Informatics 1 Introduction to Computation Lecture 14

Laziness, Higher-order, and Sorting

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Part I

The importance of being lazy

Searching for the first odd number

Quickcheck

```
prop_odd :: Int -> Bool
prop_odd n = a == b && b == c
  where
  a = ho n
  b = comp n
  c = rec n

[1 of 1] Compiling Main
Ok, one module loaded.
> quickCheck prop_odd
+++ OK, passed 100 tests.
```

Timing

```
> :set +s
> ho 1000000
[1]
(0.00 secs, 64,776 bytes)
> comp 1000000
[1]
(0.00 secs, 64,984 bytes)
> rec 1000000
[1]
(0.00 secs, 65,168 bytes)
```

How it works: rec

```
rec :: Int -> [Int]
rec n = helper 0
 where
 helper :: Int -> [Int]
 helper i | i > n = []
           \mid odd i = [i]
           | otherwise = helper (i+1)
 rec 1000000
=
 helper 0
=
 helper 1
 [1]
```

How it works: ho

```
ho :: Int -> [Int]
ho n = (take 1 . filter odd) [0..n]
  ho 1000000
=
  (take 1 . filter odd) [0..1000000]
=
  take 1 (filter odd | [0..1000000]
  take 1 (filter odd (0 : |[1..1000000]|))
=
  take 1 (filter odd (1 : | [2..1000000] |))
=
  take 1 (1 : filter odd | [2..1000000] |)
=
  1 : take 0 (filter odd | [2..1000000] |)
=
  1: []
```

Part II

Sum of odd squares three ways

Sum of odd squares

Quickcheck

```
prop_sqr :: Int -> Bool
prop_sqr n = a == b && b == c
  where
  a = ho n
  b = comp n
  c = rec n

Ok, one module loaded.
> quickCheck prop_sqr
+++ OK, passed 100 tests.
```

Runtimes in ghci

```
> :set +s
> ho 1000000
1666666666666500000
(0.43 secs, 596,687,792 bytes)
> comp 1000000
16666666666666500000
(0.67 secs, 628,685,832 bytes)
> rec 1000000
1666666666666500000
(1.02 secs, 692,881,968 bytes)
```

The Moral

Usually coding involves tradeoffs: simple and slow

VS.

complex and fast.

The big win is when you can find a way to be both *simple* and *fast*.

Part III

Sorting three ways

Insertion sort

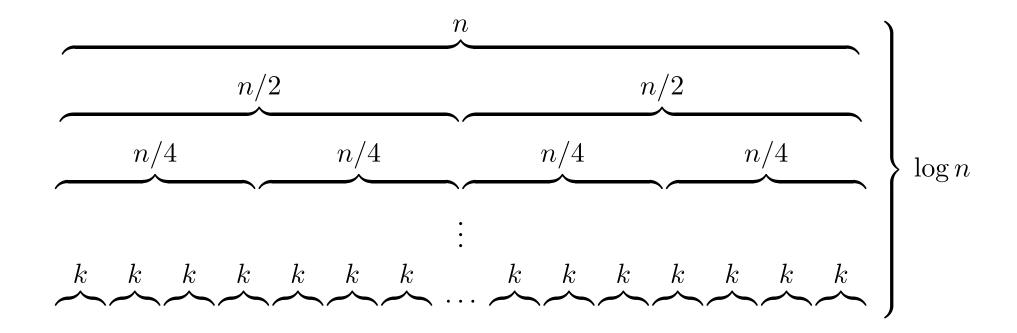
```
foldr :: (a -> b -> b) -> b -> [a] -> b
foldr f e [] = e
foldr f e (x:xs) = x 'f' foldr f e xs
  foldr f e [x,y,z] = (x 'f' (y 'f' (z 'f' e)))
isort :: Ord a => [a] -> [a]
isort = foldr insert []
 where
 insert :: Ord a => a -> [a] -> [a]
                               = [X]
 insert x []
 insert x (y : ys) | x \le y = x : y : ys
                   | otherwise = y : insert x ys
```

Quicksort

```
qsort :: Ord a => Int -> [a] -> [a]
qsort k xs | length xs <= k = isort xs
qsort k (y:xs) =
  qsort k [ x | x <- xs, x < y ]
  ++ [ y ] ++
  qsort k [ x | x <- xs, x >= y ]
```

Merge sort

Why quicksort and mergesort are $O(n \log n)$



- number of elements to be sorted
- k cutoff size

Part IV

A few graphs

