Inf2 - Foundations of Data Science: Multiple logistic regression for explanation and prediction



THE UNIVERSITY of EDINBURGH informatics

FOUNDATIONS OF DATA SCIENCE

Announcements

- Week 4 workshop - we'll look at the paper that we'll be refer to in the exam

- Uses concepts from today's lecture!
- Solutions for Week 3 Workshop now available
- Solutions for this Week 4 Workshop will be available later in the week
- Badges on order!

Where we're at in the Maximum Likelihood Principle and Regression

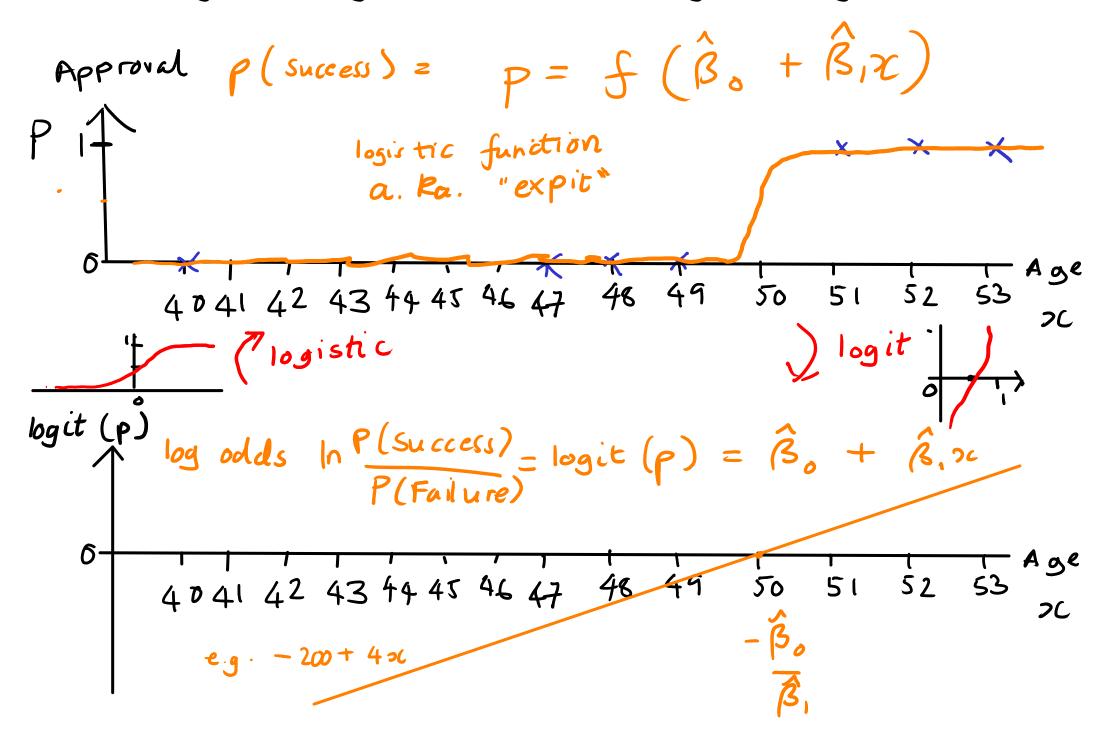
Week 4: Logistic regression

Week 5: The maximum likelihood principle, and how we can use it to derive linear, logistic and other types of regression

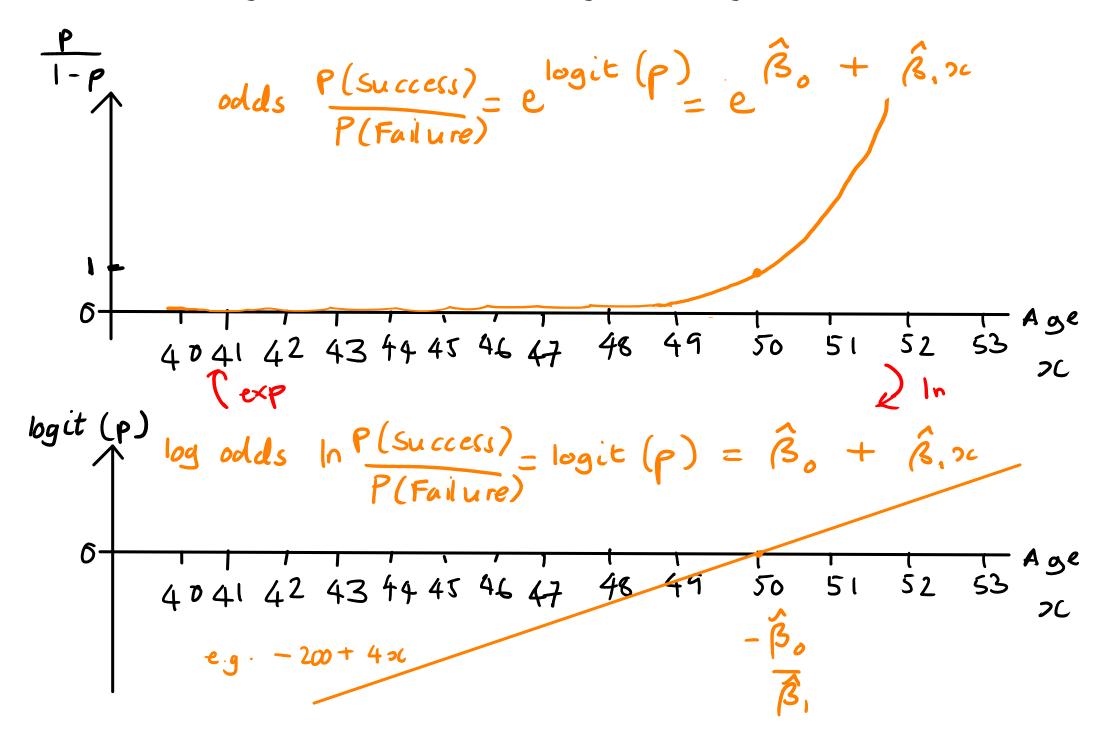
Today

- Recap
- Multiple Logistic Regression
- Confidence intervals on coefficients
- Machine learing: Logistic Regression as a classifier
- Ethics of logistic regression

Probability and log odds views of logistic regression



Odds and log odds views of logistic regression



Binary variables: odds and odds ratios

$$P(\gamma = y | X = z)$$

	_			C Emproyed		
	Approved	Not approved	Approval odds	_		
Employed				OR(x) = 2.42 0.34		
0	0.25	0.75	0.34	7 = 7.09		
1	0.71	0.29	2.42			
				- Effect sizc		
(669 0/0					
			, "Approved"] "Eman" ?			
2		Vot Emp.	, "Emp."]			
Odds (Sucress) = P(Success) = P(Success)						
			P(Sailure)	1 - P(Succs)		
			B11.16	(1) = -True		

P(Sucess) Odde (Snaces) x=True) Odds rabid OR(x) -Odds (success) x = False)

Age 1

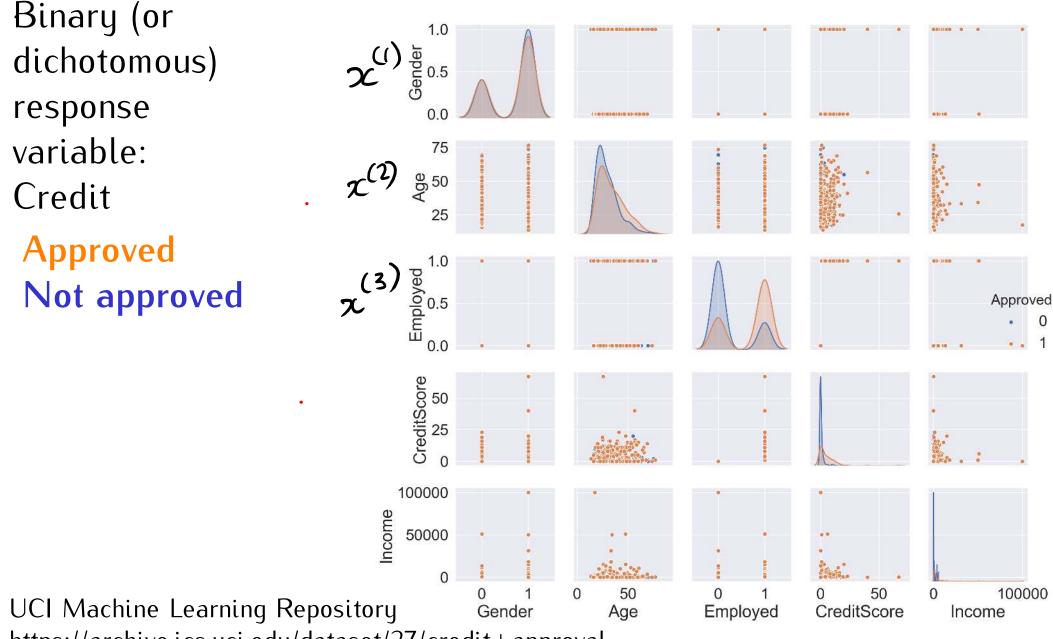
Inf2 – Foundations of Data Science: Multiple logistic regression



THE UNIVERSITY of EDINBURGH informatics

FOUNDATIONS OF DATA SCIENCE

Supervised classification



https://archive.ics.uci.edu/dataset/27/credit+approval

Principle of multiple logistic regression

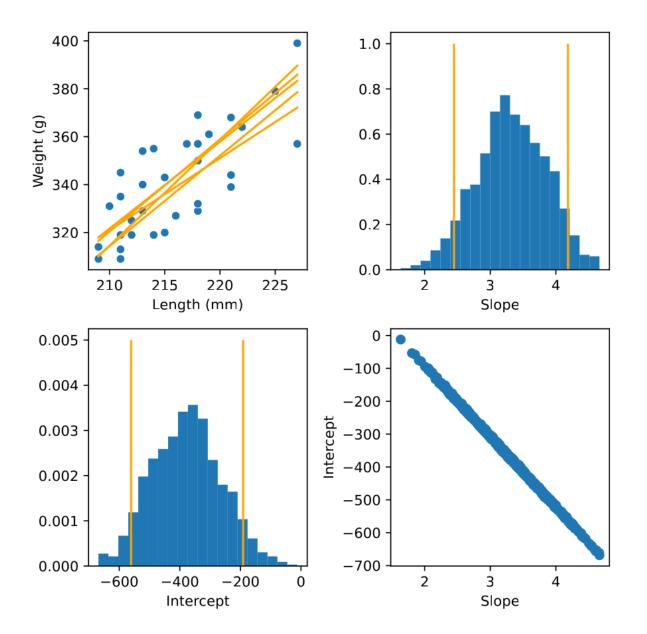
Predictor variables
$$x^{(1)}$$
: Age
 $x^{(2)}$: Employment

$$P(\gamma = | | x^{(1)}, x^{(2)}, ...) = f(\beta_0 + \beta_1 x^{(1)} + \beta_2 x^{(2)} + ...)$$

Multiple logistic regression applied to the credit example

	Variable	Coefficient	Odds or OR
\hat{eta}_0	Intercept	-1.969	0.140
$\hat{oldsymbol{eta}}_1$	Age	0.029	1.030
$\hat{oldsymbol{eta}}_2$	Employed	1.881	6.562

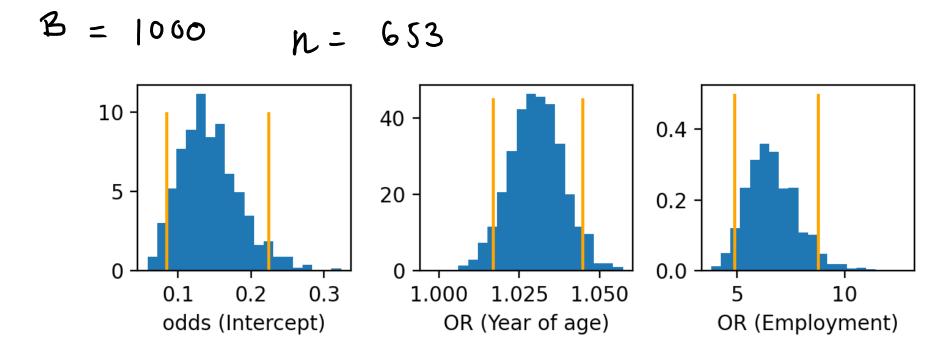
Boostrap confidence intervals for regression coefficients



Demo

Code this for Logistic Regression in the lab!

Bootstrap confidence intervals



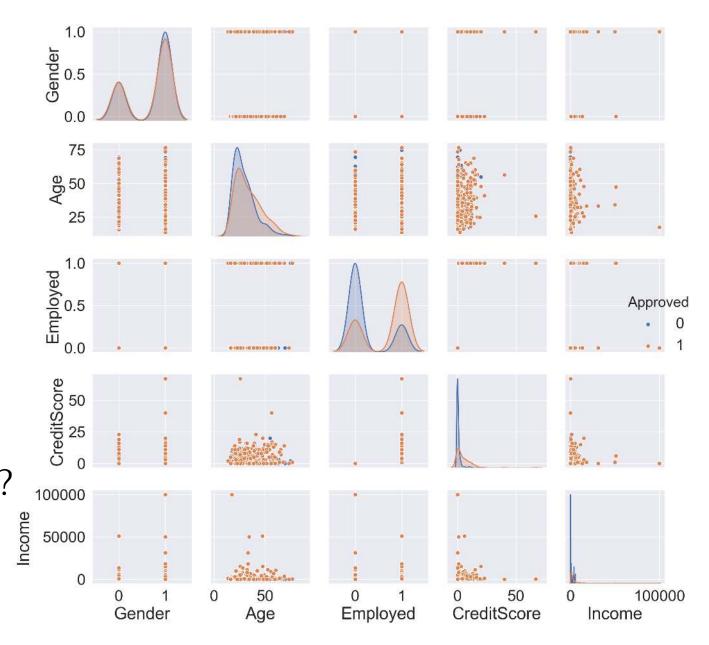
Does age affect credit approval?

Discussion question

Our analysis so far shows that age and credit approval are related.

So all other things being equal, a 20 year old is less likely to have credit approved than a 50 year old.

Do we believe this yet? What further analysis should we do?



Explanation - "controlling for", "adjusting for"

This week's lab

Multiple logistic regression on fuller set of variables

Using Logsitic Regression as a Machine Learning algorithm

Inf2 - Foundations of Data Science: The logistic regression classifier



THE UNIVERSITY of EDINBURGH informatics

FOUNDATIONS OF DATA SCIENCE

Converting logistic regression to a classifier

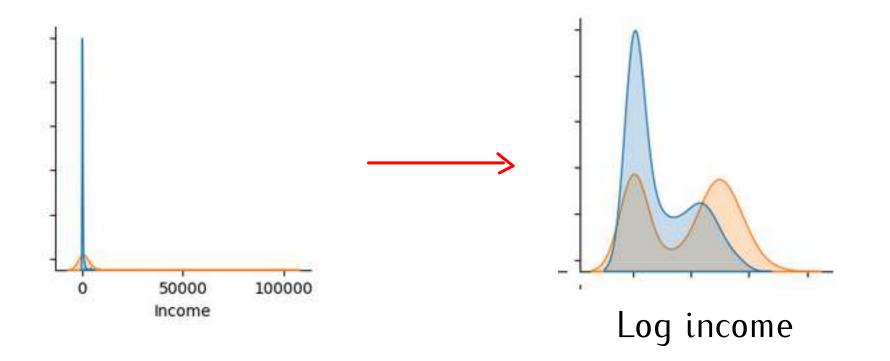
- Fit logistic regression model to data
- Set threshold in terms of log odds and apply to predicted log odds

$$\hat{\beta}_{0} + \hat{\beta}_{1} \chi^{(1)} + \hat{\beta}_{2} \chi^{(2)} + \dots \quad 7C \implies \hat{y} = 1$$

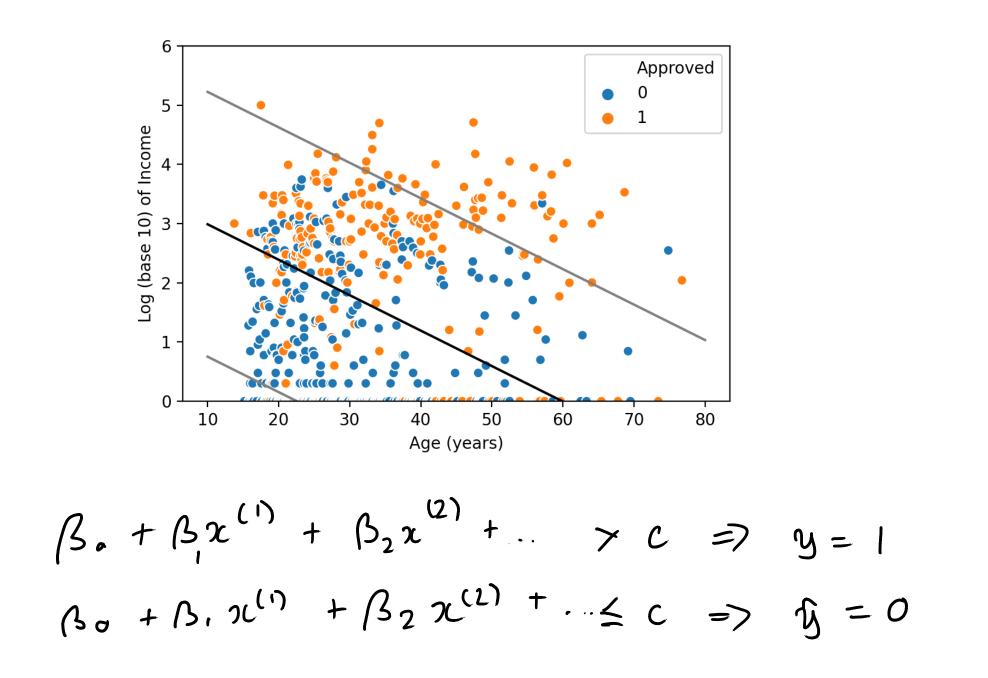
$$\hat{\beta}_{0} + \hat{\beta}_{1} \chi^{(1)} + \hat{\beta}_{2} \chi^{(2)} + \dots < C \implies \hat{y} = 0$$

C = 0 = 7 odds of 1 = 7 p = 0.5

Machine learning trick: make marginal distributions more normal



Decision boundary



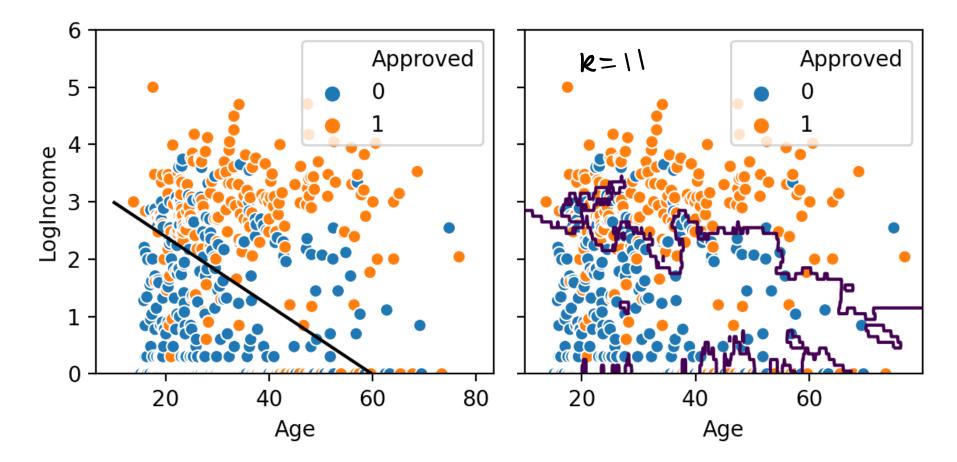
Ethics: logistic regression can be transparent

Credit scoring system:

- If you are in employment you score 1.625, if not you score 0
- Multiply your age by 0.029 and add the result to your score
- Round your income to the nearest 1000. Multiply the number of zeros in this figure by 0.320 and add the result to your score
- If you scored more than 2.246, your credit will be approved

Cf. "Promote Values of Transparency, Autonomy and Trustworthiness" (Vallor, 2018)

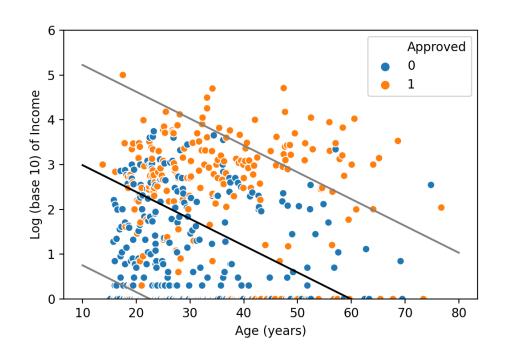
Logistic regression versus k-NN



Decision boundary, flexibility/over-fitting, transparency

Standardised input variables

Receiver-operator characteristic



Sensitivity

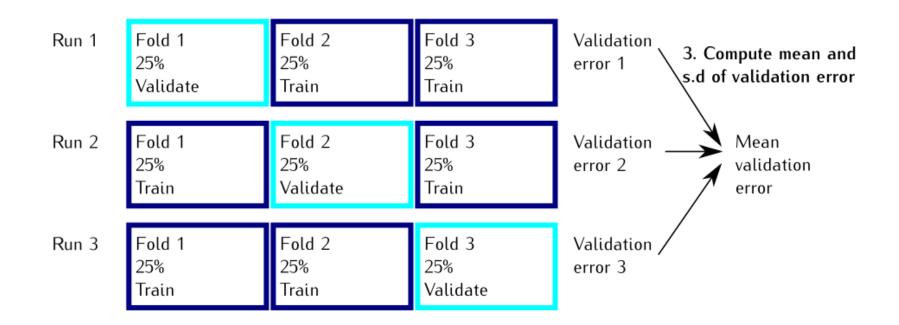
Selectivity/ Specificity

False positive rate

9



Cross validation for predicting metrics



c.f. Chapter 12 of the lecture notes

Summary - Interpret $\hat{\beta}_{o}$ and $\hat{\beta}_{i}$, in terms of log odds

- Extend logistic regression to multiple variables
- Use logistic regression as a classifier
- Practiccal and ethical pros and cons of logistic regression versus other methods