# Networks of Neurons (1 of 2)
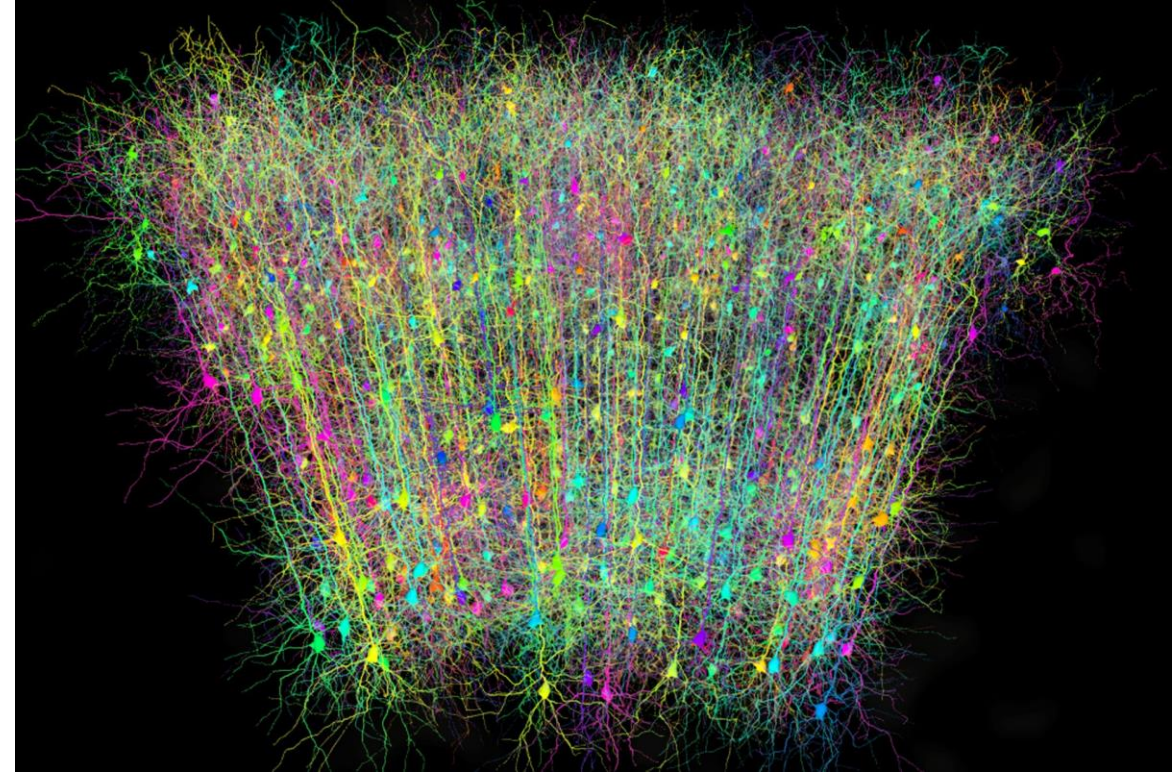
Angus Chadwick

School of Informatics, University of Edinburgh, UK

Computational Neuroscience (Lecture 11, 2024/2025)
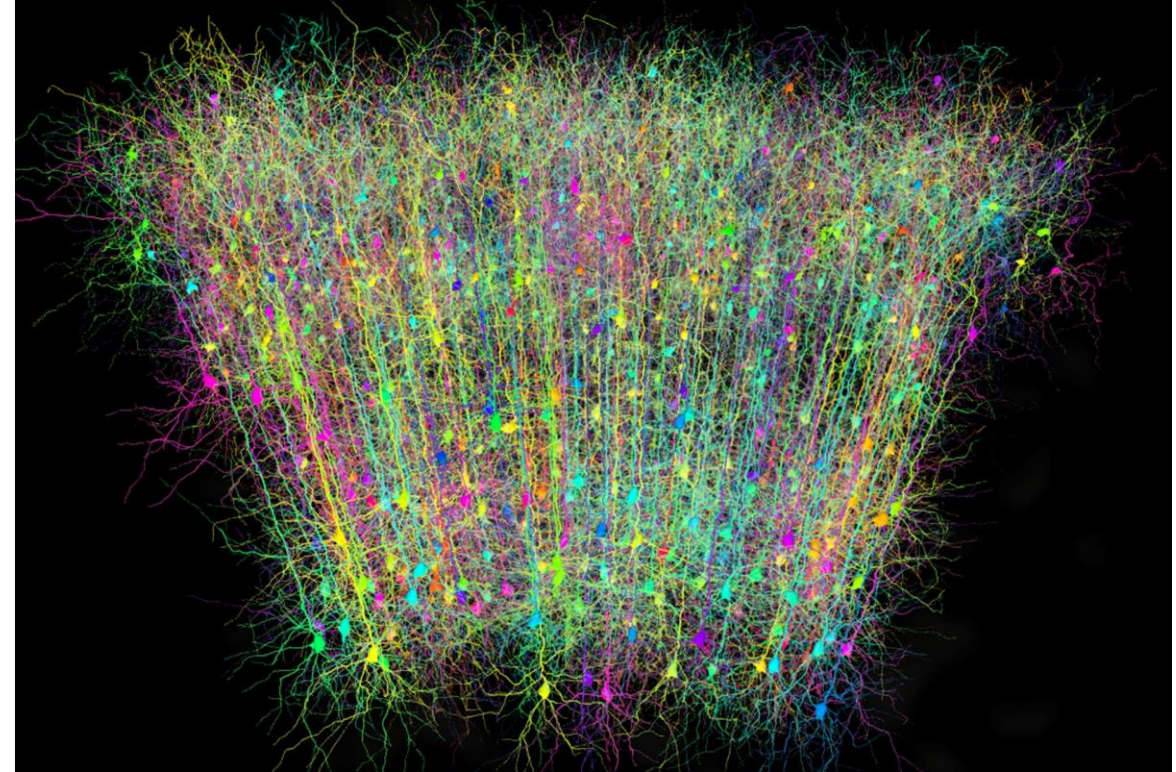
# Outline of Lecture

- Introduction to networks

- Spiking and firing rate network models

- Feedforward and recurrent networks

- Excitatory-inhibitory networks



The "brainbow" (an image of a real network)

# Outline of Lecture

- **Introduction to networks**

- Spiking and firing rate network models

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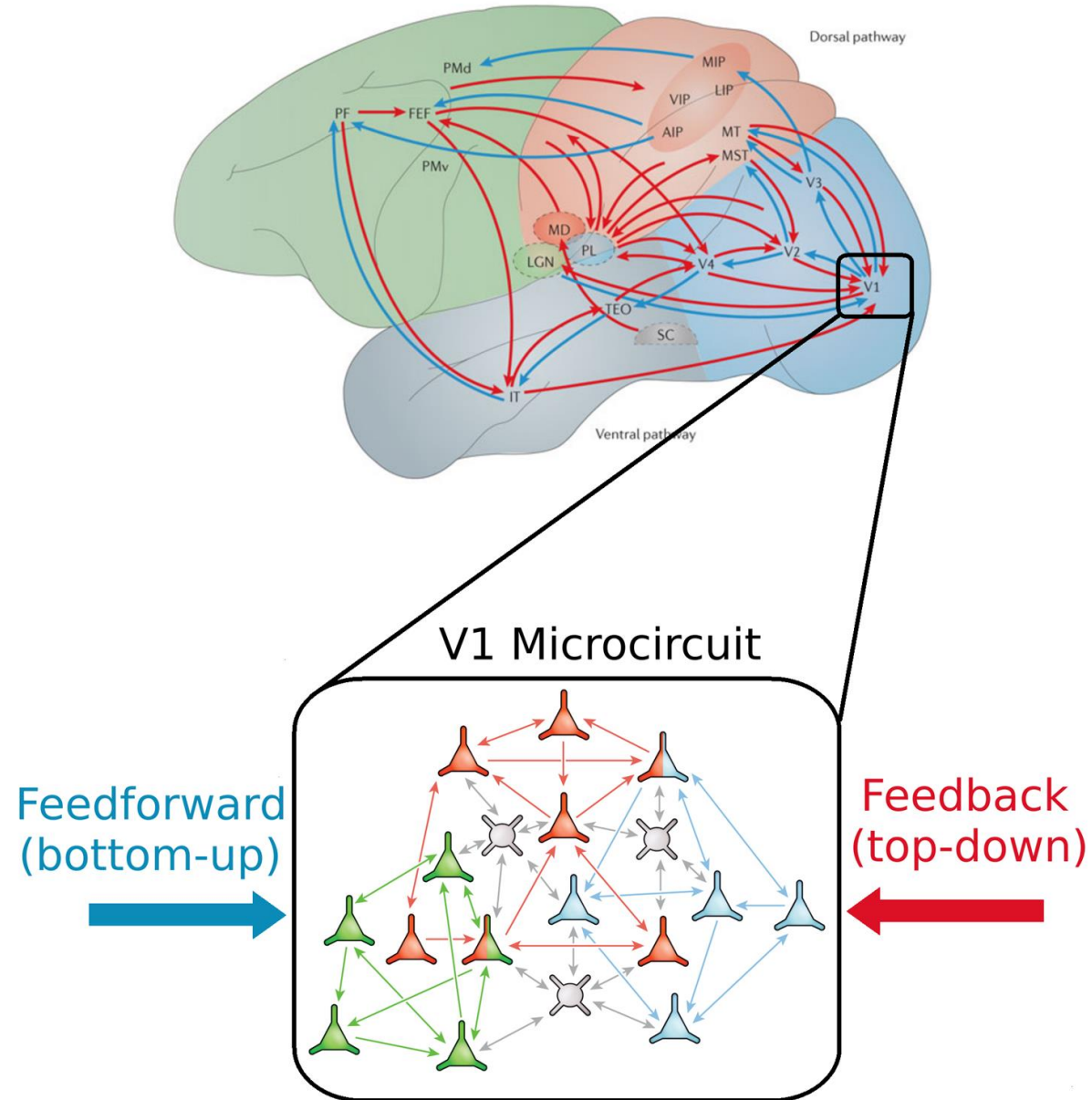
- Excitatory-inhibitory networks



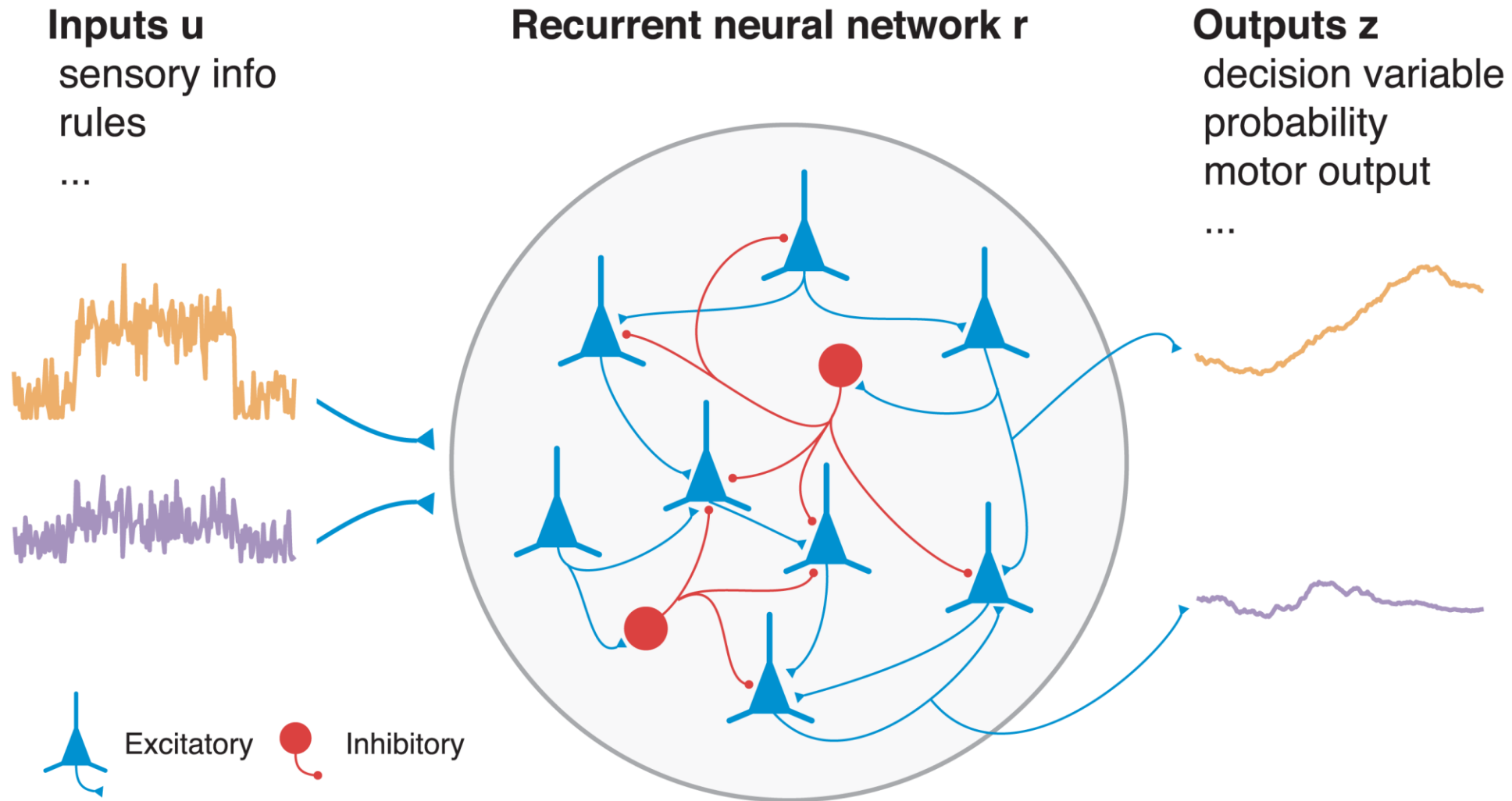The "brainbow" (an image of a real network)

# Networks of Neurons

- Neurons in the brain connect to form *networks*

- Networks of neurons *transform* external inputs into a pattern of spiking output

- This input-output transformation may be viewed as a *computation*

- These computations are thought to be the neural basis for *perception, decision making, memory, motor control*, etc.

- In this lecture we focus on models of *biological* networks of neurons (in contrast to artificial neural networks)

# Networks of the Brain



Dorsal pathway

Ventral pathway

PMd · PF · FEF · PMv · MIP · VIP · LIP · AIP · MT · MST · V3 · MD · LGN · PL · V4 · V2 · V1 · TEO · SC · IT

V1 Microcircuit

Feedforward
(bottom-up)

Feedback
(top-down)

# Networks Dynamics and Computation



**Inputs u**
sensory info
rules
...

**Recurrent neural network r**

**Outputs z**
decision variable
probability
motor output
...

Excitatory    Inhibitory

Song et al., 2016

- *What* are the properties of neural networks? (experimental/descriptive modelling question)

- *How* do networks generate their activity patterns and associated computations? (mechanistic question)

- *Why* are networks the way they are? What are problems do they solve and what constraints do they solve them under? ("teleological" question, ultimately appeals to evolution)

# Marr's 3 Levels of Analysis

We are mainly taking a "bottom-up" approach to understanding networks...

But remember Marr's three levels - we saw examples of "top-down" approaches with e.g. sparse coding, predictive coding, etc.



"...trying to understand perception by studying only neurons is like trying to understand bird flight by studying only feathers. It cannot be done" - David Marr (1982/2010, p. 27)

Algorithm = flapping

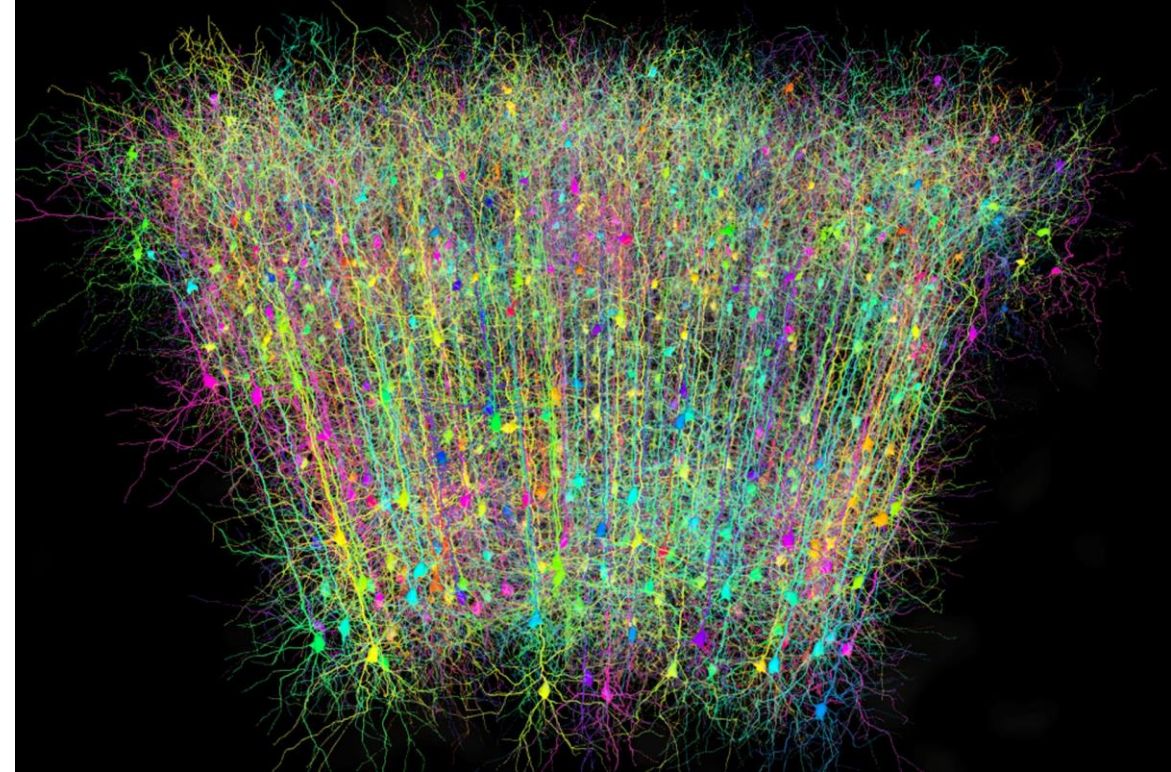Implementation = feathers

Computation = flight
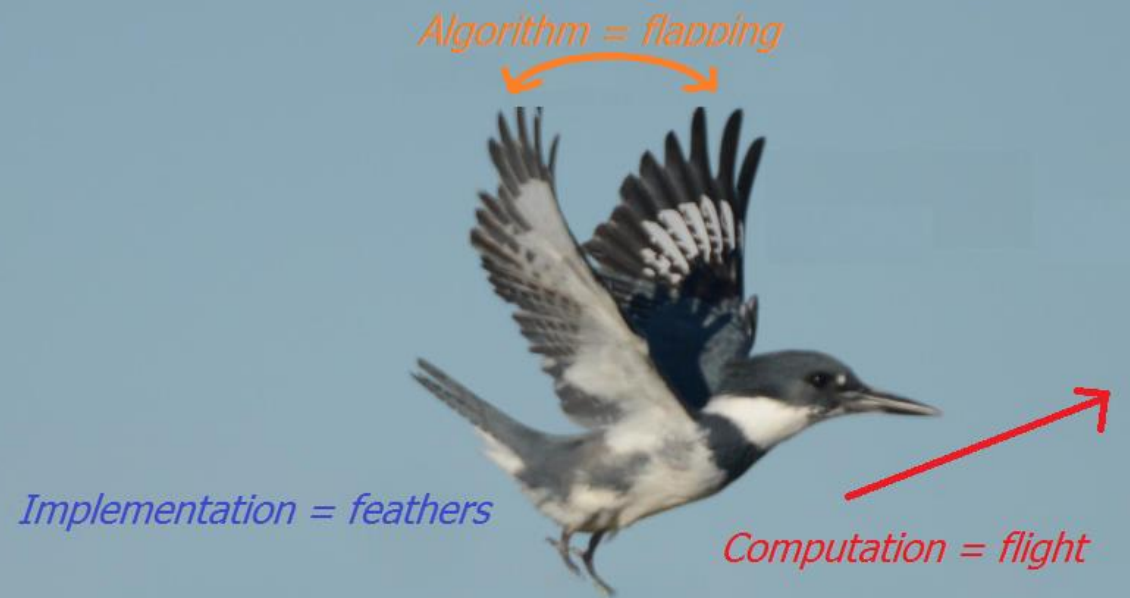
- How do the *connectivity* and *single-neuron properties* relate to the *global properties* (dynamics, input-output transformation, etc.)?

- How do networks *learn*? What are the learning rules? What are the initial conditions?

- What aspects of biological networks can be distilled into *artificial applications* (AI, neural hardware, etc.)? What aspects can we ignore?

- When do networks go wrong? How does this relate to *disease*?

# What Tools do we Use?

- **Experiment:** measurements of connectivity, neuronal activity, etc.

- **Mathematical analysis**: on simplified or reduced models (e.g., firing rate models, mean field theory)

- **Numerical simulation**: often of more biologically-plausible models

- **Machine learning**: e.g., by training an artificial neural network to solve a task and studying the learned network solution

- **Neural data analysis tools:** e.g., inference of network dynamics from recordings of neural activity

# Outline of Lecture

- Introduction to networks

- **Spiking and firing rate network models**

- Feedforward and recurrent networks

- Dynamics of recurrent networks

- Excitatory-inhibitory networks



The "brainbow" (an image of a real network)

- Consider a leaky integrate and fire neuron receiving inputs through a set of synapses:

Membrane potential dynamics:

$$\tau_m \frac{dV}{dt} = -(V - E_m) - I_{syn}(t)/g_m$$

Spike-reset rule:

$$\text{if } V(t) \geq V_{\text{threshold}}, \quad \text{set } V(t) = V_{\text{reset}}$$

Synaptic input current:

$$I_{syn}(t) = \sum_{j=1}^{N_{\text{synapse}}} g_{syn,j}(t)(V(t) - E_{syn,j})$$

# Spiking Network Models: An Example

- Consider a leaky integrate and fire neuron receiving inputs through a set of synapses:

Membrane potential dynamics:

$$\tau_m \frac{dV}{dt} = -(V - E_m) - I_{syn}(t)/g_m$$

Spike-reset rule:

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Synaptic input current:

$$I_{syn}(t) = \sum_{j=1}^{N_{\text{synapse}}} g_{syn,j}(t)(V(t) - E_{syn,j})$$

- Now consider multiple such neurons coupled together via these synapses:

Membrane potential of neuron i:

$$\tau_{m,i} \frac{dV_i}{dt} = -(V_i - E_{m,i}) - \sum_{j \neq i} g_{syn,ij}(t)(V_i - E_{syn,ij})/g_{m,i}$$

# Spiking Network Models

- A spiking network consists of:

1) A neuron model (e.g., Hodgkin-Huxley, leaky integrate and fire, etc.)

2) A synapse model (e.g., delta synapse, exponential synapse, etc.)

3) A set of parameters for the synaptic and membrane conductances, etc.

- Mathematically, a spiking network model is a set of coupled differential equations

- For example, a network of Hodgkin-Huxley neurons has 4N neuron equations, and *O(N^2)* synapse equations (depending on synapse model, could be more...)

- We typically make simplifications to reduce the number/complexity of equations
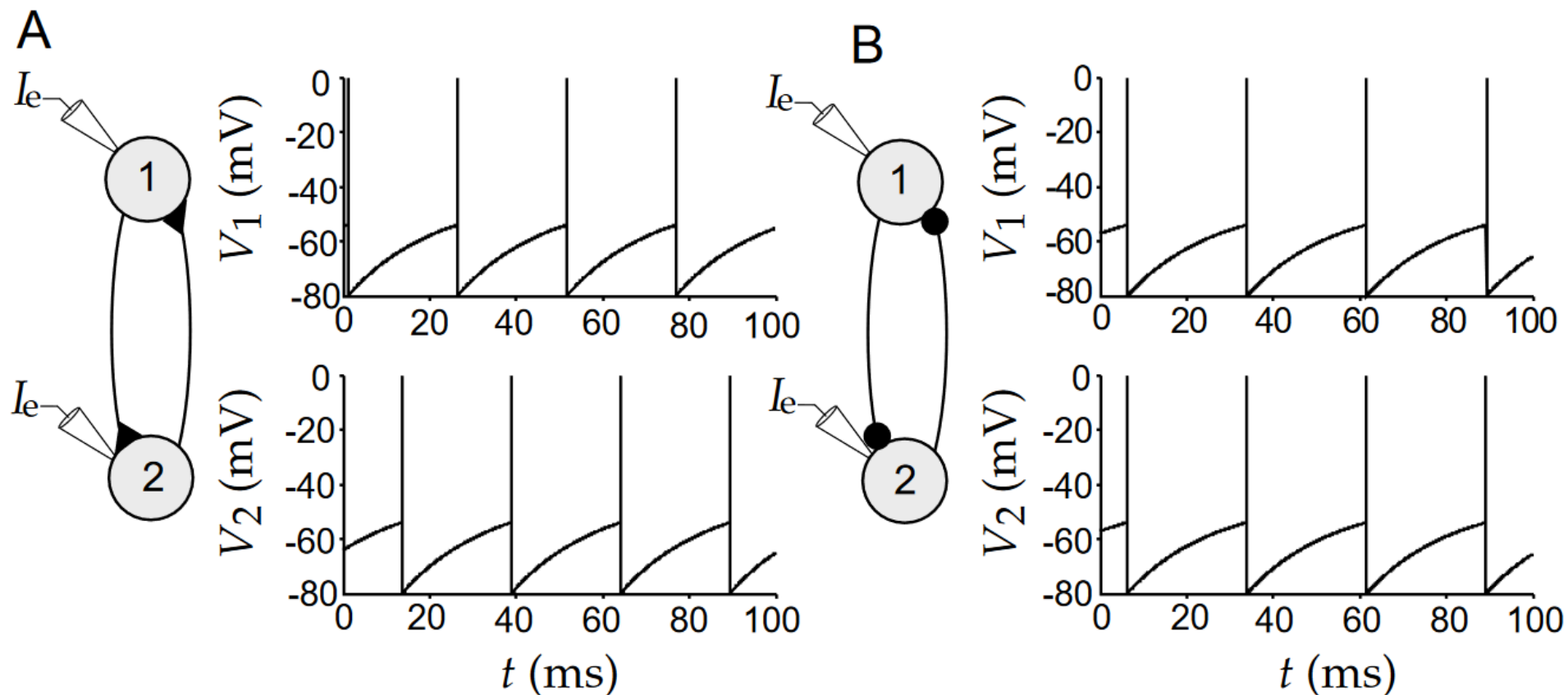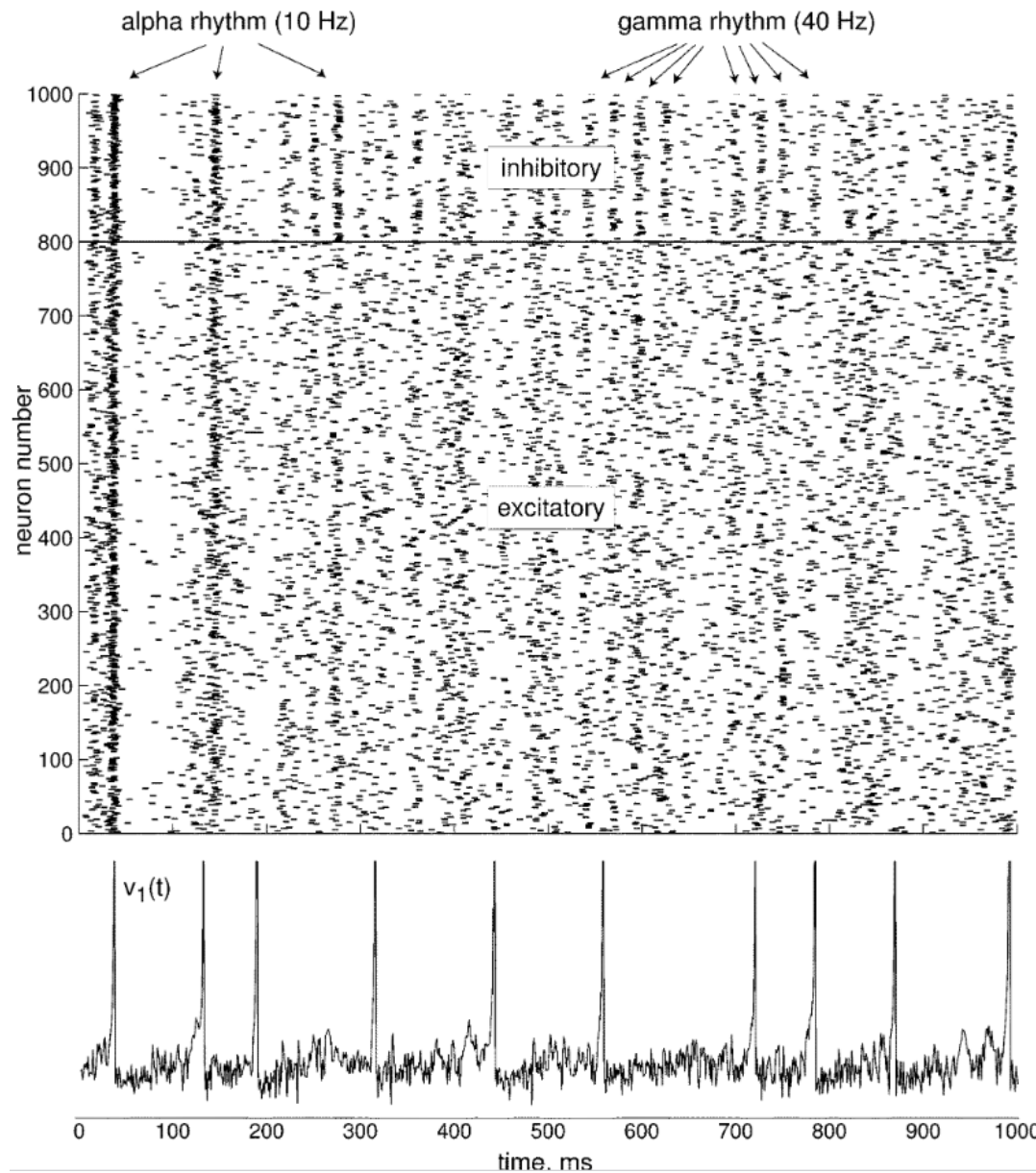
# A Simple Spiking Network



Figure 5.20 Two synaptically coupled integrate-and-fire neurons. (A) Excitatory synapses ($E_s = 0$ mV) produce an alternating, out-of-phase pattern of firing. (B) Inhibitory synapses ($E_s = -80$ mV) produce synchronous firing. Both model neurons have $E_L = -70$ mV, $V_{th} = -54$ mV, $V_{reset} = -80$ mV, $\tau_m = 20$ ms, $r_m \bar{g}_s = 0.05$, $P_{max} = 1$, $R_m I_e = 25$ mV, and $\tau_s = 10$ ms.

# A More Complex Spiking Network



[Izhikevitch, 2003]

- The leaky integrate and fire model with conductance-based synapses is:

$$\tau_{m,i}\frac{dV_i}{dt} = -(V_i - E_{m,i}) - \sum_{j\neq i} g_{syn,ij}(t)(V_i - E_{syn,ij})/g_{m,i}$$

# Spiking Network Models – Current-Based Synapses

- The leaky integrate and fire model with <span style="color:red">conductance-based synapses</span> is:

$$\tau_{m,i}\frac{dV_i}{dt} = -(V_i - E_{m,i}) - \sum_{j\neq i} g_{syn,ij}(t)(V_i - E_{syn,ij})/g_{m,i}$$

- We often simplify these synaptic currents by <span style="color:red">neglecting their voltage-dependence</span>:

$$\tau_{m,i}\frac{dV_i}{dt} = -(V_i - E_{m,i}) + \sum_{j\neq i} w_{ij}g_{syn,ij}(t) \qquad w_{ij} = -(\langle V_i \rangle - E_{syn,ij})/g_{m,i}$$

# Spiking Network Models – Current-Based Synapses

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- This approximation assumes that (*V-Esyn*) is roughly constant (*Esyn* is synaptic reversal potential: -80 mV for inhibitory and 0 mV for excitatory)

- These <span style="color:red">current-based</span> synapse models are easier to work with analytically, and form the basis of further simplified firing-rate network models

# Dales Law

- Synapses are either excitatory or inhibitory (E or I)

- For any neuron, all of its outgoing synapses are the same type (E or I)

- This suggests an important simplification - we can write the synaptic conductance as:

conductance of
synapse from *j* to *i*

fixed weight of *j* to *i*
(number of ion channels etc.)

timecourse of all outgoing
synapses from neuron *j*

$$g_{syn,ij}(t) = \bar{g}_{syn,ij} \, g_{syn,j}(t)$$

- This reduces the number of synaptic conductance equations from N^2 to N

- This makes quite strong assumptions – in reality, half of synapses may fail on any given spike, synapses may release different amounts of neurotransmitter, etc.

# Firing Rate Network Models

Firing rate models abstract the spiking of a neuron into a firing rate (spikes/second)

We can replace our spiking network models with firing rate models using two key approximations:

1) We replace spikes with the time- or neuron-averaged firing rates

2) We model the inputs as an average current

*Spiking Network [current based synapses]*

$$\tau_{m,i}\frac{dV_i}{dt} = -(V_i - E_{m,i}) + \sum_j w_{ij} g_{syn,ij}(t) + I_{ext,i}(t)/g_{m,i}$$

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firing rate

transfer function

*Rate Approximation*

$$g_{syn,ij}(t) \rightarrow \langle g_{syn,ij}(t) \rangle \approx \bar{g}_{syn,ij}r_j(t) \approx \bar{g}_{syn,ij}\phi(V_j)$$

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firing rate          transfer function

*Rate Approximation*     $g_{syn,ij}(t) \rightarrow \langle g_{syn,ij}(t) \rangle \approx \bar{g}_{syn,ij}r_j(t) \approx \bar{g}_{syn,ij}\phi(V_j)$

*Firing Rate Network*     $\tau_{m,i}\frac{dV_i}{dt} = -(V_i - E_{m,i}) + \sum_j \bar{w}_{ij}\phi(V_j) + I_{ext,i}(t)/g_{m,i}$

# Firing Rate Network Models

What do we mean by firing rate? What are we averaging over?

Two interpretations: average over neurons or time (or both). Usually we don't specify which.

**Time-Average**
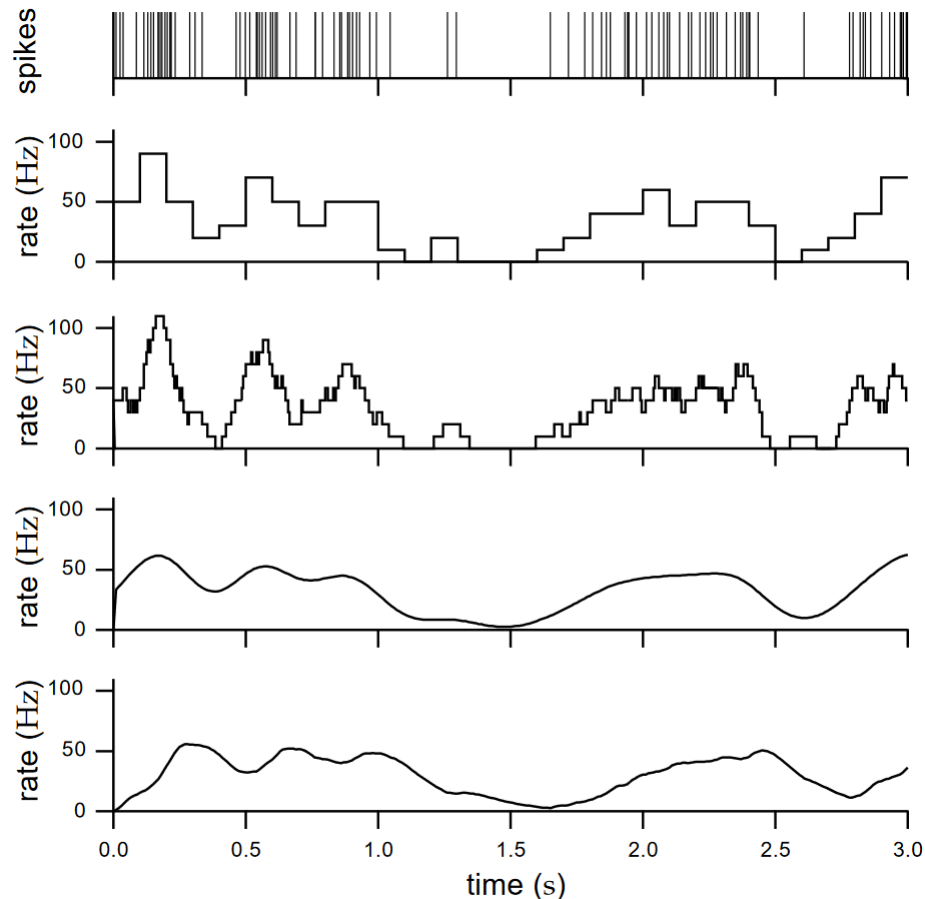
**Neuron-Average**

rate = average over pool of equivalent neurons
(several neurons, single run)
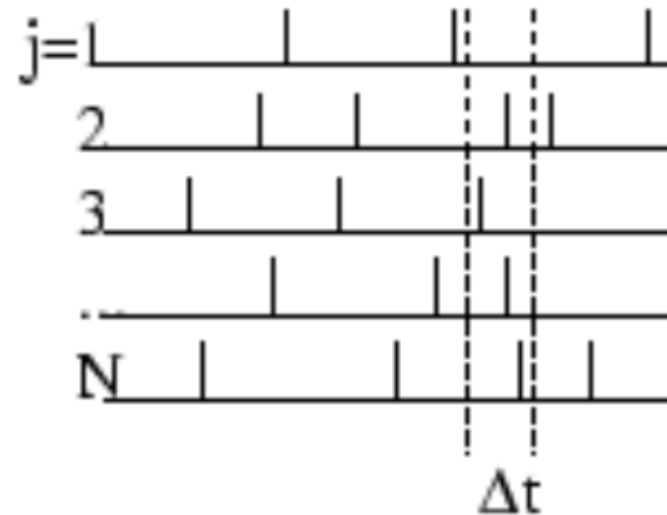
$$A = \frac{1}{\Delta t} \frac{n_{act}(t;t+\Delta t)}{N}$$

activity

# Firing Rate Network Models

- Advantages of firing rate network models:

- Numerically efficient

- Analytically tractable

- Can train to optimise cost functions (e.g., train RNNs via backprop)

- Simpler to visualise/understand


- Disadvantages:

- Lose information about spike timing

- Assumptions required for averaging may be unrealistic

- Sometimes a firing rate network behaves very differently when converted to a spiking network (e.g., may become unstable, or require fine-tuning of parameters)

# Firing Rate Models: Assumptions

- When is it reasonable to approximate a neuron's spike pattern in terms of its rate?

- We are ignoring spike patterns, e.g. synchrony, sequences, refractory periods, etc.

- Firing rate models make sense for neurons that fire asynchronously and irregularly (e.g., Poisson firing)

- This is often a reasonable approximation for neurons in cortex, but some brain regions or brain states have reliable temporal spike patterns that are ignored by firing rate models

# Two Firing Rate Network Models

- There are two common variants of firing rate network models in the field

- We discussed the following model earlier:

$$\tau_{m,i} \frac{dV_i}{dt} = -(V_i - E_{m,i}) + \sum_j \bar{w}_{ij} \phi(V_j) + I_{ext,i}(t)/g_{m,i}$$

$V_i$ = membrane potential

$\phi$ = "transfer function"
(the f-I curve)

- This would usually be rewritten in a simpler form:

$$\tau_m \frac{dV_i}{dt} = -(V_i - E_m) + \sum_j w_{ij} \phi(V_j) + u_i(t)$$

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$$\tau_m\frac{dV_i}{dt} = -(V_i - E_m) + \sum_j w_{ij}\phi(V_j) + u_i(t)$$

- A very common alternative equation for a firing rate network is:

$$\tau_m\frac{dr_i}{dt} = -r_i + \phi\left(\sum_j w_{ij}r_j + u_i(t)\right)$$

$r_i$ = "firing rate"
(spikes per second)

- Many choices of transfer function are available: rectified-linear, rectified-power law, sigmoid, rectified-tanh etc.

- Often a threshold-linear function is used, and sometimes even a purely linear function.

- Neurons can't have negative firing rates, and their firing rates saturate for very strong input currents, so threshold-sigmoid transfer functions may be more realistic.
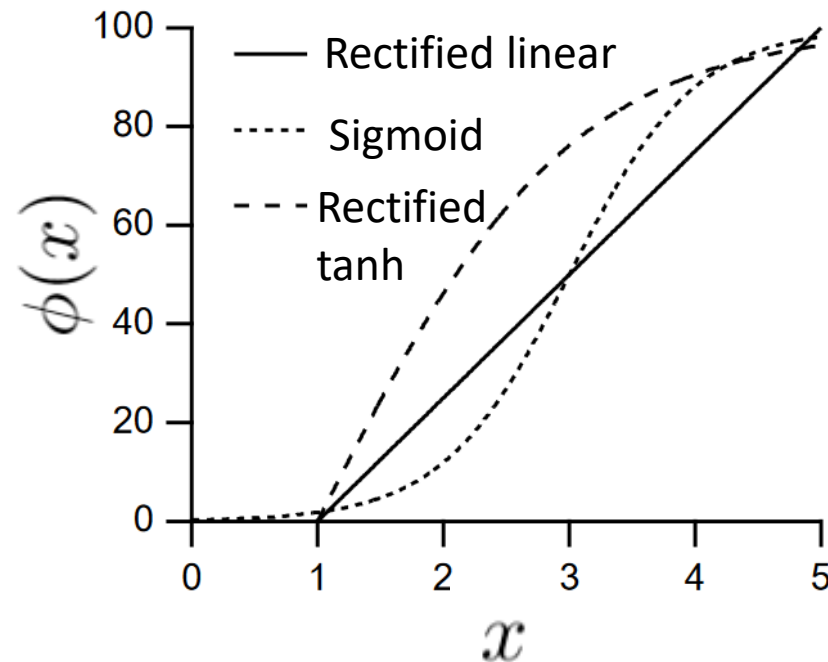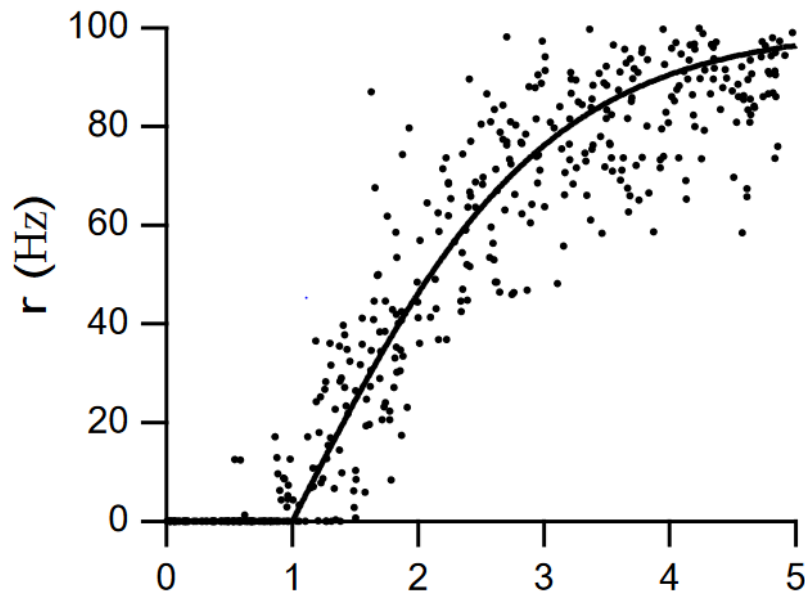
# Summary: Network Models

- Spiking network models couple together neurons via synapses to capture spiking patterns of the network

- Firing rate models abstract spike patterns into a single firing rate for each neuron

- Firing rate models can be justified using various approximations, and are much simpler and easier to work with, but less realistic

- Usually, our goal is to create the simplest model that captures some phenomenon, not the most detailed model. Unless we are interested in spike timing, firing rate models are the default option

# Outline of Lecture

- Introduction to networks

- Spiking and firing rate network models

- **Feedforward and recurrent networks**

- Excitatory-inhibitory networks



The "brainbow" (an image of a real network)

# Computations in Feedforward Networks

- Feedforward networks are those with no loops

- Feedforward networks are simple to analyse and can capture important properties of sensory systems (as we saw with convolutional neural networks)

- But they omit the recurrent and top-down (feedback) connections found in the brain, and are therefore unrealistic biologically
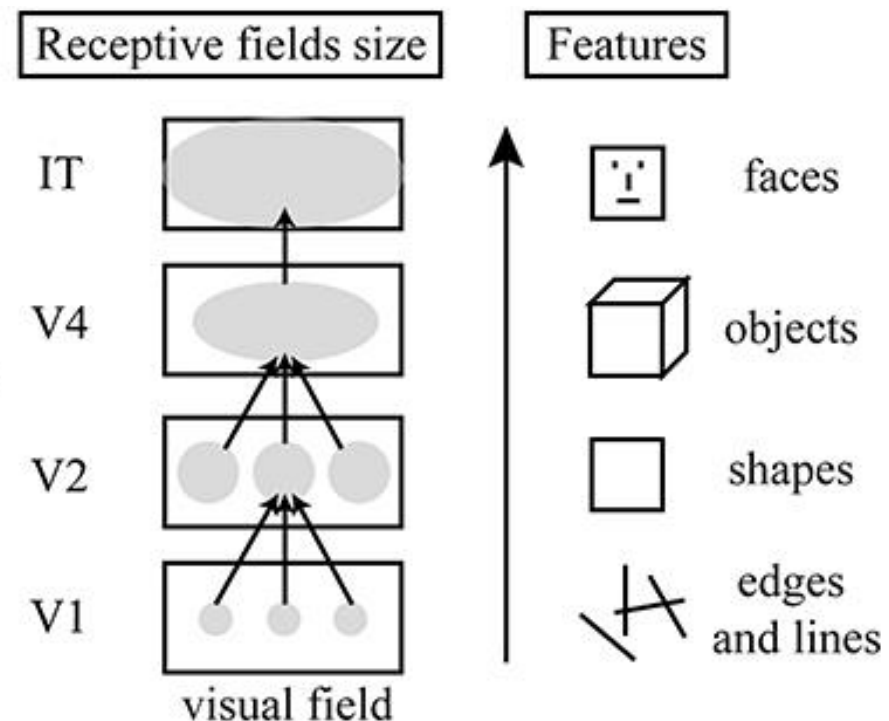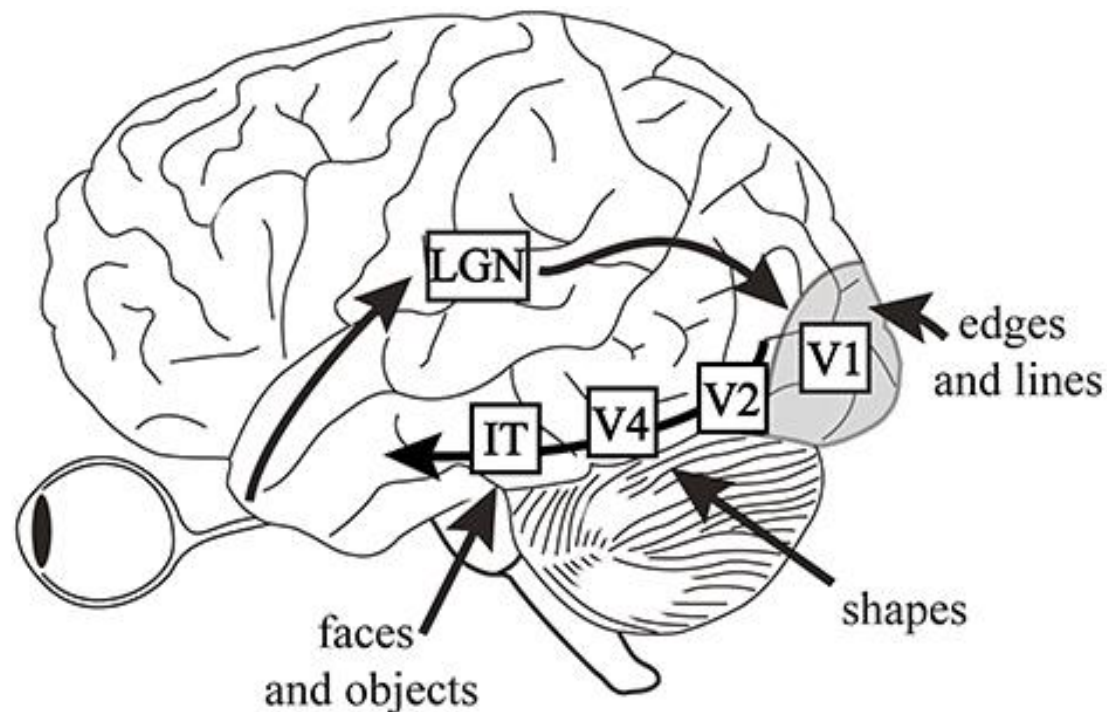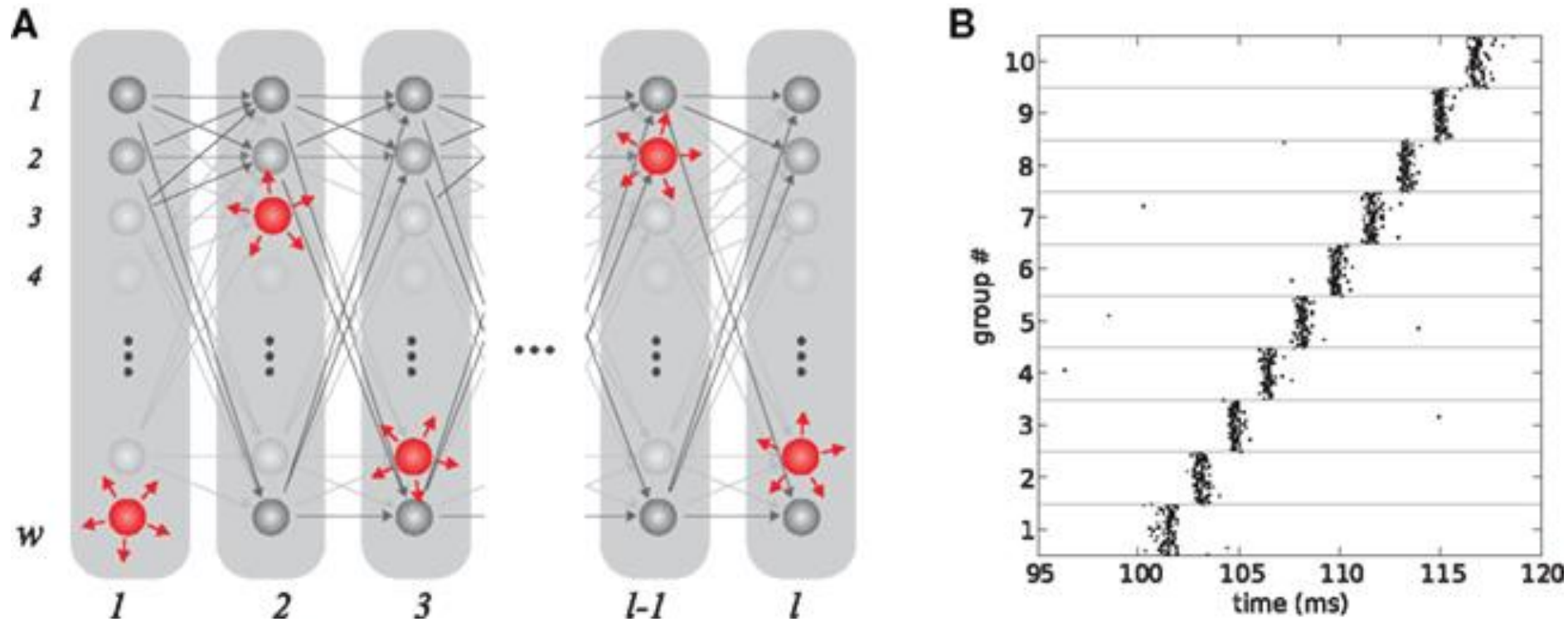
- A synfire chain is a feedforward spiking network comprising multiple layers

- Spiking propagates in volleys from one layer to the next

- We can ask questions such as: will spiking propagate indefinitely or eventually die out? How does this depend on connectivity?

- This can offer a useful model of sensory processing (first ~100 ms after stimulus onset).

# Feedforward vs Recurrent Processing



**Box 2. The feedforward sweep**

≤40 ms    ≤50 ms    <65 ms    <80 ms    <115 ms
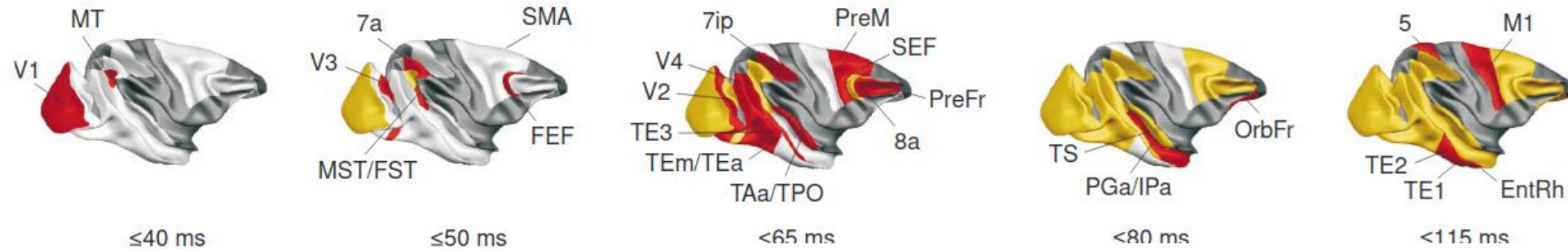
Initial feedforward sweep is like a synfire chain. We can already recognise and categorise objects with this.

Later, recurrent and top-down process take place, which are necessary for higher level "conscious" perception

REVIEW

## The distinct modes of vision offered by feedforward and recurrent processing

Victor A.F. Lamme and Pieter R. Roelfsema

An analysis of response latencies shows that when an image is presented to the visual system, neuronal activity is rapidly routed to a large number of visual areas. However, the activity of cortical neurons is not determined by this feedforward sweep alone. Horizontal connections within areas, and higher areas providing feedback, result in dynamic changes in tuning. The differences between feedforward and recurrent processing could prove pivotal in understanding the distinctions between attentive and pre-attentive vision as well as between conscious and unconscious vision. The feedforward sweep rapidly groups feature constellations that are hardwired in the visual brain, yet is probably incapable of yielding visual awareness; in many cases, recurrent processing is necessary before the features of an object are attentively grouped and the stimulus can enter consciousness.

*Trends Neurosci.* (2000) 23, 571–579

# Recurrent Networks: Fixed Points, Oscillations and Chaos

- Recurrently connected networks of neurons admit many kinds of emergent collective behaviour depending on their connectivity and transfer functions

- We can use dynamical systems theory to study these different kinds of behaviour

- Can exhibit fixed points (attractors), oscillations (limit cycles) or chaotic dynamics

- These dynamics confer different computational capabilities to the network

- Attractors may be useful for memory, oscillations may be useful for neuronal communication, chaos may be useful for high-capacity input discrimination

# Network Dynamics: Fixed Points, Oscillations and Chaos

One Fixed Point (Point Attractor)
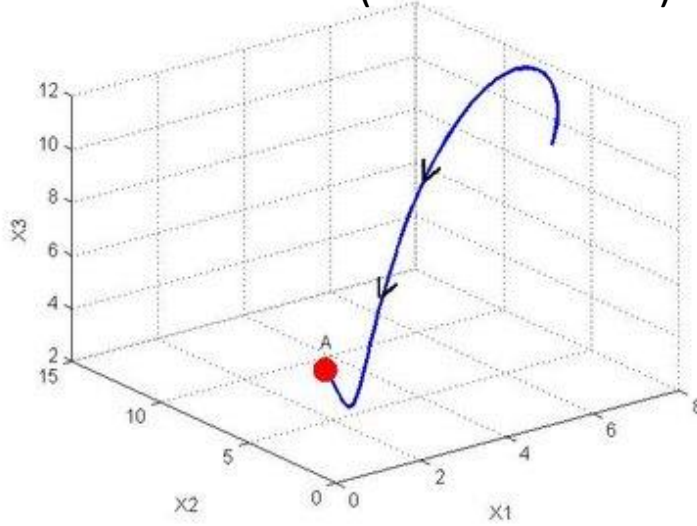
Multiple Discrete Fixed Points
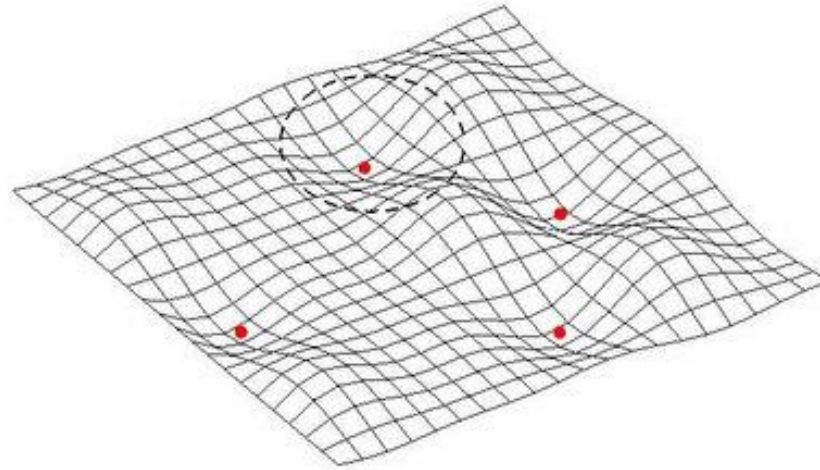
A Continuum of Fixed Points (Line Attractor)
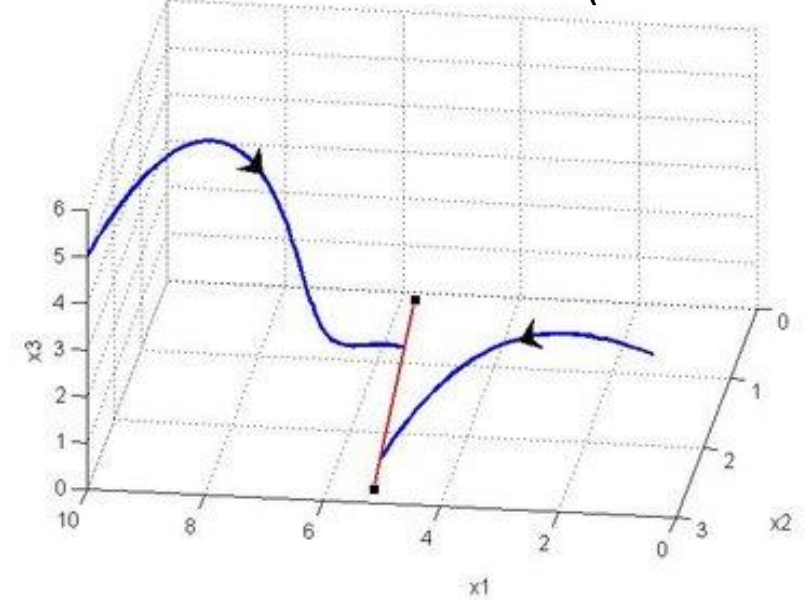
Stable Oscillation (Limit Cycle)
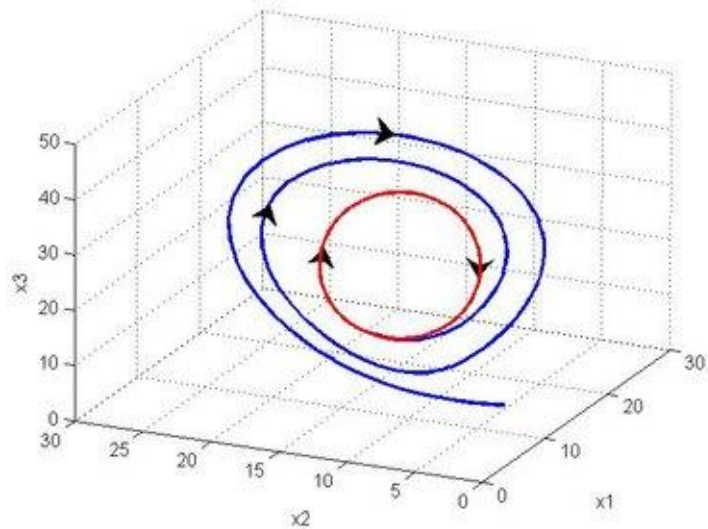
Chaos (Lorenz Attractor)
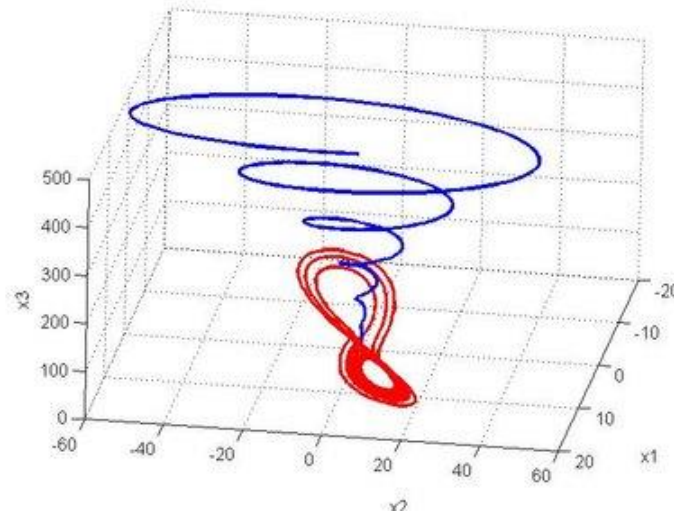
# Chaos in Randomly Connected Spiking Networks

## Chaos in Random Neural Networks

H. Sompolinsky[a] and A. Crisanti

*AT&T Bell Laboratories, Murray Hill, New Jersey 07974, and*
*Racah Institute of Physics, The Hebrew University, 91904 Jerusalem, Israel[b]*

and

H. J. Sommers[a]

*Fachbereich Physik, Universität-Gesamthochschule Essen, D-4300 Essen, Federal Republic of Germany*

A continuous-time dynamic model of a network of $N$ nonlinear elements interacting via random asymmetric couplings is studied. A self-consistent mean-field theory, exact in the $N \to \infty$ limit, predicts a transition from a stationary phase to a chaotic phase occurring at a critical value of the gain parameter. The autocorrelations of the chaotic flow as well as the maximal Lyapunov exponent are calculated.

## Beyond the edge of chaos: Amplification and temporal integration by recurrent networks in the chaotic regime

T. Toyoizumi[1,2,*] and L. F. Abbott[1]
[1]*Department of Neuroscience and Department of Physiology and Cellular Biophysics, Columbia University, New York, New York 10032, USA*
[2]*RIKEN Brain Science Institute, Wako-shi, Saitama 351-0198, Japan*

Randomly connected networks of neurons exhibit a transition from fixed-point to chaotic activity as the variance of their synaptic connection strengths is increased. In this study, we analytically evaluate how well a small external input can be reconstructed from a sparse linear readout of network activity. At the transition point, known as the edge of chaos, networks display a number of desirable features, including large gains and integration times. Away from this edge, in the nonchaotic regime that has been the focus of most models and studies, gains and integration times fall off dramatically, which implies that parameters must be fine tuned with considerable precision if high performance is required. Here we show that, near the edge, decoding performance is characterized by a critical exponent that takes a different value on the two sides. As a result, when the network units have an odd saturating nonlinear response function, the falloff in gains and integration times is much slower on the chaotic side of the transition. This means that, under appropriate conditions, good performance can be achieved with less fine tuning beyond the edge, within the chaotic regime.

## Real-Time Computation at the Edge of Chaos in Recurrent Neural Networks

Nils Bertschinger
*nilsb@igi.tugraz.at*
*Institute for Theoretical Computer Science, Technische Universitaet Graz, A-8010 Graz, Austria*

Thomas Natschläger
*Thomas.Natschlaeger@scch.at*
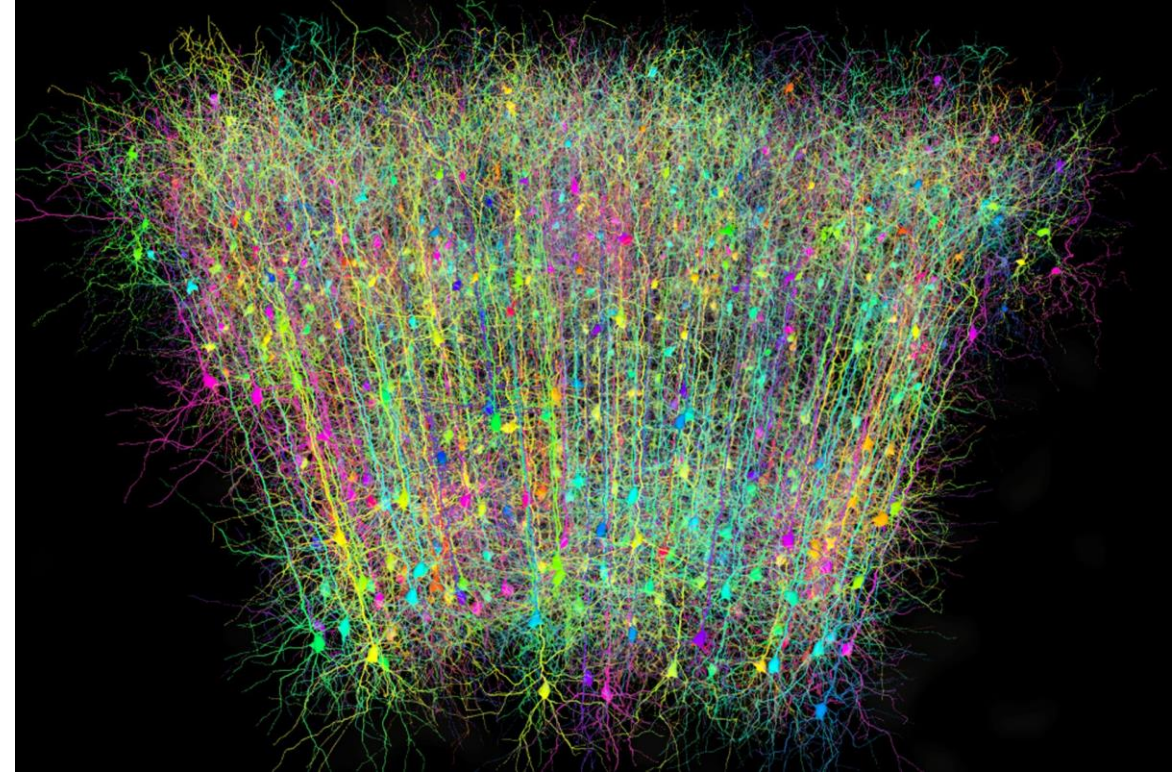*Software Compentence Center Hagenberg, A-4232 Hagenberg, Austria*

Depending on the connectivity, recurrent networks of simple computational units can show very different types of dynamics, ranging from totally ordered to chaotic. We analyze how the type of dynamics (ordered or chaotic) exhibited by randomly connected networks of threshold gates driven by a time-varying input signal depends on the parameters describing the distribution of the connectivity matrix. In particular, we calculate the critical boundary in parameter space where the transition from ordered to chaotic dynamics takes place. Employing a recently developed framework for analyzing real-time computations, we show that only near the critical boundary can such networks perform complex computations on time series. Hence, this result strongly supports conjectures that dynamical systems that are capable of doing complex computational tasks should operate near the edge of chaos, that is, the transition from ordered to chaotic dynamics.

# Summary: Feedforward and Recurrent Networks

- Two models of feedforward networks: deep neural networks and synfire chains

- Offer a good model for the multi-layer propagation of sensory activity following stimulus onset

- Recurrent networks are far richer due to their dynamics

- Dynamics can be used for computation, e.g. fixed points for memory, line attractors for evidence integration, etc.

- We will see examples of such networks later in the course

  (ring network, Hopfield network, etc.)

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- Feedforward and recurrent networks

- **Excitatory-inhibitory networks**



The "brainbow" (an image of a real network)

# E-I Firing Rate Networks

- Some models consider a single population of cells whose outgoing synaptic weights may be positive or negative (violating Dale's principle)

- Other models include separate E and I populations:

$$\tau_E \frac{dr_i^E}{dt} = -r_i^E + \phi(\sum_j W_{ij}^{EE} r_j^E - \sum_j W_{ij}^{EI} r_j^I + u_i^E)$$

$$\tau_I \frac{dr_i^I}{dt} = -r_i^I + \phi(\sum_j W_{ij}^{IE} r_j^E - \sum_j W_{ij}^{II} r_j^I + u_i^I)$$

- For firing rate models, it is often assumed that we are averaging over both E and I neurons, so don't need to treat E and I separately

- For spiking models, E and I neurons are usually treated separately

## Chaos in Neuronal Networks with Balanced Excitatory and Inhibitory Activity

C. van Vreeswijk and H. Sompolinsky

Neurons in the cortex of behaving animals show temporally irregular spiking patterns. The origin of this irregularity and its implications for neural processing are unknown. The hypothesis that the temporal variability in the firing of a neuron results from an approximate balance between its excitatory and inhibitory inputs was investigated theoretically. Such a balance emerges naturally in large networks of excitatory and inhibitory neuronal populations that are sparsely connected by relatively strong synapses. The resulting state is characterized by strongly chaotic dynamics, even when the external inputs to the network are constant in time. Such a network exhibits a linear response, despite the highly nonlinear dynamics of single neurons, and reacts to changing external stimuli on time scales much smaller than the integration time constant of a single neuron.
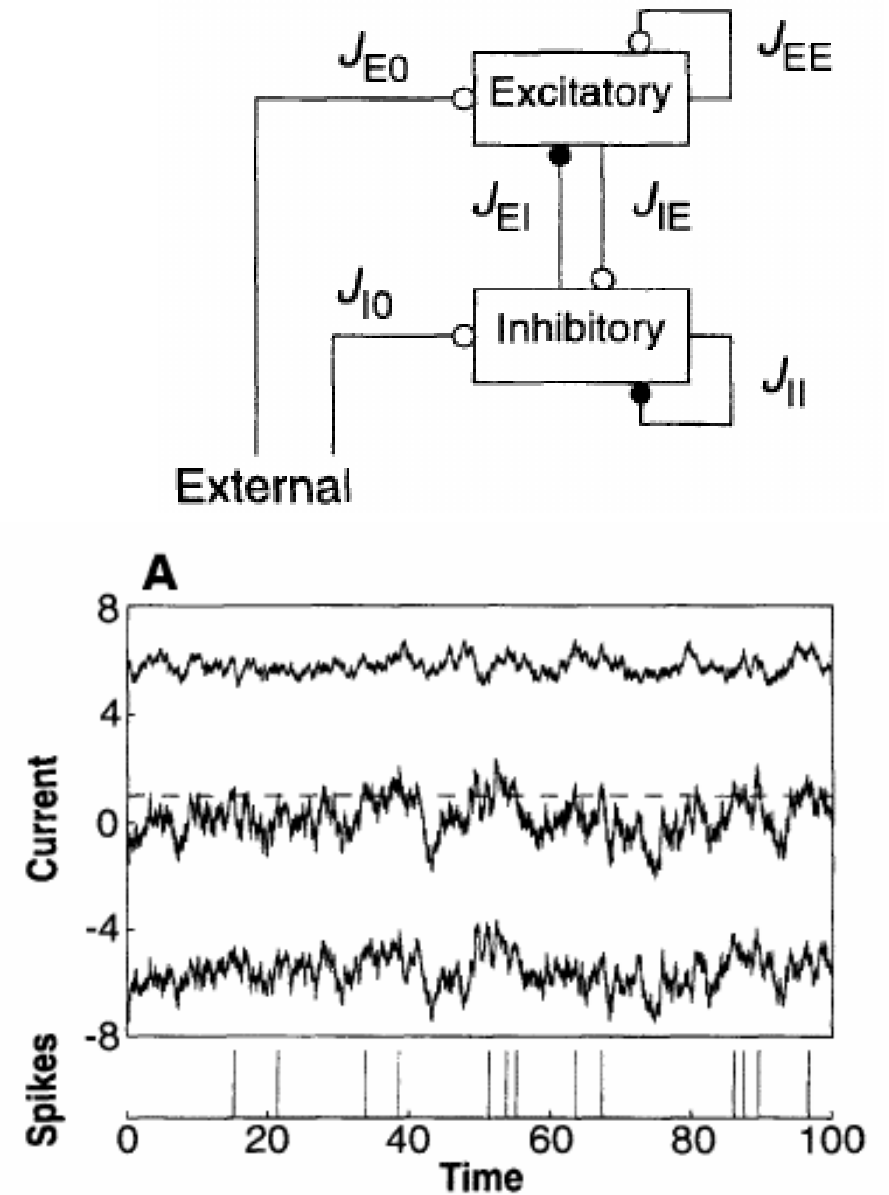
# Balanced Excitatory-Inhibitory Network Models

- The theory of balanced network dynamics <span style="color:red">explains the irregular asynchronous regime</span> of cortex

- Network generates this regime even when inputs are constant!

- Network has sparse but strong synapses. Take limit of many neurons and solve analytically (uses tools from statistical physics)

- Behaviour of network:

- excitatory and inhibitory inputs to each neuron are <span style="color:red">strong</span> and <span style="color:red">balanced</span>, and almost cancel one another

- Fluctuations in external input are rapidly cancelled by recurrent inhibition

- Spiking is generated by <span style="color:red">fluctuations</span> in E-I balance

# Evidence for E-I Balance

- E-I balance has been confirmed in multiple experiments. A successful theoretical prediction! Below shows how E and I inputs to a neuron track each other in time.
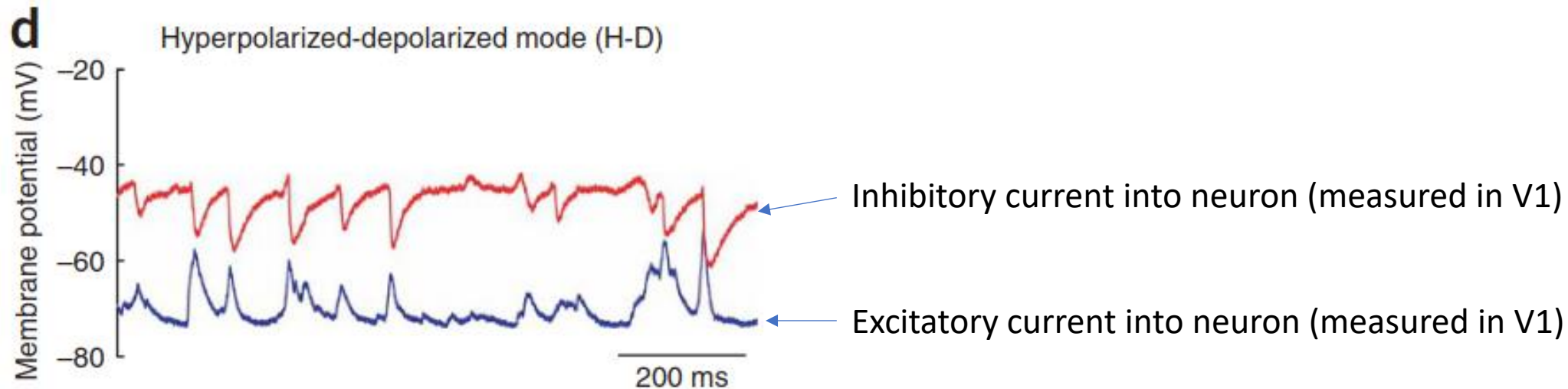


Inhibitory current into neuron (measured in V1)

Excitatory current into neuron (measured in V1)

Bilal Haider, Alvaro Duque, Andrea R. Hasenstaub, and David A. McCormick
Department of Neurobiology, Kavli Institute for Neuroscience, Yale University School of Medicine, New Haven, Connecticut 06510

Instantaneous correlation of excitation and inhibition during ongoing and sensory-evoked activities

Michael Okun & Ilan Lampl

# Other Dynamical Regimes

• Other dynamical regimes are possible, and have been studied theoretically
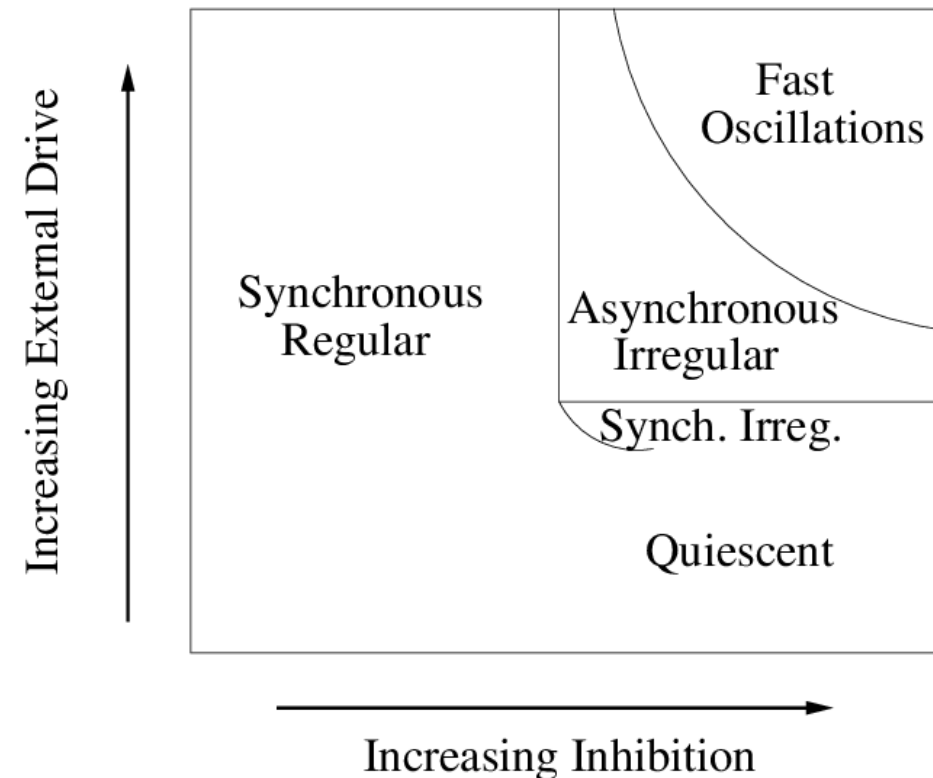
# Asynchronous Activity and E-I Balance

- Two states in cortex:

1) balanced regime, characterised by irregular, asynchronous, Poisson spiking

2) synchronous regime, characterised by global, synchronous fluctuations in network activity

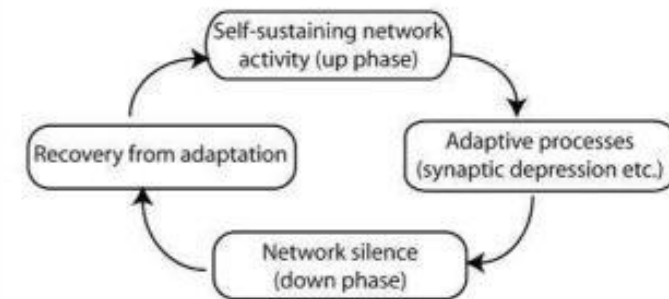Cortical state is modulated by attention, alertness, etc.



Harris et al., 2011

# Inhibitory Stabilization and Paradoxical Inhibition

## Paradoxical Effects of External Modulation of Inhibitory Interneurons

Misha V. Tsodyks,[1,2,3] William E. Skaggs,[2] Terrence J. Sejnowski,[3,4] and Bruce L. McNaughton[2]

[1]Department of Neurobiology, Weizmann Institute, Rehovot 76100, Israel, [2]Arizona Research Laboratories, Division of Neural Systems, Memory and Aging, University of Arizona, Tucson, Arizona 85724, [3]Howard Hughes Medical Institute, Computational Neurobiology Laboratory, The Salk Institute for Biological Studies, La Jolla, California 92037, and [4]Department of Biology, University of California at San Diego, La Jolla, California 92093

- Networks in the brain are often "inhibitory-stabilised" (recurrent excitation causes unstable positive feedback, but inhibition stabilises this)

- Inhibitory-stabilised networks exhibit a counter-intuitive behaviour called "paradoxical inhibition"

**Paradoxical Effects of External Modulation of Inhibitory Interneurons**

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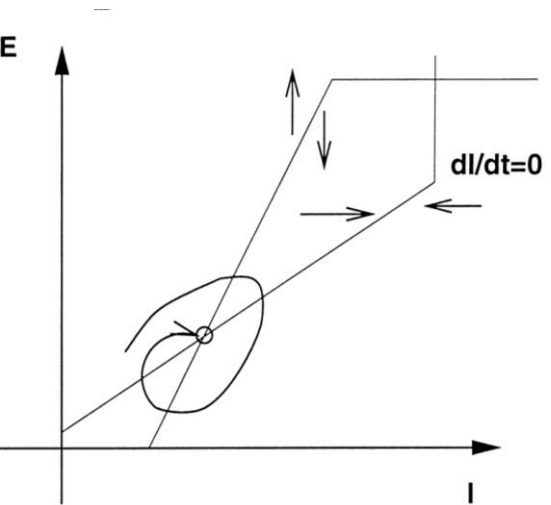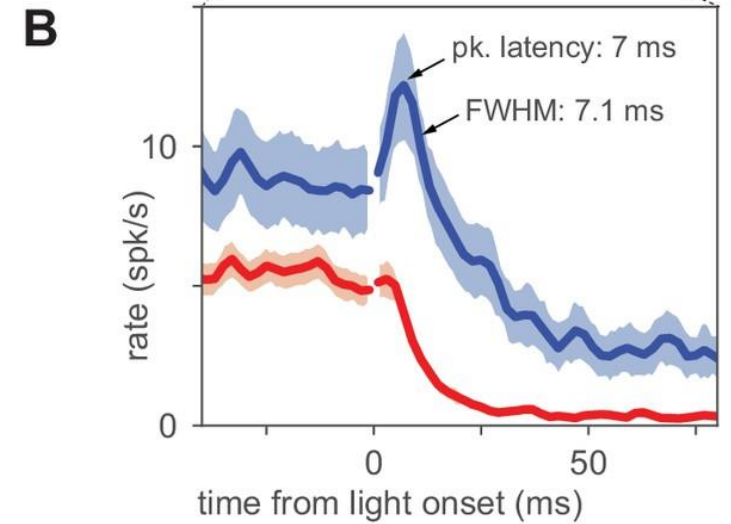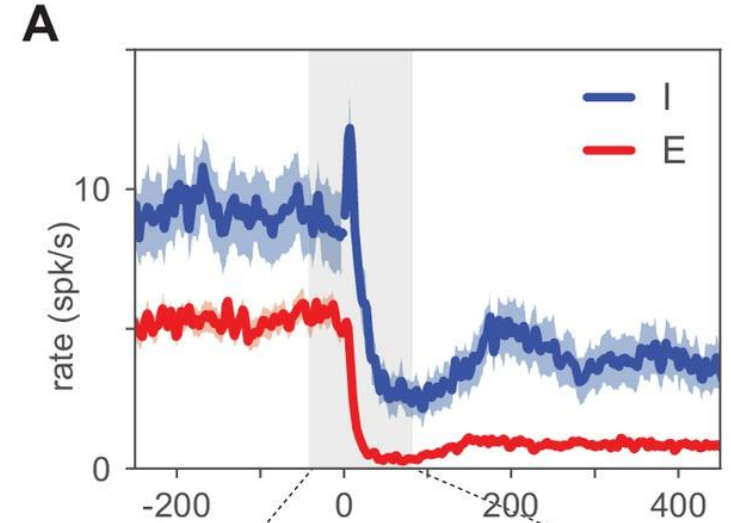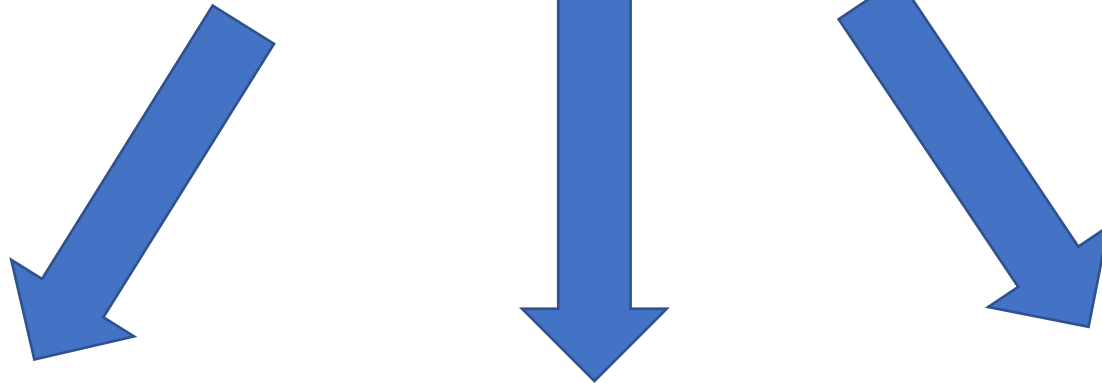


- Networks in the brain are often "inhibitory-stabilised" (recurrent excitation causes unstable positive feedback, but inhibition stabilises this)

- Inhibitory-stabilised networks exhibit a counter-intuitive behaviour called "paradoxical inhibition"

- Positive external current input to inhibitory neurons causes their firing rate to decrease
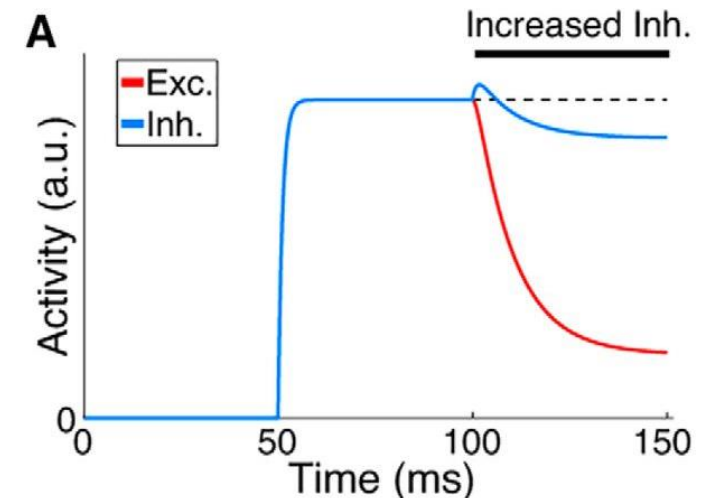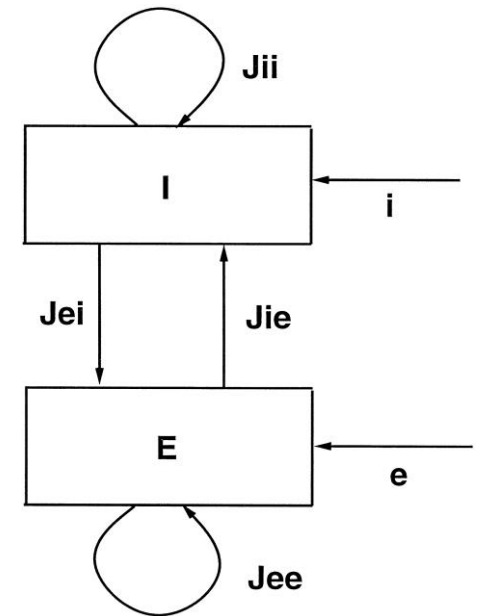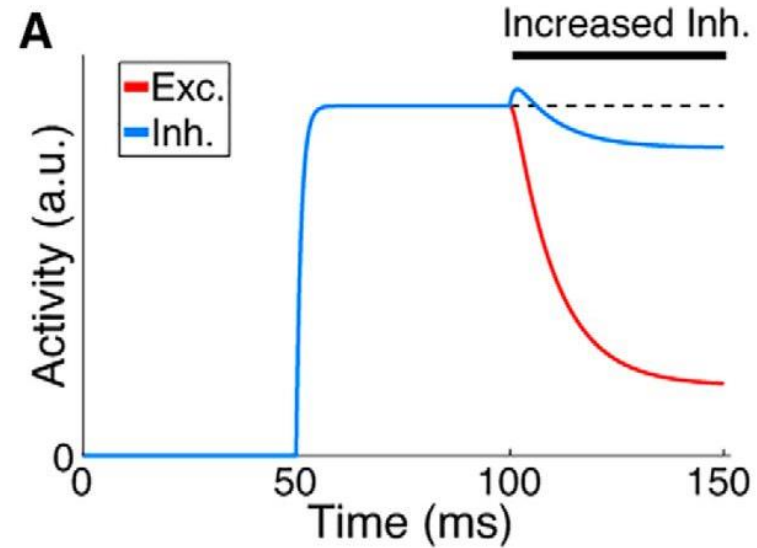
# Inhibitory Stabilization and Paradoxical Inhibition
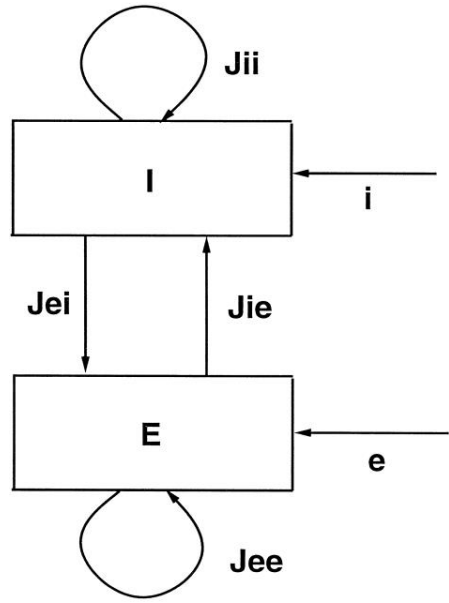
**Theory - Simulation - Experiment**



Tsodyks et al., 1997

Sadeh et al., 2017

Sanzeni et al., 2020

# Summary: E-I Networks

- Networks in the brain are made of excitatory and inhibitory neurons

- When coupled together, these can generate interesting dynamical behaviour, including:

- Balanced network dynamics (with asynchronous irregular firing)

- Synchronised dynamics (with large collective fluctuations)

- Paradoxical inhibition (where positive input to I cells decreases their firing rate)

# Summary of Neural Networks (Lecture 1)

- Networks can be used to perform computations

- Two main classes of network – feedforward and recurrent

- Two main strategies for modelling biological networks – spiking and firing rate

- Recurrent networks exhibit rich and complex dynamics

- During alert brain states, cortical networks are characterised by E-I balance, asynchronous activity, and inhibitory-stabilized dynamics

# Bibliography

- Lecture notes Ch 10

- Dayan and Abbott Ch 7 [network dynamics, firing rate vs spiking networks]

- Lamme and Roelfsema (2000)  [feedforward vs recurrent processing]

- Van Vreeswijk and Sompolinsky (1996) [balanced network dynamics]

- Harris and Thiele (2011) [two cortical states]

- Tsodyks et al. (1997) [paradoxical inhibition]