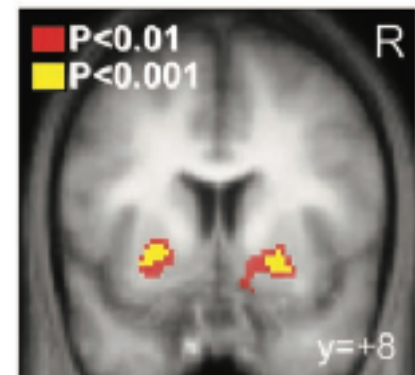
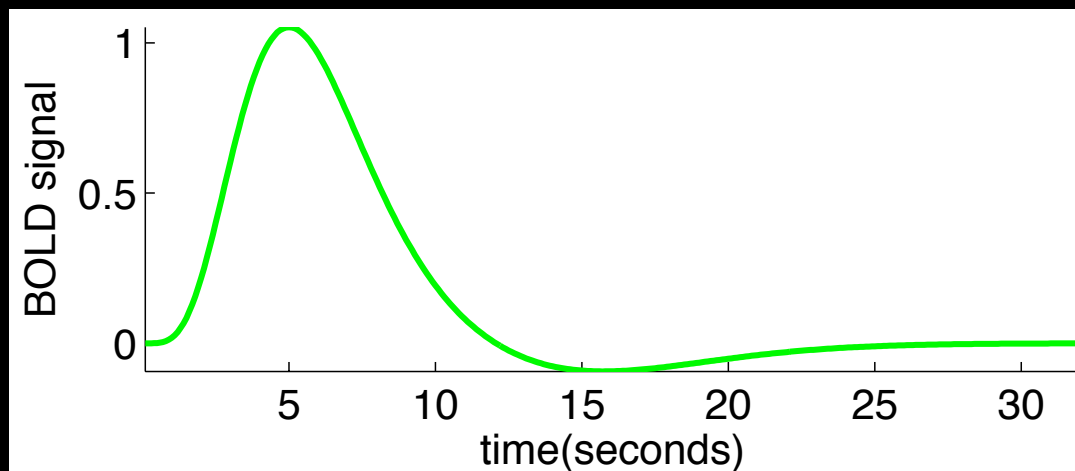
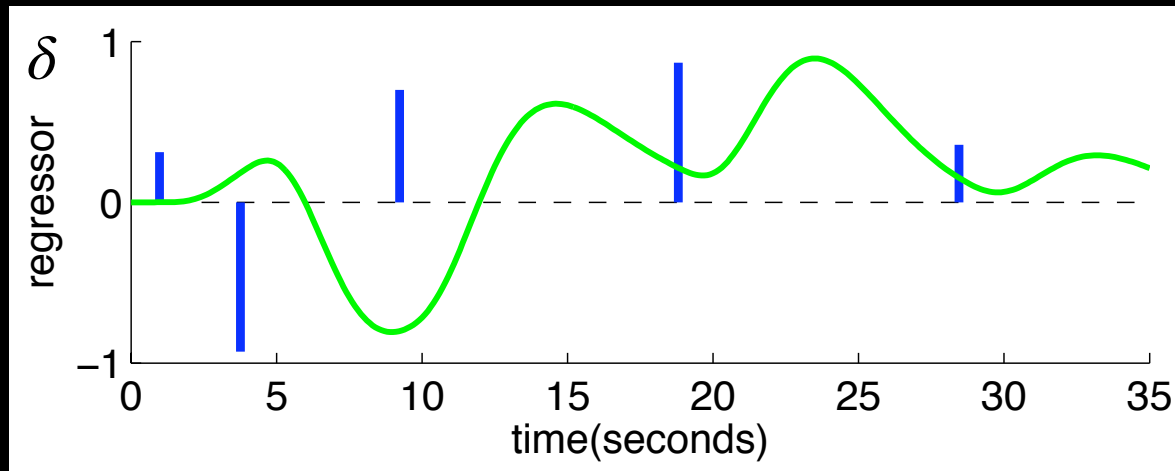


Fig. 1. Trial structure. On each trial, subjects were presented with a meal that their patient had eaten, and then they made a predictive response. Finally they were informed of the effect of that meal on their patient.

$$V_{new}(CS_i) = V_{old}(CS_i) + \eta \left[\lambda_{US} - \sum_i V_{old}(CS_i) \right].$$



short aside: functional magnetic resonance imaging (fMRI)



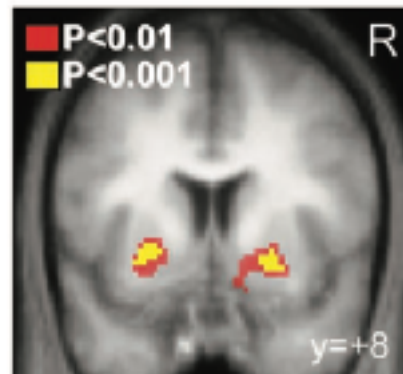
Using fMRI to visualise prediction errors

- **Prediction errors signals found**

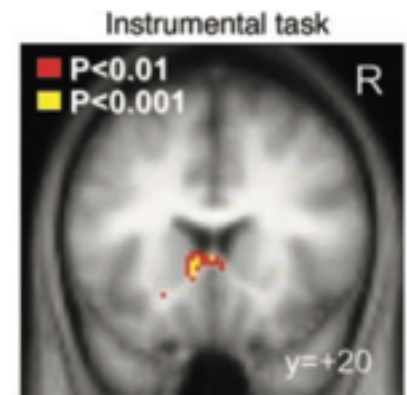
in nucleus accumbens (part of striatum) and orbito-frontal cortex, both major dopaminergic targets.

- O'Doherty et al (2004): fMRI correlates of prediction error signals can be dissociated in dorsal and ventral striatum, according to whether instrumental vs pavlovian conditioning,
-- supporting an **Actor/Critic architecture**.

ventral striatum activity
found in both Pavlovian
and instrumental task



dorsal striatum activity
found only in
instrumental task



- Model-based fMRI opens the door to investigating decision-making and reward signals differences in mental illness, e.g.

doi:10.1093/brain/awm173

Brain (2007), 130, 2387–2400

Disrupted prediction-error signal in psychosis: evidence for an associative account of delusions

P. R. Corlett,¹ G. K. Murray,^{1,2} G. D. Honey,¹ M. R. F. Aitken,³ D. R. Shanks,⁴ T. W. Robbins,³ E. T. Bullmore,^{1,2} A. Dickinson³ and P. C. Fletcher¹

- Frontal cortex responses in the patient group were suggestive of disrupted prediction-error processing.
- Across subjects, the extent of disruption was significantly related to an individual's propensity to delusion formation.
- Delusions as a consequence of abnormal learning.

Summary

- Optimal learning depends on prediction and control
- The problem: prediction of future reward (or punishment)
- The algorithm: TD learning (or variants)
Update values so as to minimise prediction error.
- Neural implementation: phasic dopamine as prediction error signal.
dopamine-dependent learning in cortico-striatal synapses in basal ganglia
- RL has revolutionised how we think of learning in the brain.
Implications for the understanding of disorders, such as Parkinson's and schizophrenia, as well as addiction, depression and more..