

Estimation

**CAN YOU
UNDERESTIMATE**



**YOUR OWN SKILL OF
ESTIMATION?**

Learning outcomes

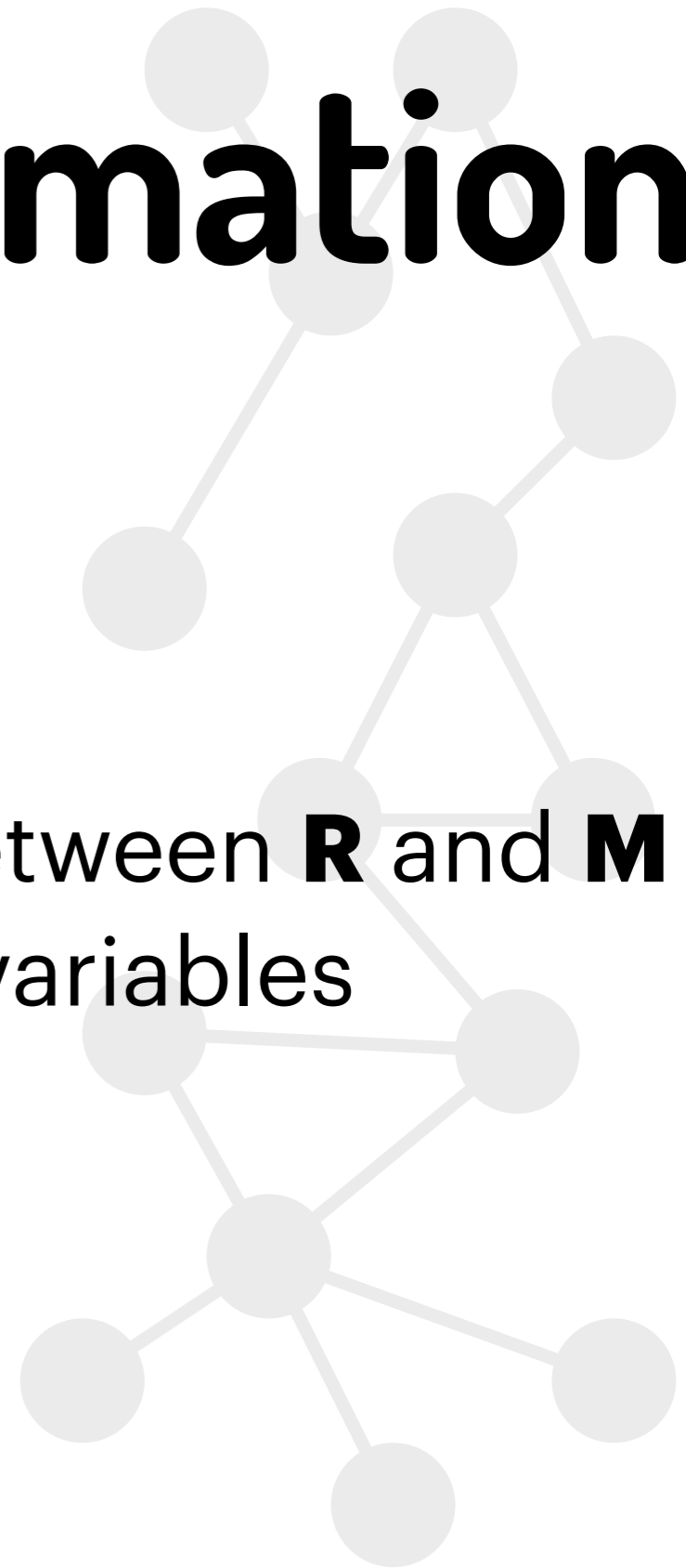


How to choose the **right data** for estimation
Implications of **ergodicity** on estimation
Use the **method of simulated moments**

Calibration vs estimation

Calibration: minimise the difference between **R** and **M**

Estimation: find the true values of the variables



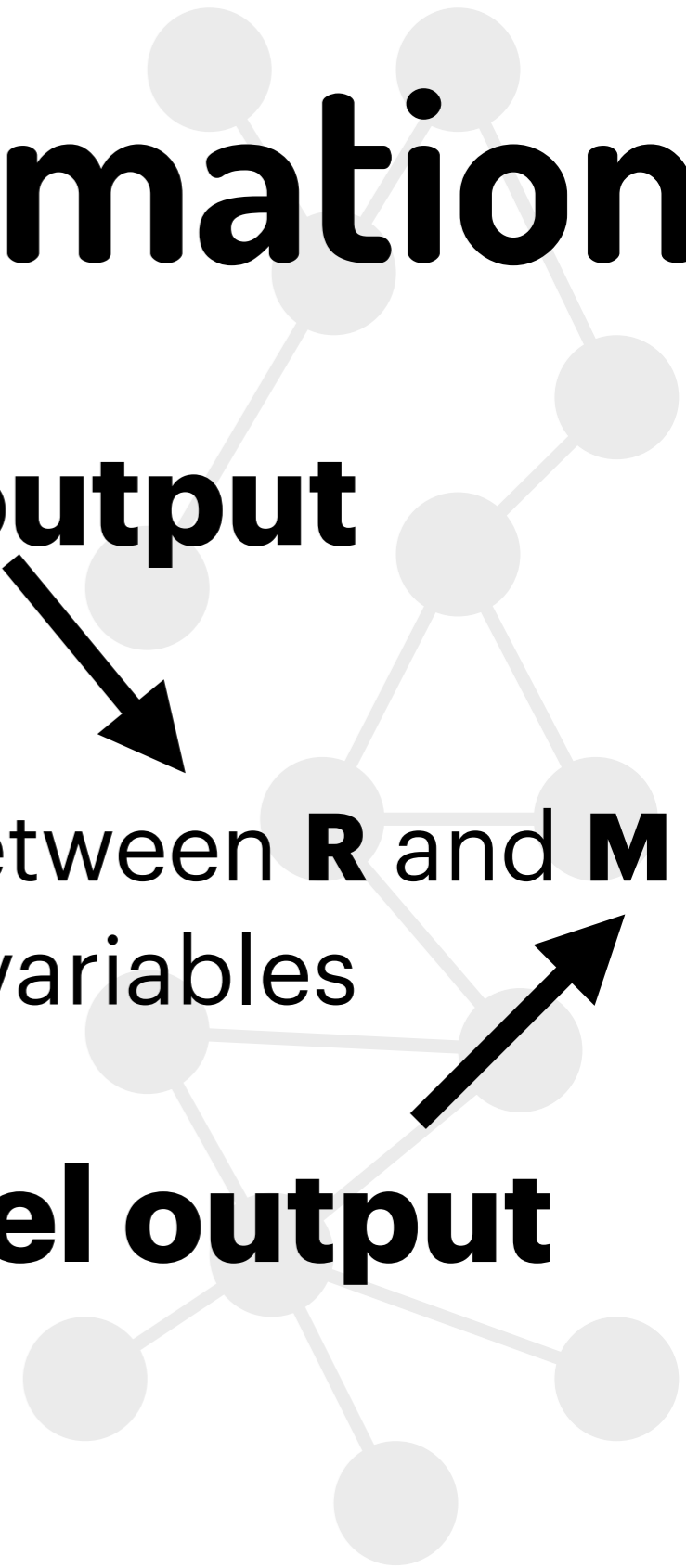
Calibration vs estimation

Real world output

Calibration: minimise the difference between **R** and **M**

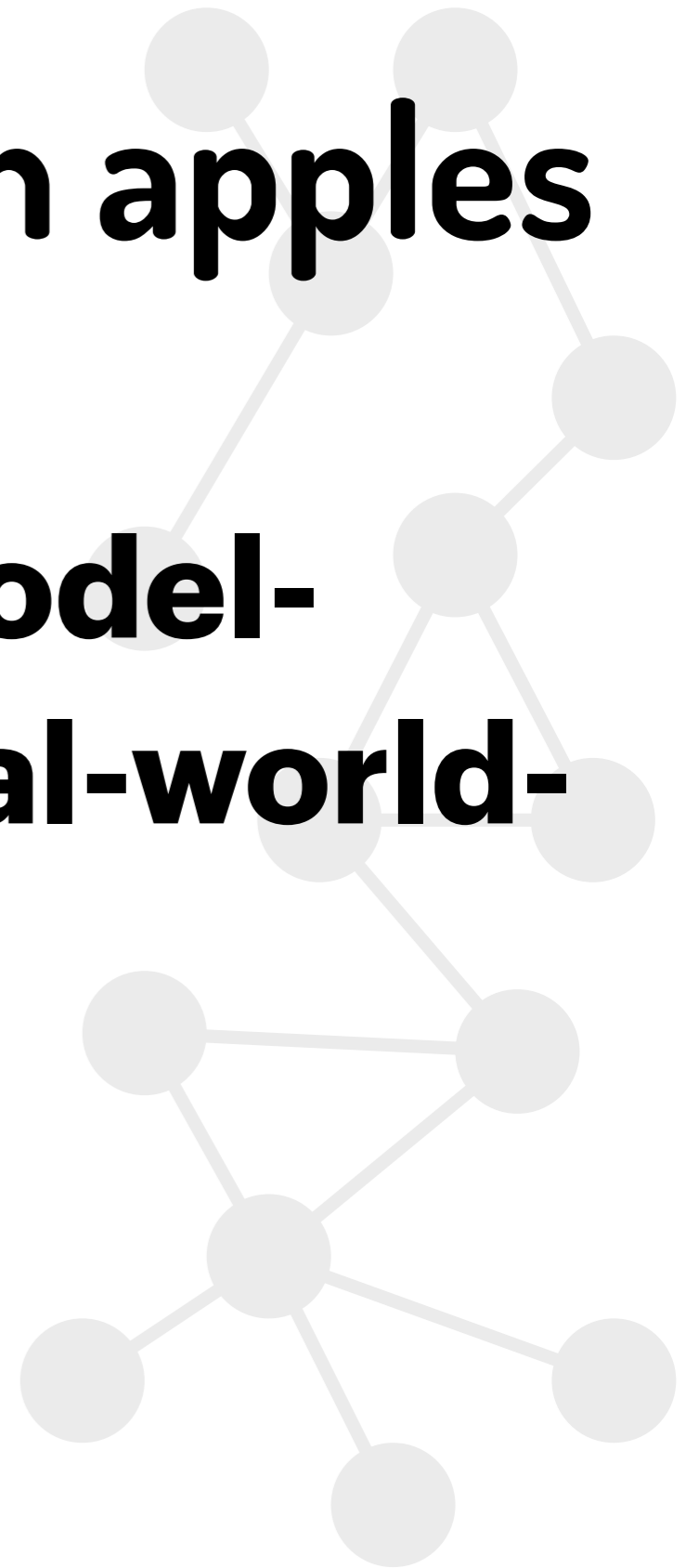
Estimation: find the true values of the variables

Model output



Comparing apples with apples

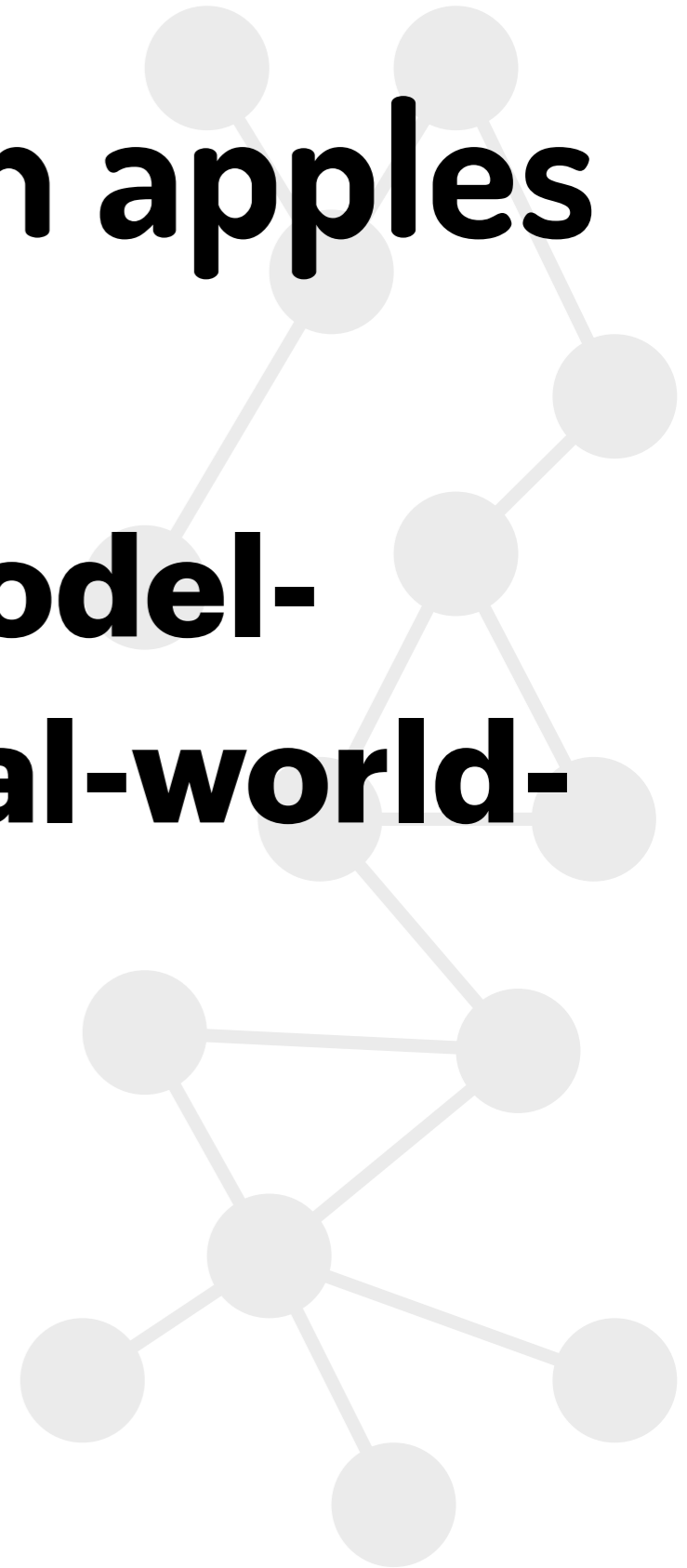
How do we compare the **model-produced data** with the **real-world-produced data**?



Comparing apples with apples

How do we compare the **model-produced data** with the **real-world-produced data**?

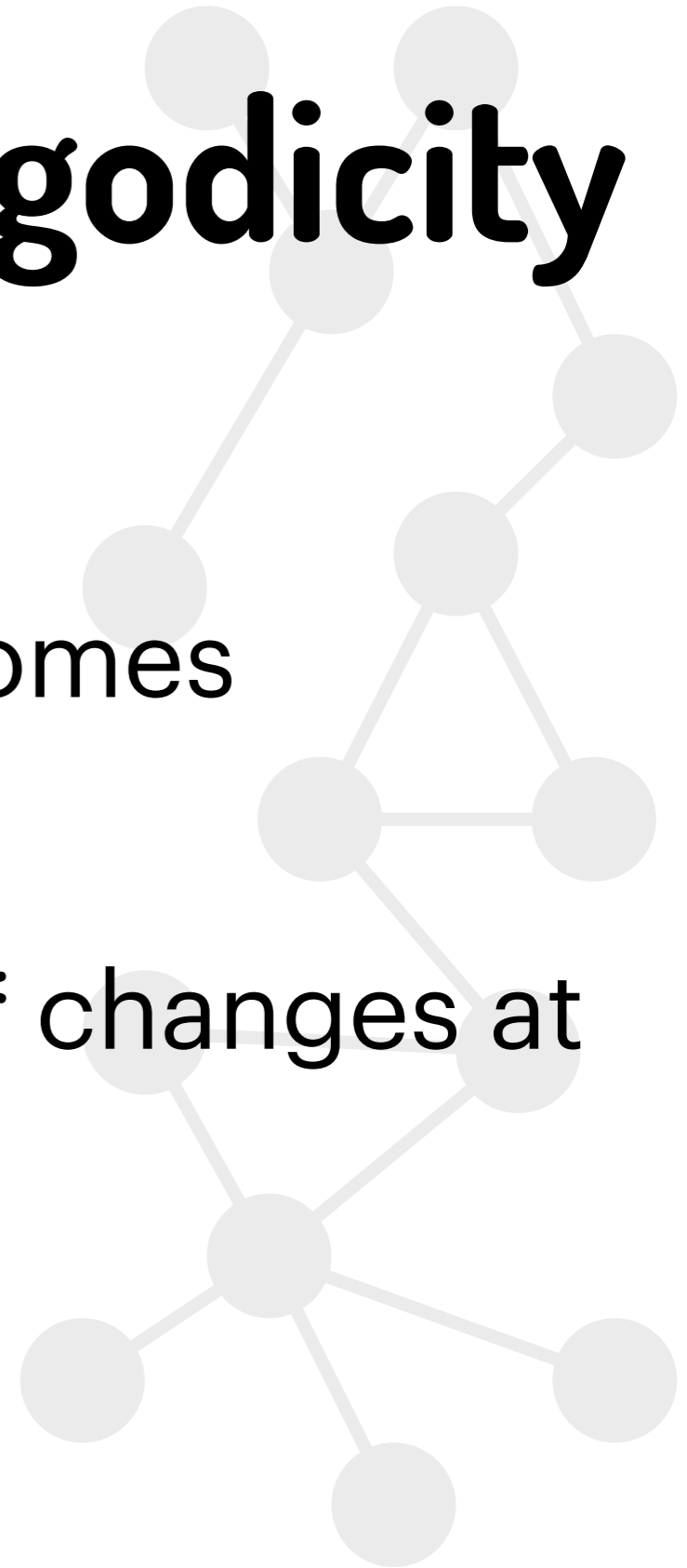
Look for equilibria!



The importance of ergodicity

Our model generates y_t , which becomes stationary with mean $\mu^* = r\theta$

Say the model is non-ergodic, so μ^* changes at every run, for the same θ



The importance of ergodicity

Our model generates y_t , which

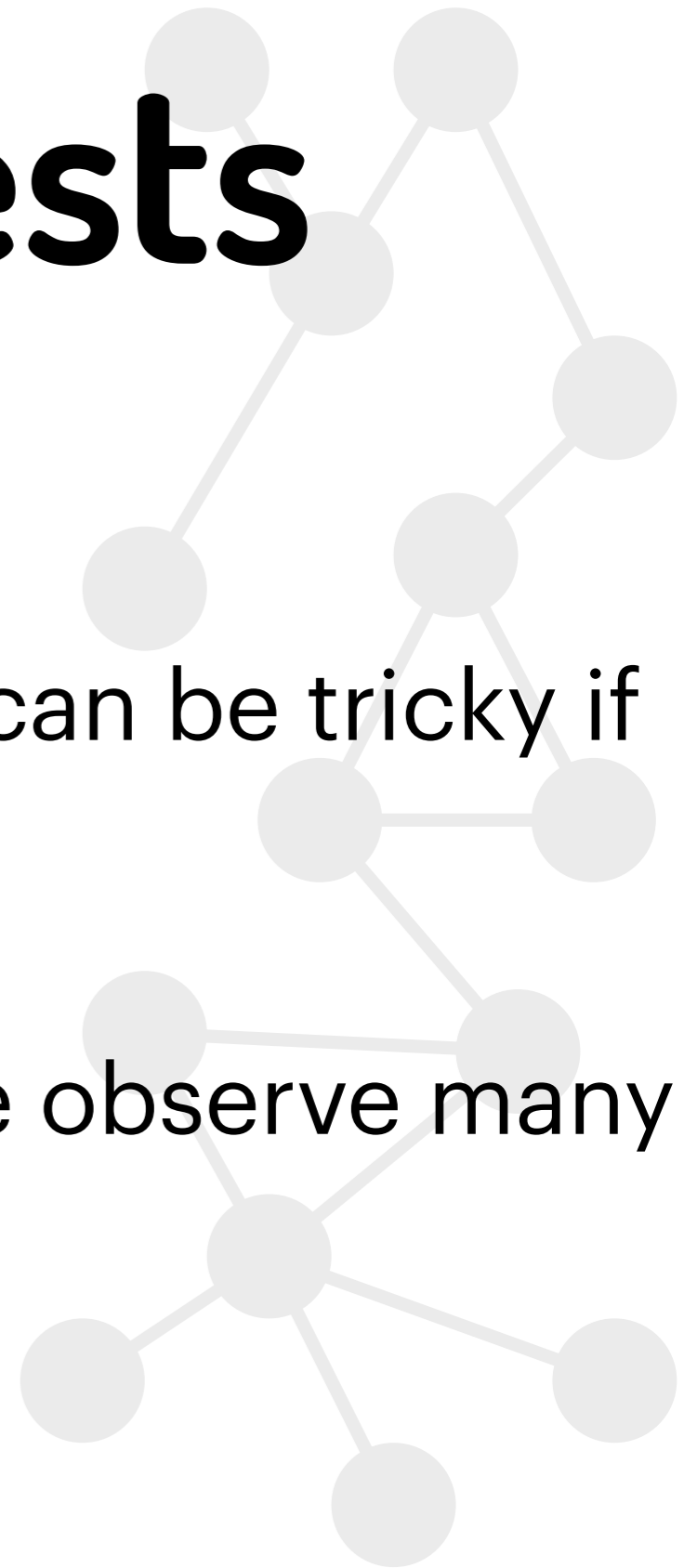
be **We need to understand the properties
of the model and of the data
before the estimation phase**

say, and the model is non-ergodic, so μ
changes at every run, for the same θ

Preliminary tests

Stationarity is easy to test but things can be tricky if the data is not stationary

Ergodicity cannot be tested unless we observe many realisations of the same process

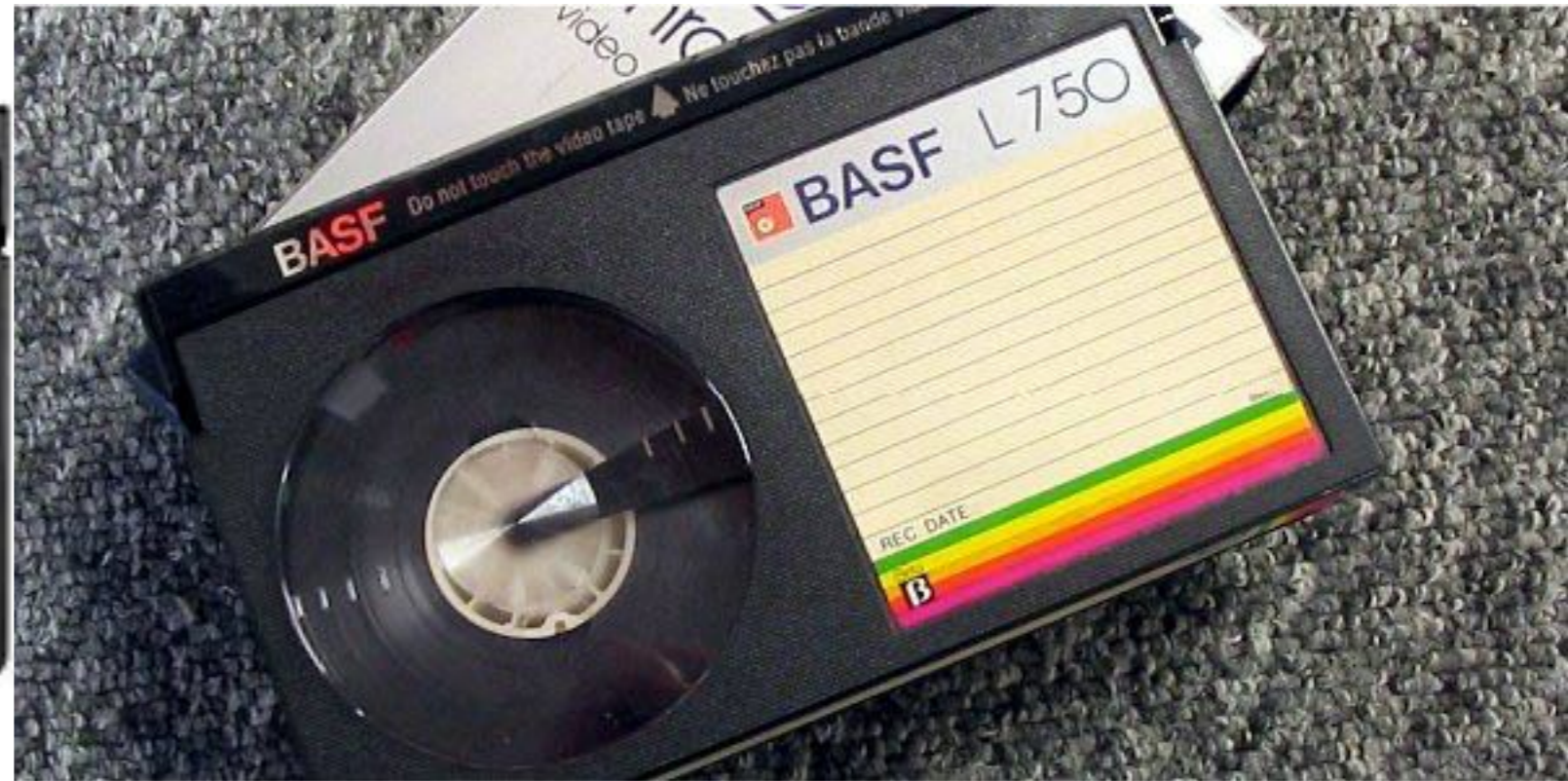


Example

JVC - vhs



Sony - betamax



Conclusion

If we, somehow, get to be fairly positive about the ergodicity of the system, then we can use that for estimation.

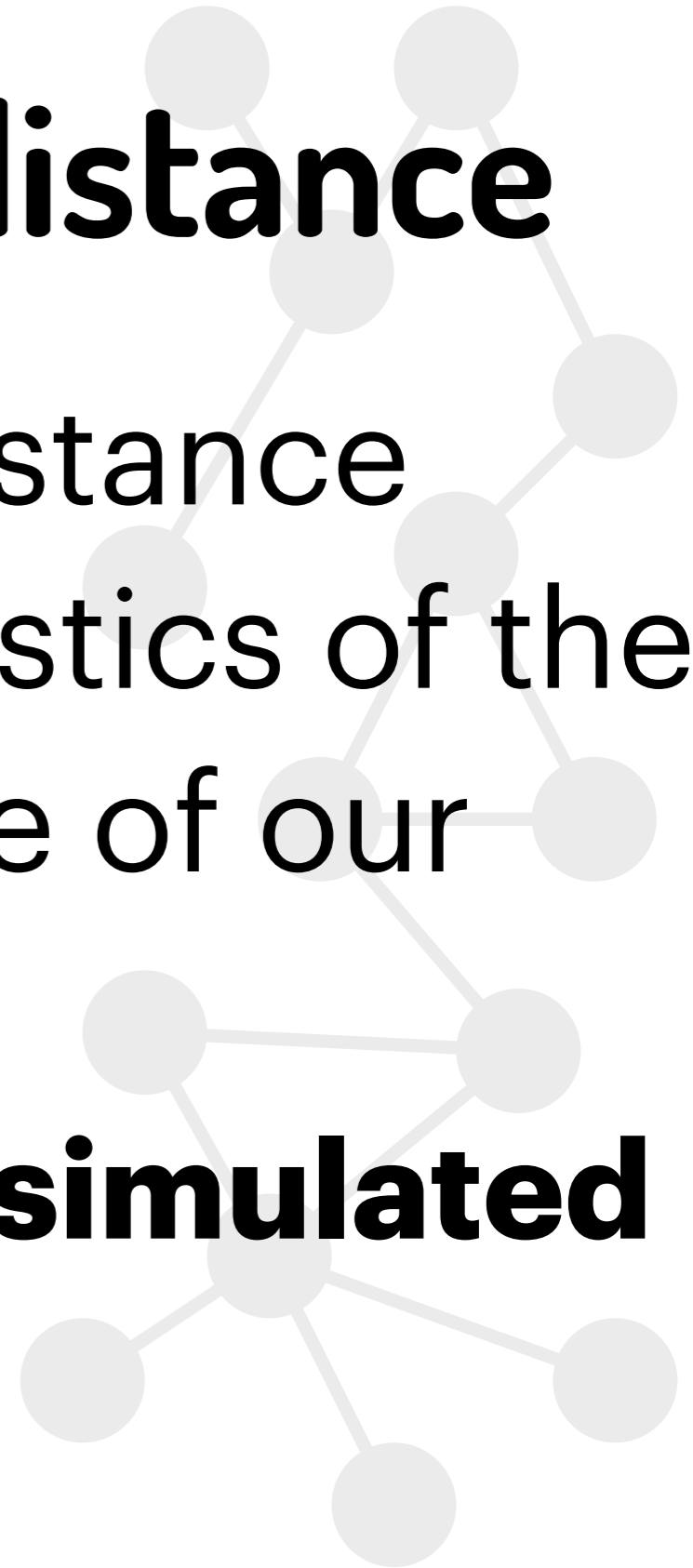
Otherwise there are other methods to deal with estimation (just wait a few slides)



Simulated minimum distance

We want to minimise the distance between the summary statistics of the real-world system and those of our model

We can use the method of simulated moments



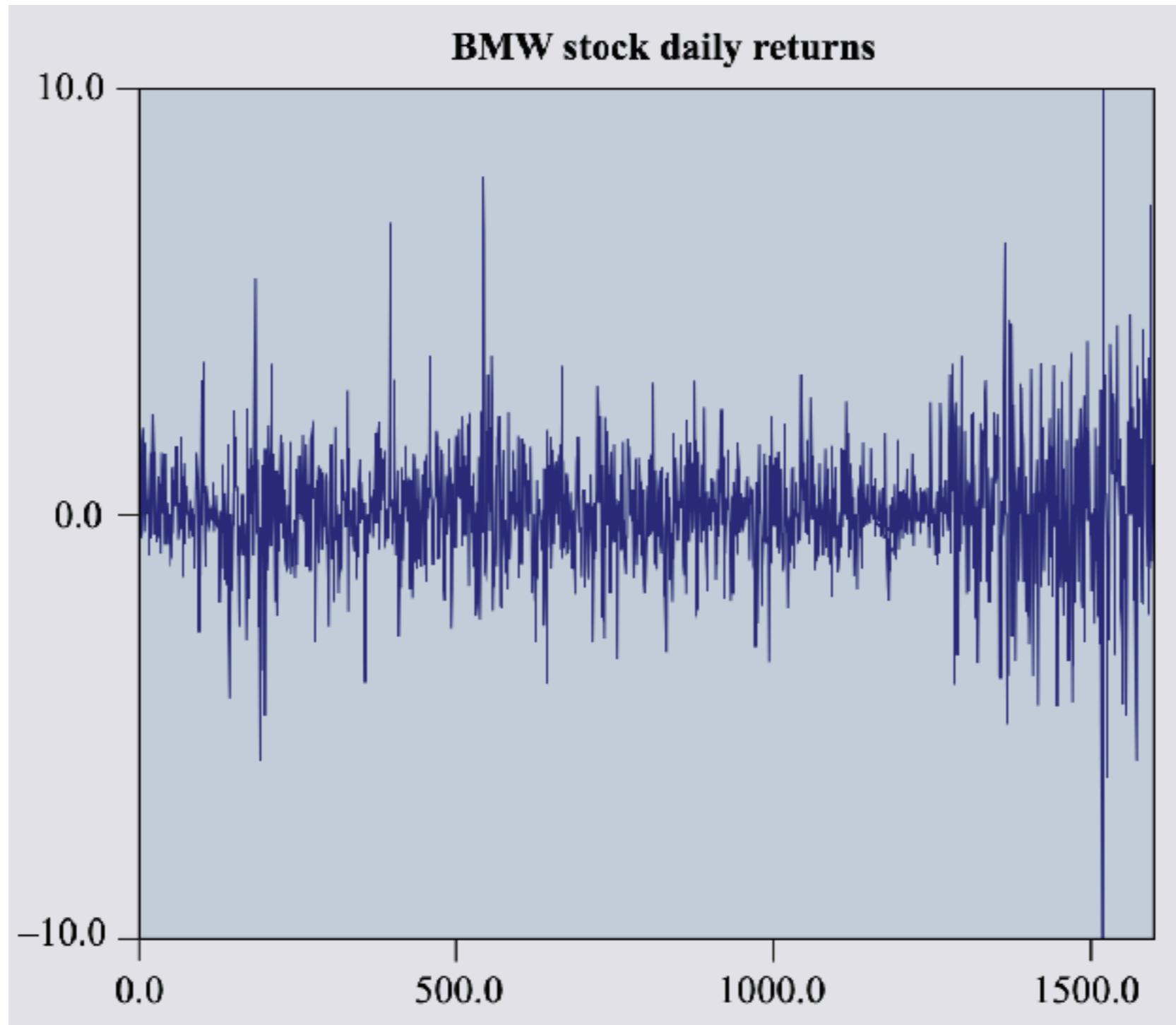
Method of simulated moments

$$\hat{\theta} = \underset{\theta}{\operatorname{argmin}} [\mu^*(\theta) - \mu_R]' W^{-1} [\mu^*(\theta) - \mu_R]$$

Weights

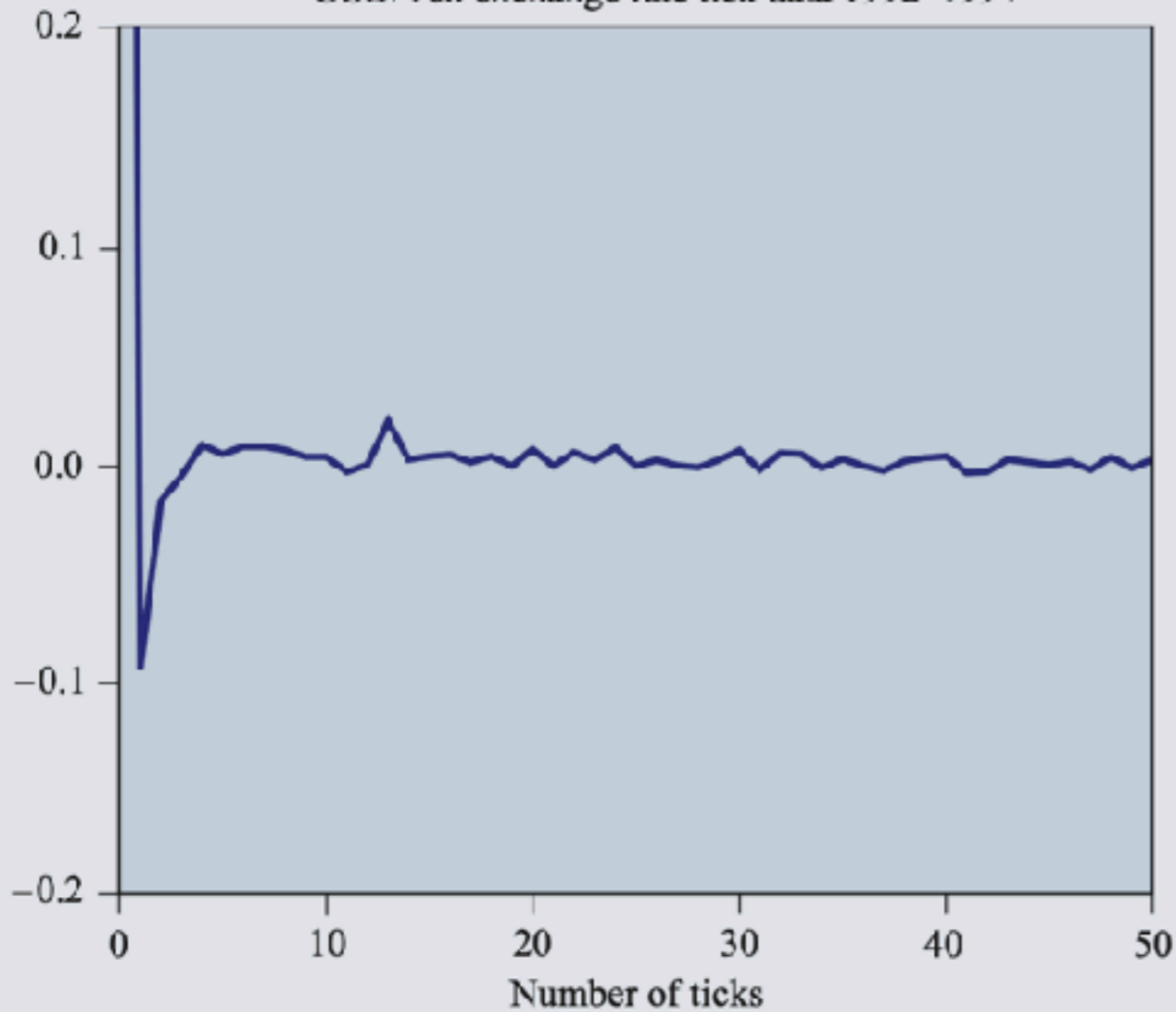


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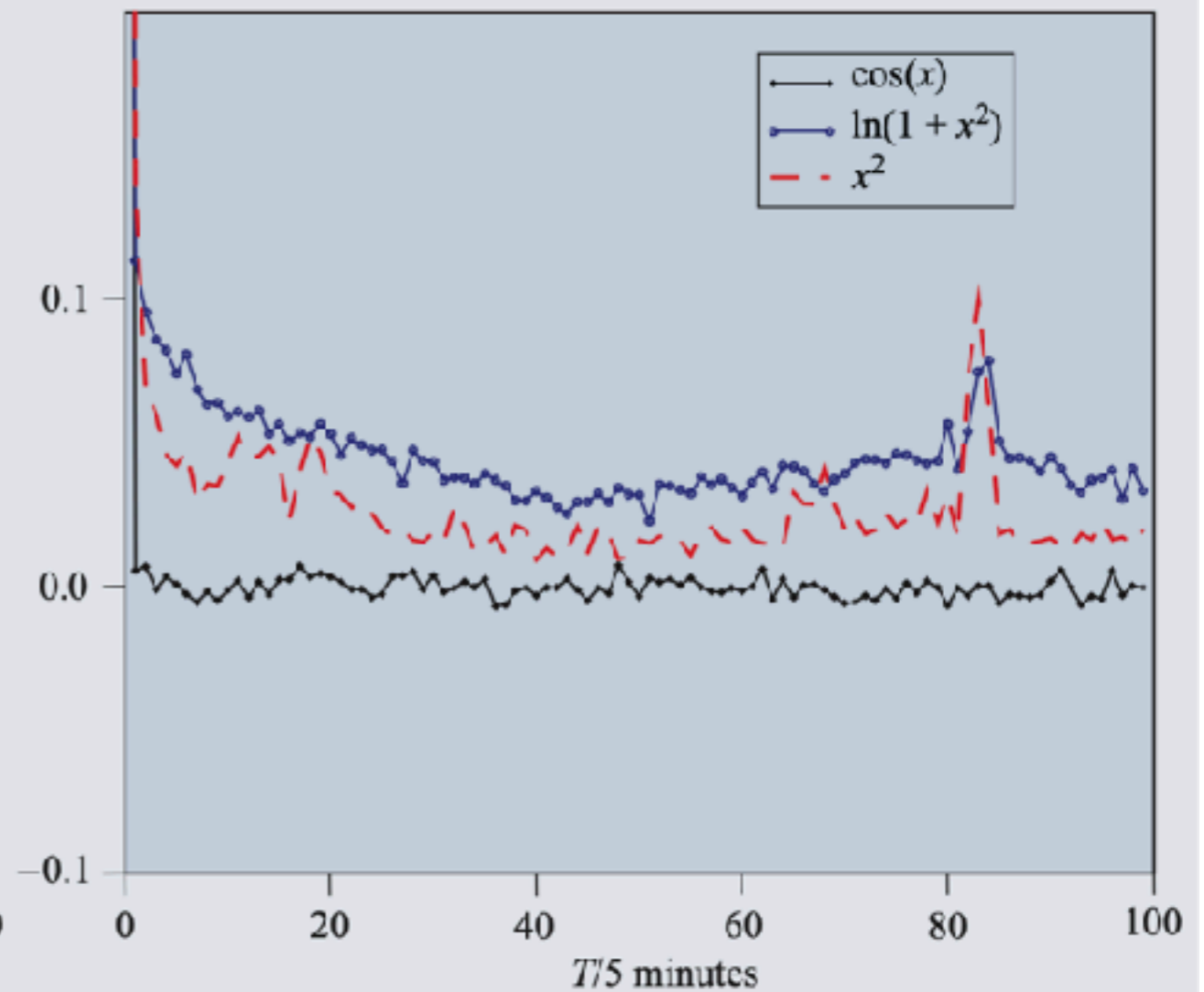


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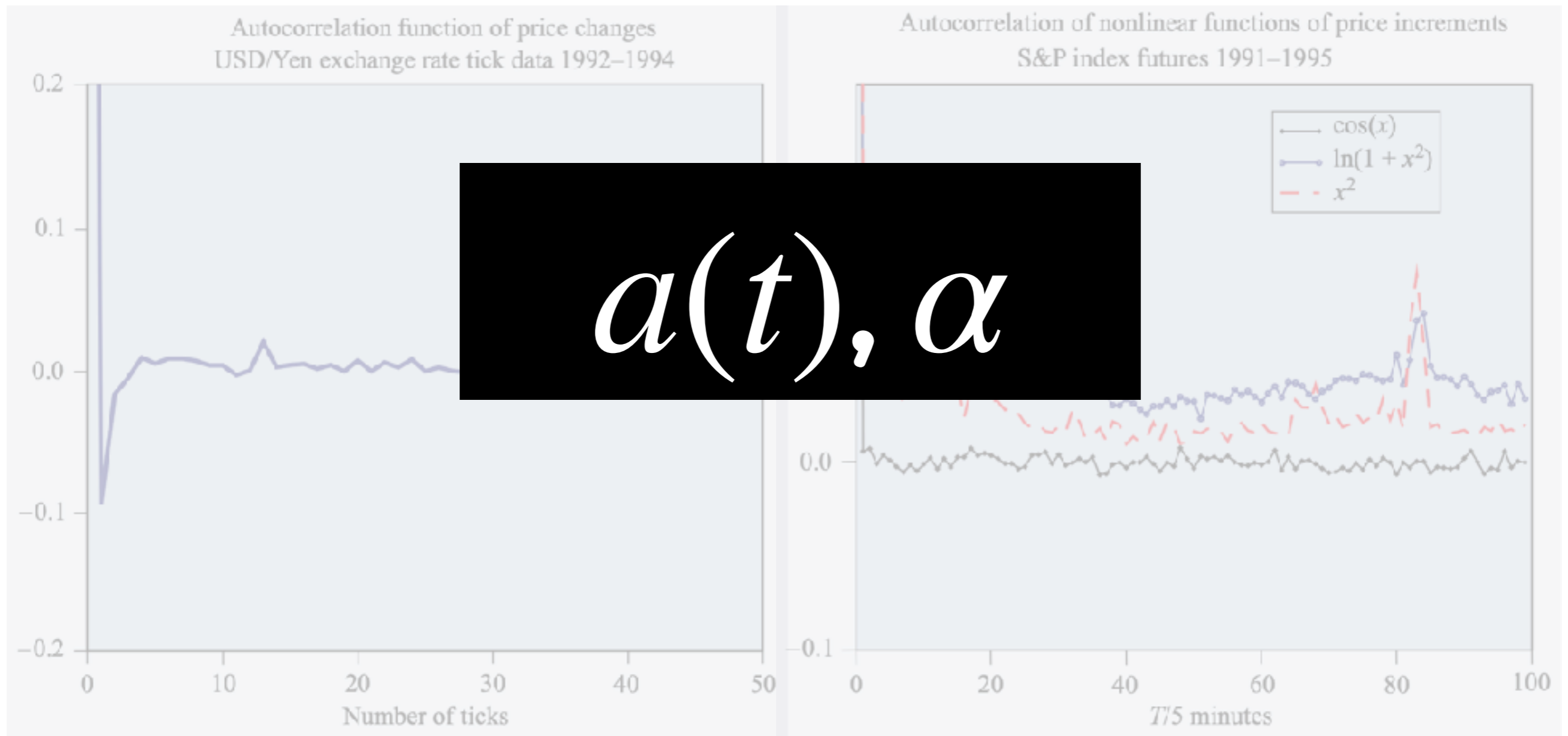
Autocorrelation function of price changes
USD/Yen exchange rate tick data 1992–1994



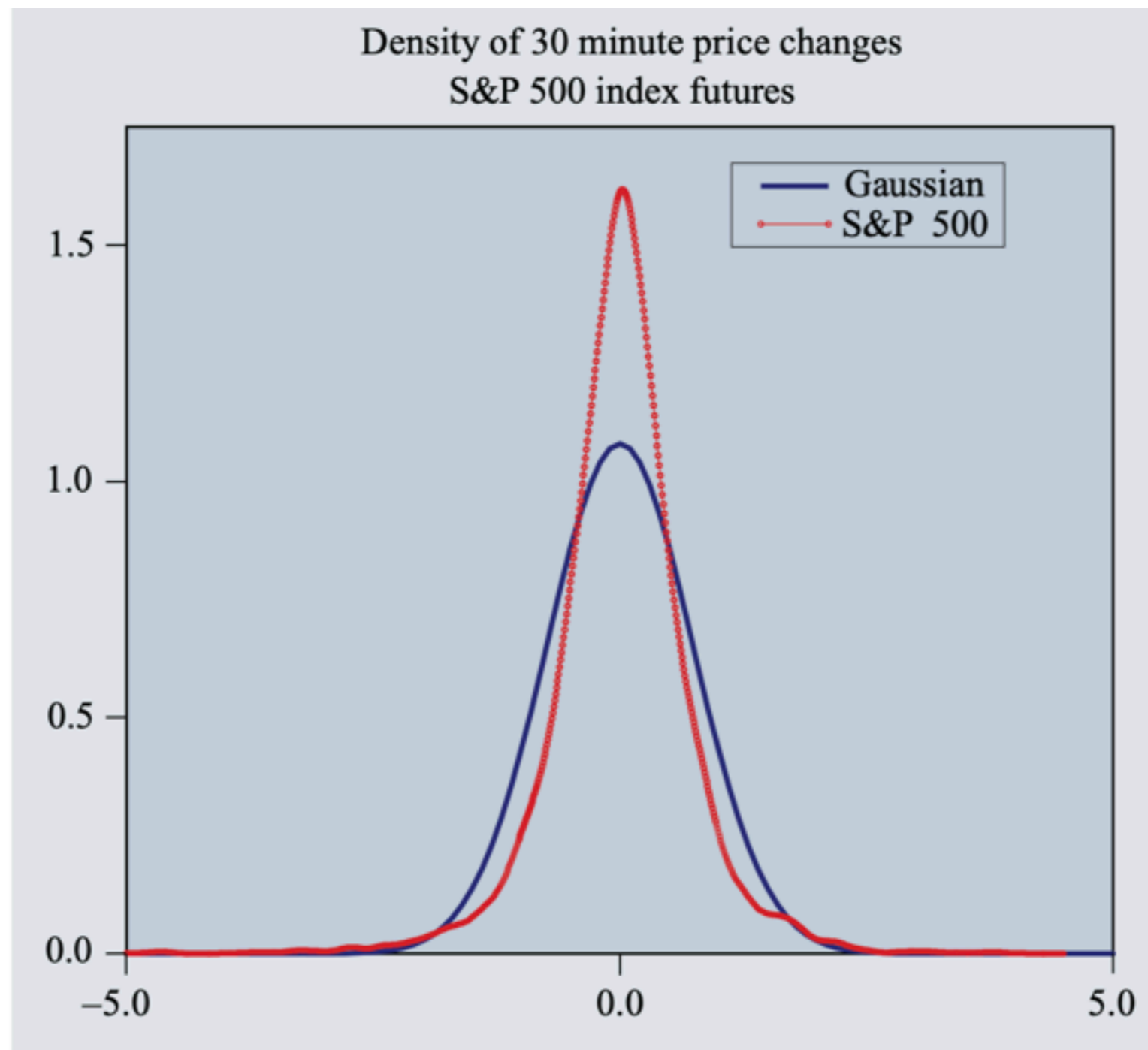
Autocorrelation of nonlinear functions of price increments
S&P index futures 1991–1995



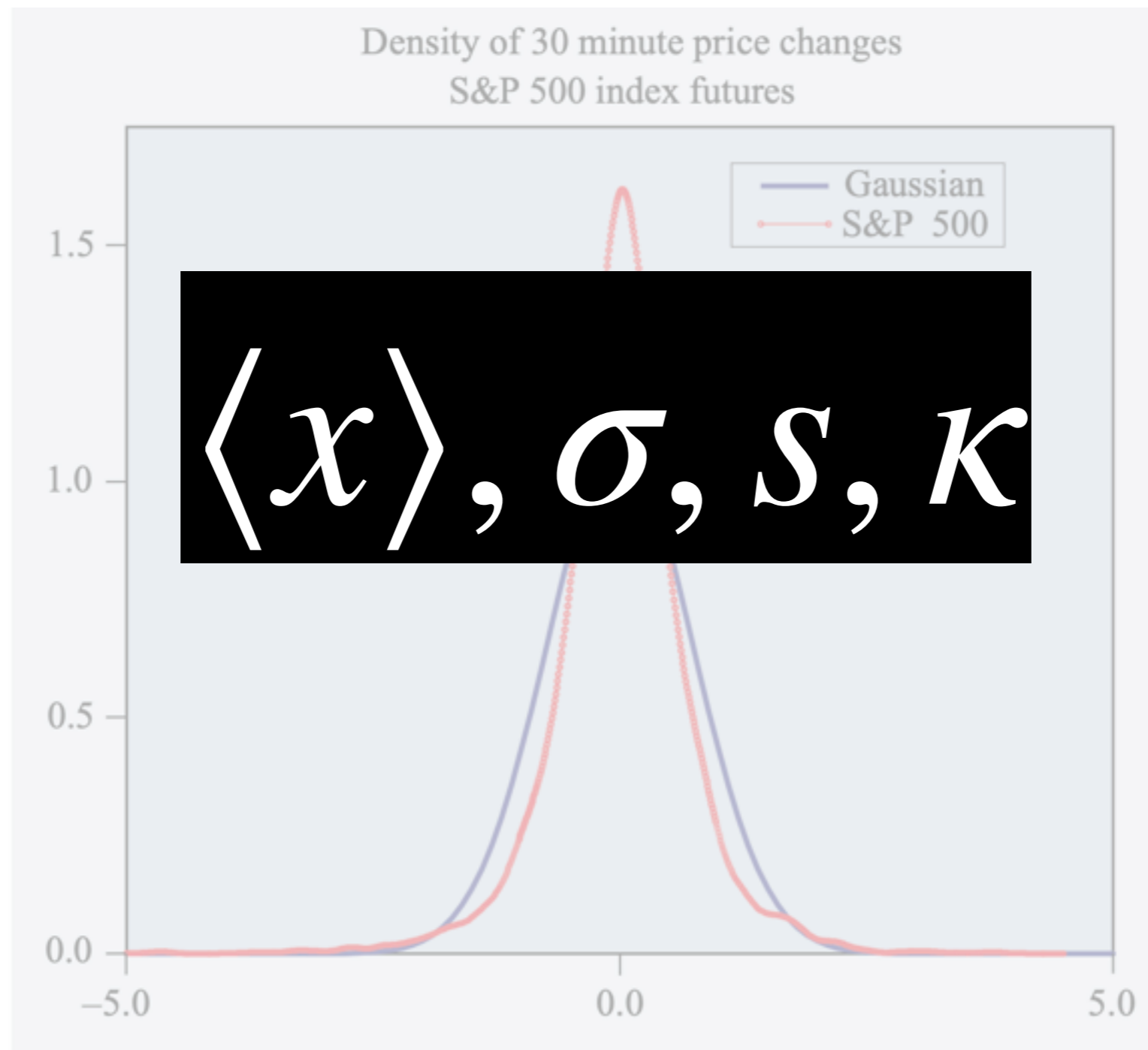
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Method of simulated moments

$$\hat{\theta} = \operatorname{argmin}_{\theta} [w_1(\hat{\kappa} - \kappa) + w_2(\hat{a}(0) - a(0)) + w_3(\hat{x} - \langle x \rangle)]$$

Method of simulated moments

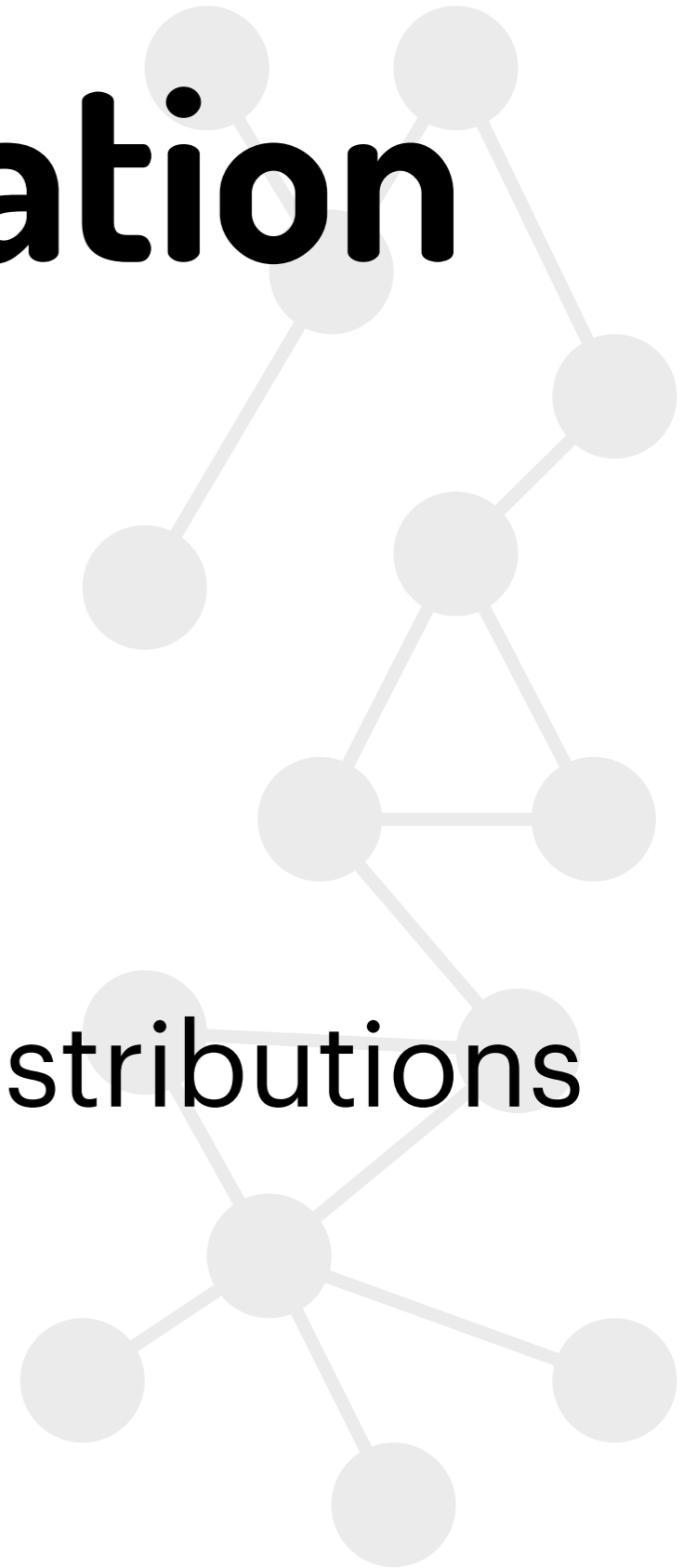
$$\hat{\theta} = \operatorname{argmin}_{\theta} [w_1(\hat{\kappa} - \kappa) + w_2(\hat{a}(0) - a(0)) + w_3(\hat{x} - \langle x \rangle)]$$

$$\hat{\theta} = \operatorname{argmin}_{\theta} [w_1(\hat{\kappa} - \kappa) + w_2(\hat{\lambda}_a - \lambda_a) + w_3(\hat{x} - \langle x \rangle)]$$

Bayesian estimation

More appropriate when:

- inference is needed
- there are prior and posterior distributions



Tesco example - Recap

One type of agents with heterogeneous variables

Variables: shopping habits, expenditure, bias on deals, etc.

Actions: buy (last year people also suggested “steal”)

Interactions: recommend products to others, interact with store



How would you use the data?

What summary statistics would you

use for estimation/calibration?

How to build abms cheat sheet

Nature of agents

List of variables describing their state

List of actions the agents can perform

Structure of their interaction with other agents

Agent design

Definition of output variables of interest

Appropriate experimental design

Analysis of equilibria

Sensitivity analysis

Experiment

How to build abms cheat sheet

Select the appropriate data
Input validation
Output validation



Validation

Select the appropriate data
Test for stationarity and ergodicity
Methods of simulated distances



Estimation

Congratulations!

**Now you know how to
build an agent-based
model**



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