Discrete Mathematics and Probability **Continuous Probability**
Session 2026/27, Semester 1 Week 9 Tutorial 7

If you need this document in another format then please contact course organiser Ian.Stark@ed.ac.uk

Homework 5 is currently running: ask your tutor if you have any questions about it; you can also discuss the work with other students in your tutorial.

Task A

Retrieve your submissions from Homework 4 in Week 8 as well as the solution notes on the course website. Compare solutions around the group.

How did you count the number of arrangements in Question 1(a)? What approach did you take to the calculation in Question 1(b)?

For Question 2, how did you calculate the probability that the box was accepted?

Task B

I roll a fair six-sided die repeatedly until I get a result that is more than two. This takes me K rolls, giving a random variable with geometric distribution $K \sim \text{Geom}(p)$ where p is the chance of succeeding in one roll. Calculate the following.

(a) The value of p.

(b) The chance that it takes me exactly three rolls to get this result.

(c) $P(K > 3)$, the probability that it takes more than three rolls.

(d) The expectation $\text{E}(K)$. (You can use the formula for expectation of geometric distribution from last week's lecture slides or the textbook.)

Task C

A commuter travels by train twice a day: heading into town in the morning and coming back home in the evening. Trains run every 20 minutes, but the commuter arrives at the station randomly and always takes the next train. This means waiting at the station between 0 and 20 minutes two times each day. These waits are distributed uniformly $\text{Unif}(0, 20)$ and it turns out that the total waiting time each day in minutes is a random variable T with the following PDF.

$$f(t) = \begin{cases} \dfrac{t}{400} & 0 \leq t < 20 \\ \dfrac{40 - t}{400} & 20 \leq t < 40 \\ 0 & t < 0 \text{ or } t \geq 40 \end{cases}$$

(a) Sketch a graph of the probability density function $f(t)$.

(b) Calculate the corresponding cumulative distribution function $F(t)$ for the random variable T. Sketch the graph of $F(t)$. (It is possible to do this by integration, but it's not essential and you may find it simpler to use geometry to calculate the area of certain triangles.)

(c) What is the probability that tomorrow the commuter has to wait no more than 10 minutes in total?