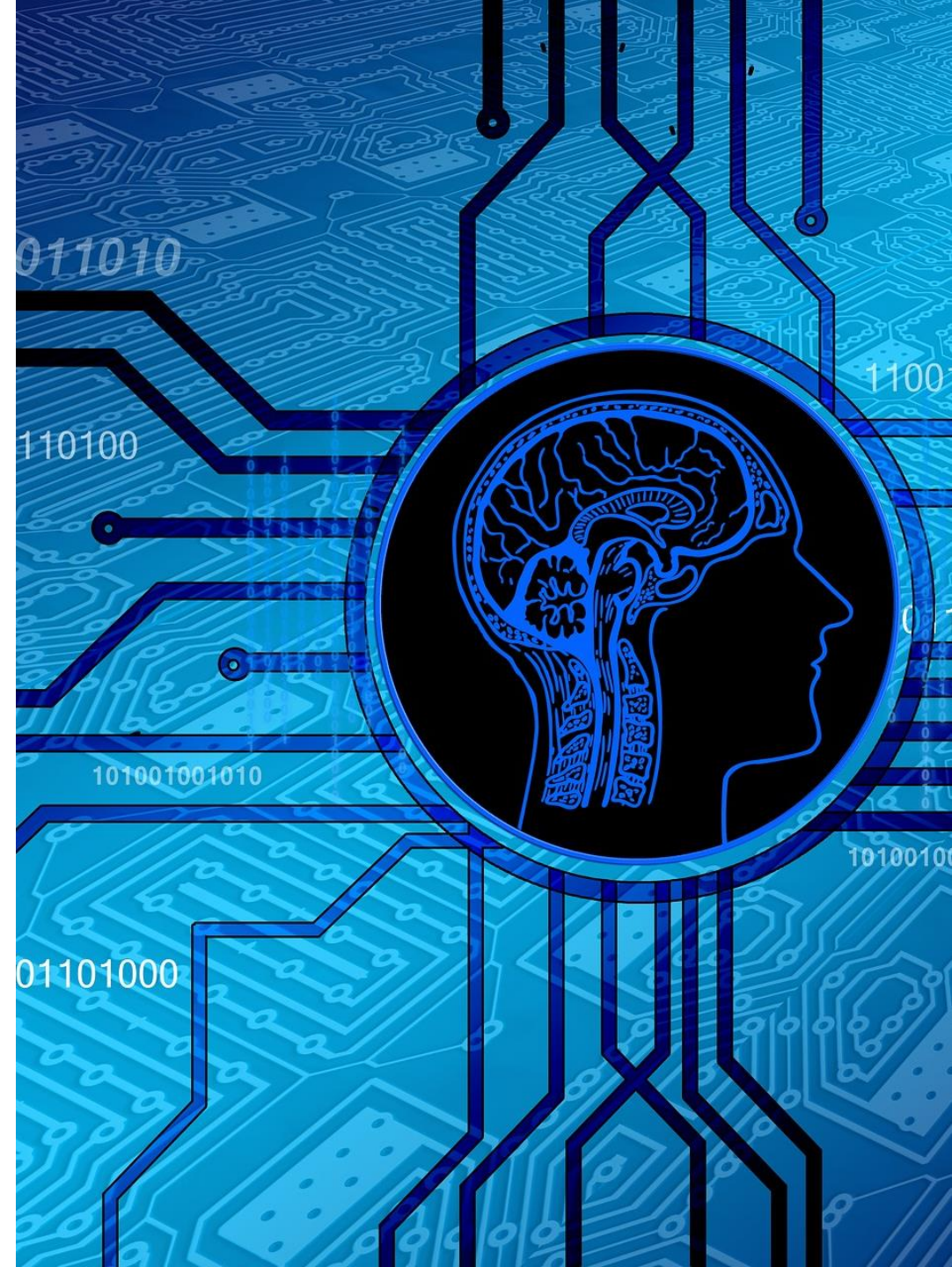


# Problem Solving and Search

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Informatics 2D: Reasoning and Agents  
**Lecture 2**

*Adapted from slides provided by Dr Petros Papapanagiotou*



# Problem-solving Agents

---

# Problem-solving agents

**function** SIMPLE-PROBLEM-SOLVING-AGENT(*percept*) **returns** an action

**persistent:** *seq*, an action sequence, initially empty  
*state*, some description of the current world state  
*goal*, a goal, initially null  
*problem*, a problem formulation

*state*  $\leftarrow$  UPDATE-STATE(*state*, *percept*)

**if** *seq* is empty **then do**

*goal*  $\leftarrow$  FORMULATE-GOAL(*state*)

*problem*  $\leftarrow$  FORMULATE-PROBLEM(*state*, *goal*)

*seq*  $\leftarrow$  SEARCH(*problem*)

**if** *seq* = *failure* **then return** a null action

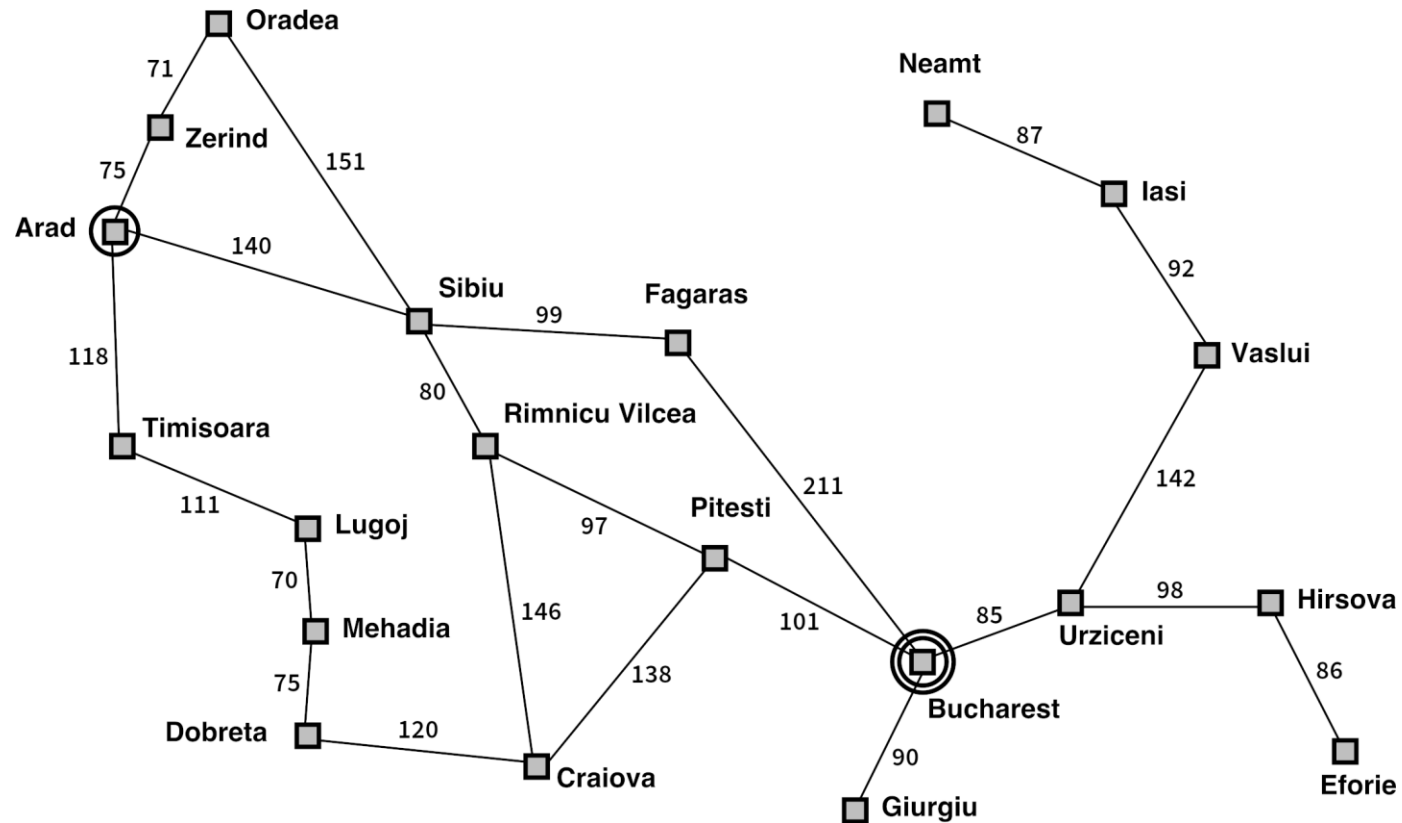
*action*  $\leftarrow$  FIRST(*seq*)

*seq*  $\leftarrow$  REST(*seq*)

**return** *action*

# Example: Romania

---



On holiday in Romania.

Currently in **Arad**.

Flight leaves tomorrow from **Bucharest**.

# Example: Romania

---

On holiday in Romania; currently in **Arad**.

Flight leaves tomorrow from **Bucharest**

Formulate goal:

- be in Bucharest

Formulate problem:

- states: various cities
- actions: drive between cities

Find solution:

- sequence of cities, e.g., Arad, Sibiu, Fagaras, Bucharest

# Problem types

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**Deterministic, fully observable** → single-state problem

- Agent knows exactly which state it will be in; solution is a sequence

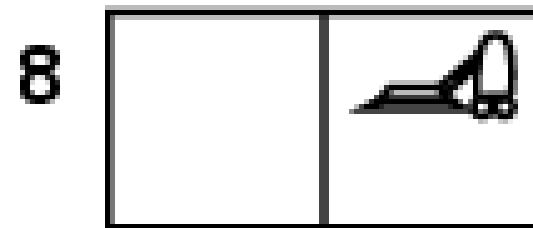
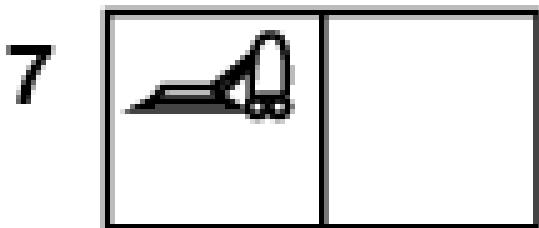
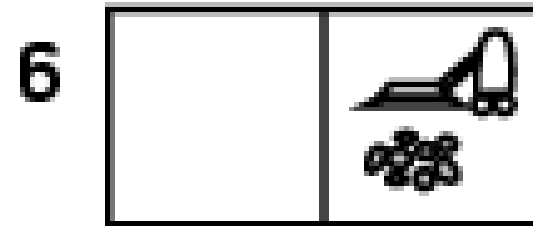
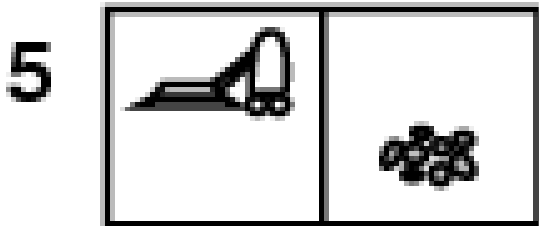
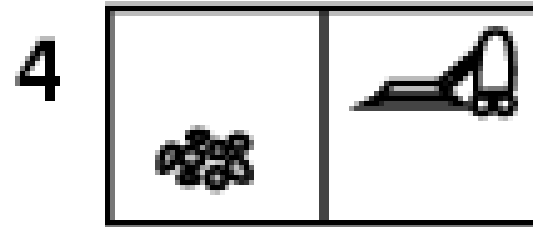
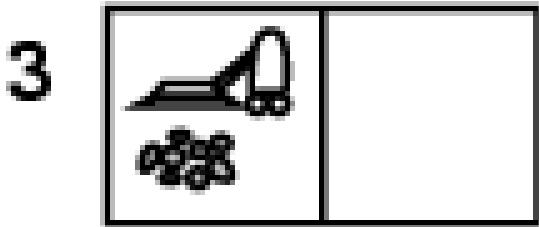
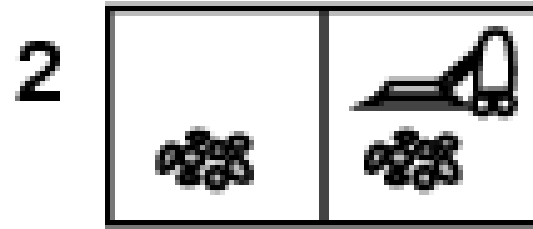
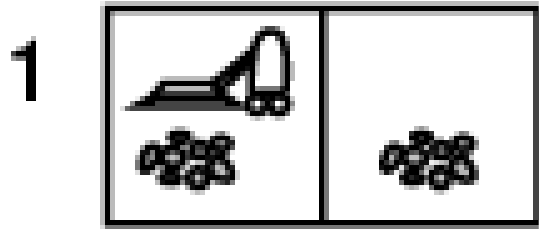
**Non-observable** → sensorless problem (conformant problem)

- Agent may have no idea where it is; solution is a sequence

**Nondeterministic and/or partially observable** → contingency problem

- percepts provide new information about current state
- often interleave search, execution

**Unknown state space** → exploration problem



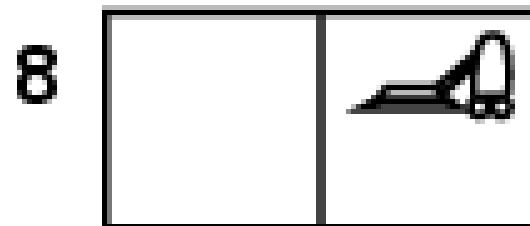
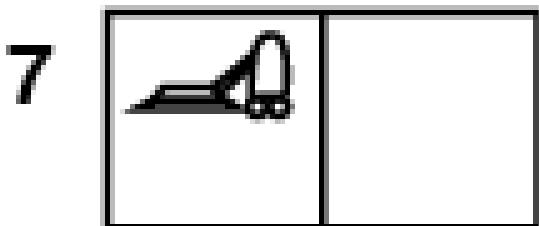
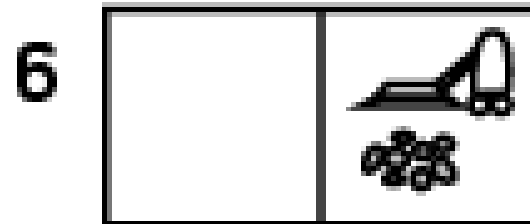
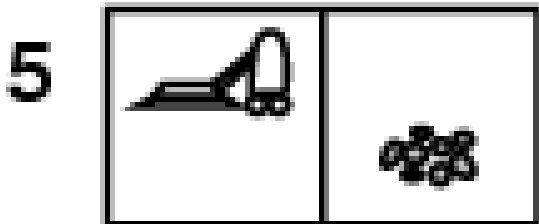
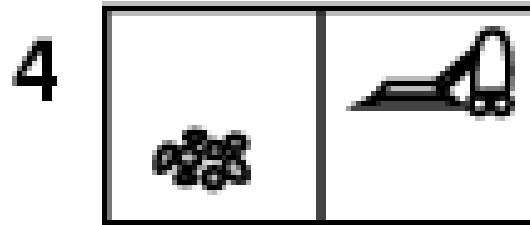
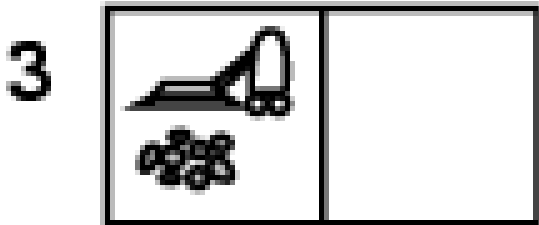
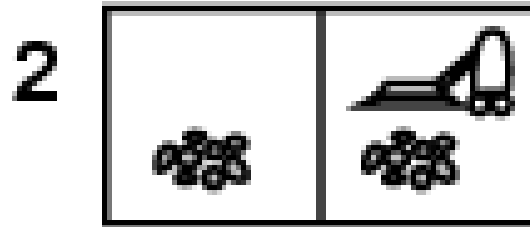
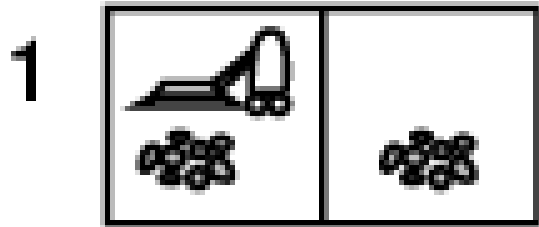
# Example: vacuum world

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Single-state:

Start in 5

Solution?



# Example: vacuum world

---

## Single-state:

Start in 5

Solution?

[*Right, Suck*]

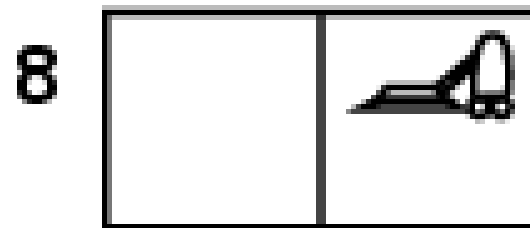
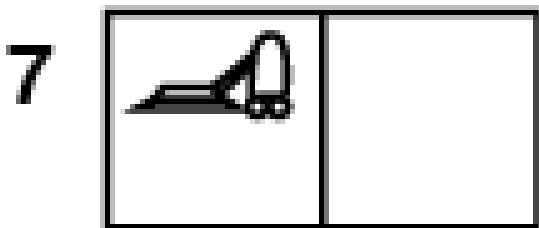
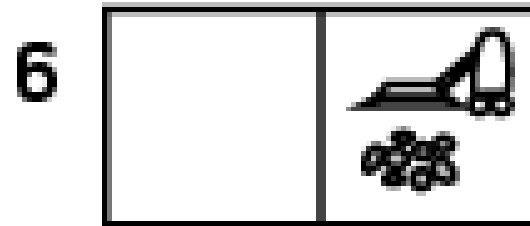
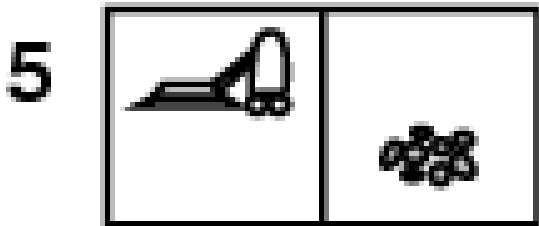
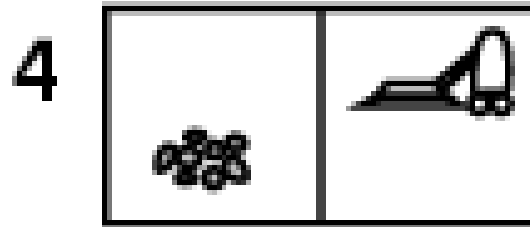
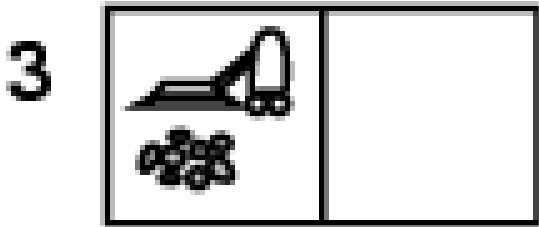
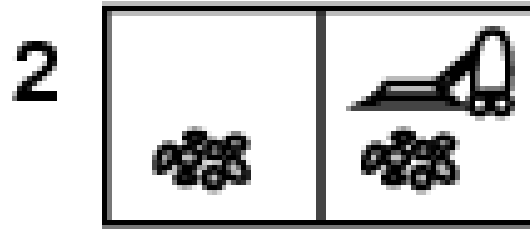
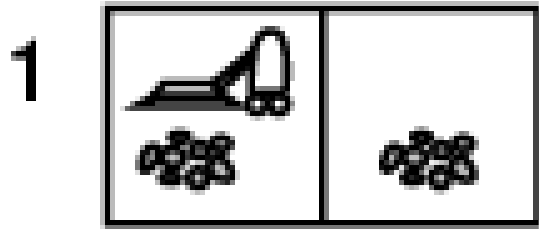
## Sensorless:

Start in {1,2,3,4,5,6,7,8}

e.g. *Right* goes to {2,4,6,8}

Solution?





# Example: vacuum world

---

## Single-state:

Start in 5

Solution?

[*Right, Suck*]

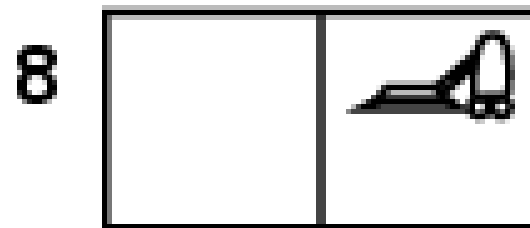
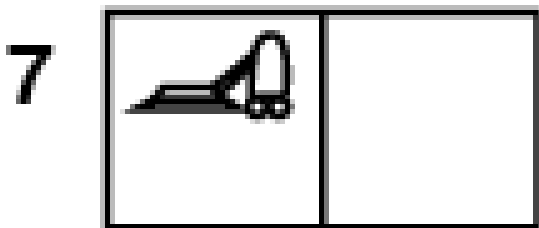
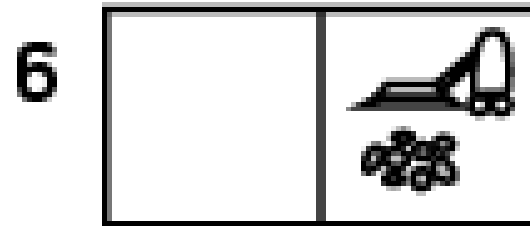
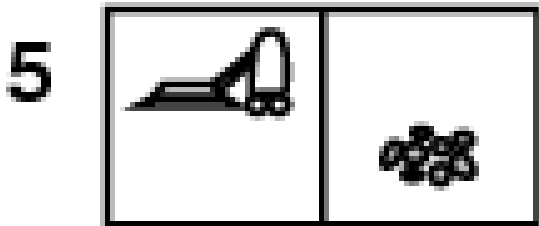
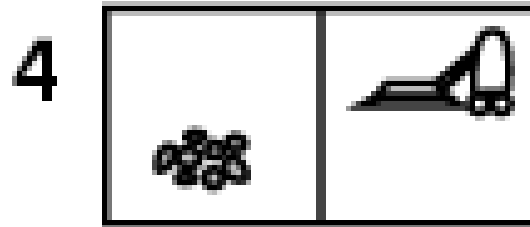
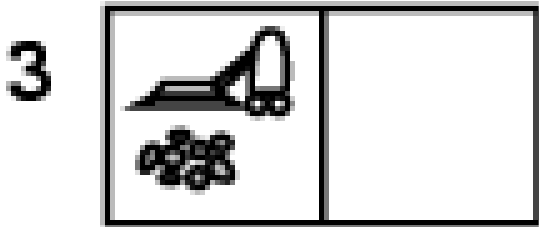
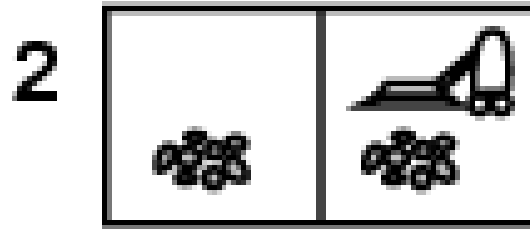
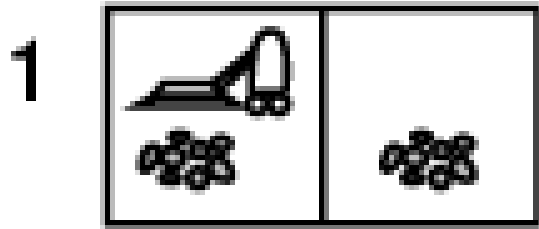
## Sensorless:

Start in {1,2,3,4,5,6,7,8}

e.g. *Right* goes to {2,4,6,8}

Solution?

[*Right, Suck, Left, Suck*]

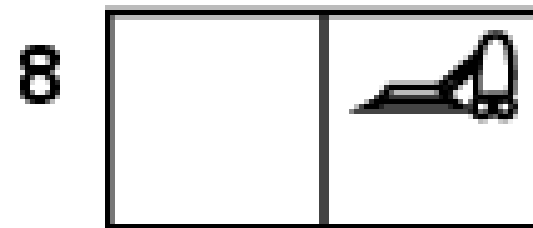
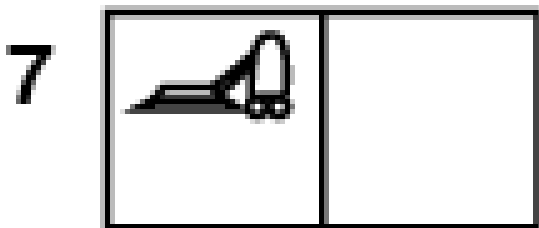
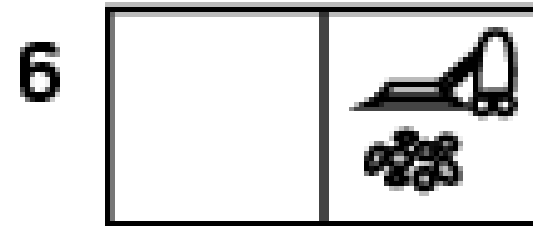
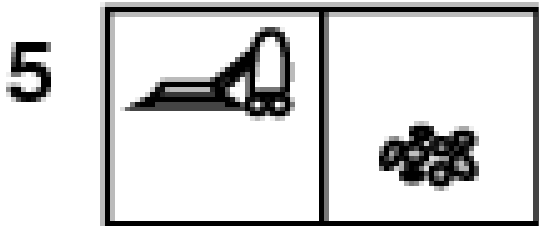
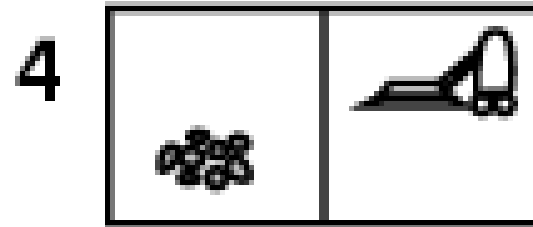
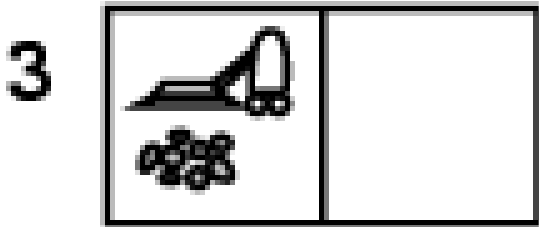
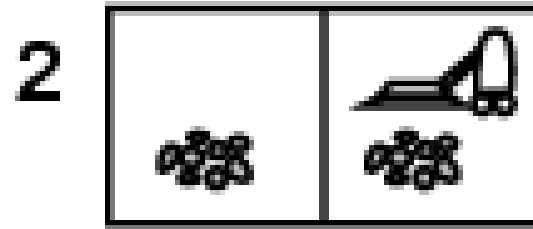
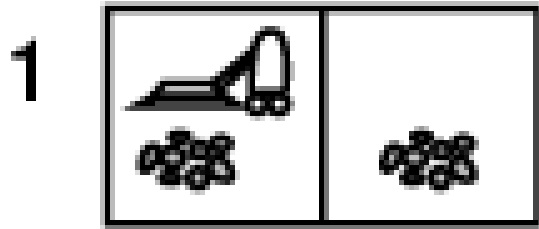


# Example: vacuum world

---

## Contingency:

- Nondeterministic: *Suck* may dirty a clean carpet
  - Partially observable: can only see dirt at current location.
  - Percept: [*Left, Clean*] i.e., start in 5 or 7
- Solution?



# Example: vacuum world

---

## Contingency:

- Nondeterministic: *Suck* may dirty a clean carpet
  - Partially observable: can only see dirt at current location.
  - Percept: [*Left, Clean*] i.e., start in 5 or 7
- Solution?  
[*Right, **if** dirt **then** Suck*]

# Problem Formulation

---

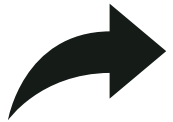
# Single-state problem formulation

---



## Initial State

- e.g. "in Arad"



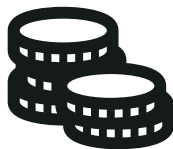
## Actions or Successor function

- $S(x)$  = set of action-state pairs
- e.g.  $S(\text{Arad}) = \{ \langle \text{Arad} \rightarrow \text{Zerind}, \text{Zerind} \rangle, \dots \}$



## Goal test

- explicit      e.g.  $x = \text{"in Bucharest"}$
- implicit      e.g.  $\text{Checkmate}(x)$



## Path cost (additive)

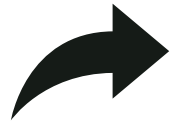
- e.g. sum of distances, number of actions executed, etc.
- $c(x,a,y)$  is the step cost of taking action  $a$  in state  $x$  to reach state  $y$ , assumed to be  $\geq 0$

# Single-state problem formulation



## Initial State

- e.g. "in Arad"



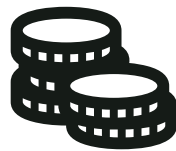
## Actions or Successor function

- A **solution** is a sequence of actions leading from the initial state to a goal
- e.g.  $S(\text{Arad}) = \{ \langle A, \text{state} \rangle \}$ , i.e. a state that succeeds the goal test.



## Goal test

- explicit      e.g.  $x = \text{"in Bucharest"}$
- implicit      e.g.  $\text{Checkmate}(x)$



## Path cost (additive)

- e.g. sum of distances, number of actions executed, etc.
- $c(x, a, y)$  is the step cost of taking action  $a$  in state  $x$  to reach state  $y$ , assumed to be  $\geq 0$

# Selecting a state space

---

Real world is absurdly complex

→ state space must be **abstracted** for problem solving

(Abstract) state = set of real states

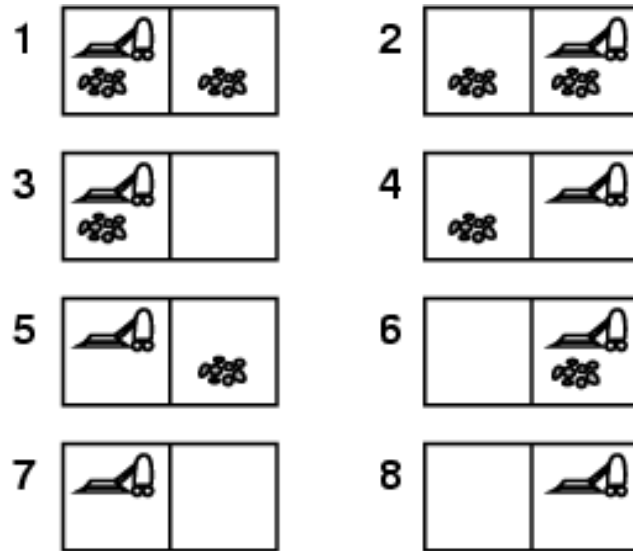
(Abstract) action = complex combination of real actions

- e.g., "Arad → Zerind" represents a complex set of possible routes, detours, rest stops, etc.
- For guaranteed realizability, **any** real state "in Arad" must get to some real state "in Zerind"

(Abstract) solution = *set of real paths that are solutions in the real world*

*Each abstract action should be "easier" than the original problem.*

# Example: Vacuum world



States



Actions



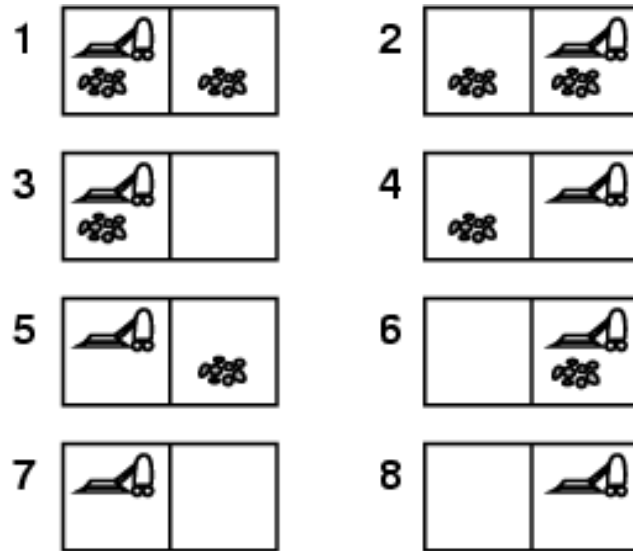
Goal test



Path cost (additive)



# Example: Vacuum world



## States

- Pair of dirt and robot locations



## Actions

- *Left, Right, Suck*



## Goal test

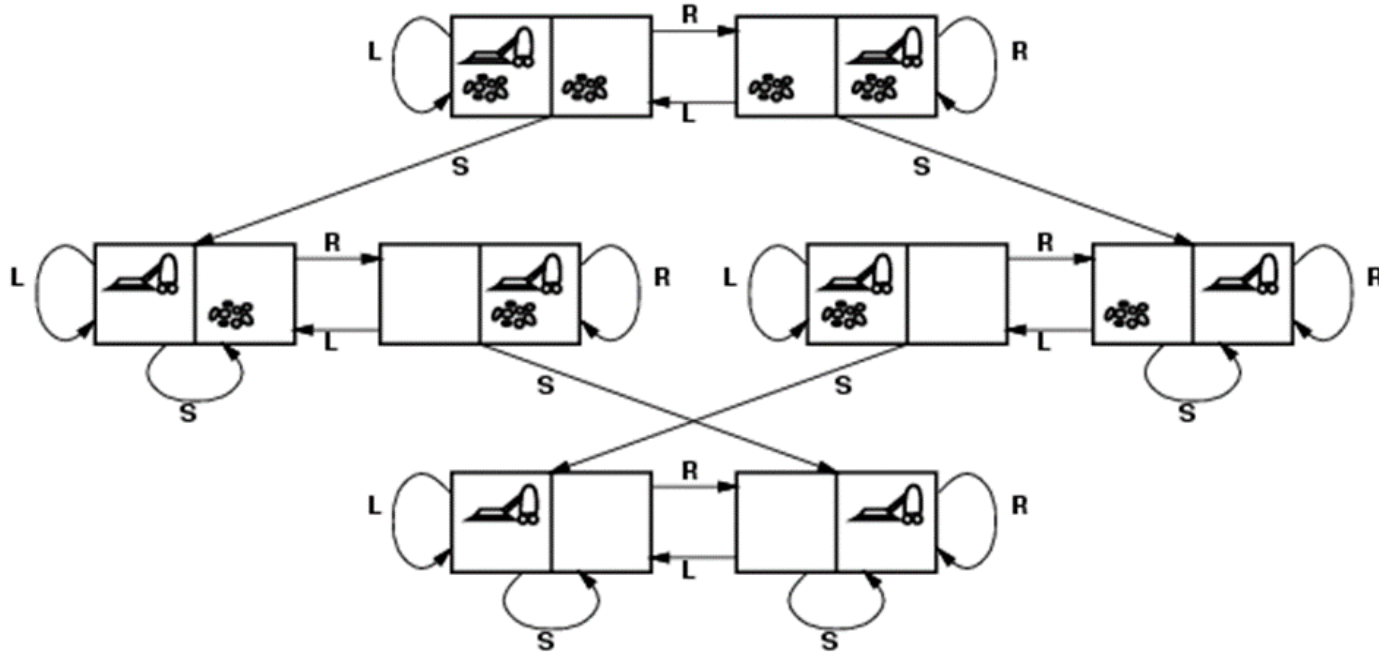
- No dirt at any location



## Path cost (additive)

- 1 per action

# Example: Vacuum world



## States

- Pair of dirt and robot locations

## Actions

- *Left, Right, Suck*

## Goal test

- No dirt at any location

## Path cost (additive)

- 1 per action

# Example: 8-puzzle

---

7	2	4
5		6
8	3	1

Start State

	1	2
3	4	5
6	7	8

Goal State



States



Actions



Goal test



Path cost (additive)

# Example: 8-puzzle

7	2	4
5		6
8	3	1

Start State

	1	2
3	4	5
6	7	8

Goal State



## States

- Integer location of tiles



## Actions

- Move blank *left, right, up, down*



## Goal test

- = Goal state (given)



## Path cost (additive)

- 1 per move

# Example: 8-puzzle

7	2	4
5		6
8	3	1

Start State

	1	2
3	4	5
6	7	8

Goal State

NP-  
Hard



## States

- Integer location of tiles



## Actions

- Move blank *left, right, up, down*



## Goal test

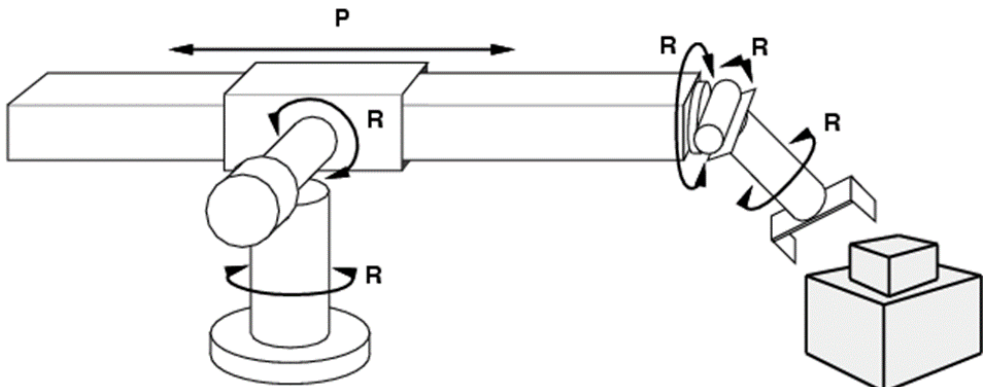
- = Goal state (given)



## Path cost (additive)

- 1 per move

# Example: Robotic assembly



## States

- Real-valued coordinates of robot joint angles
- Parts of the object to be assembled



## Actions

- Continuous motions of robot joints



## Goal test

- = complete assembly



## Path cost (additive)

- Time to execute

# Searching for Solutions

---

# Tree search algorithms

**function** TREE-SEARCH(*problem*) **returns** a solution, or failure

initialize the frontier using the initial state of *problem*

**loop do**

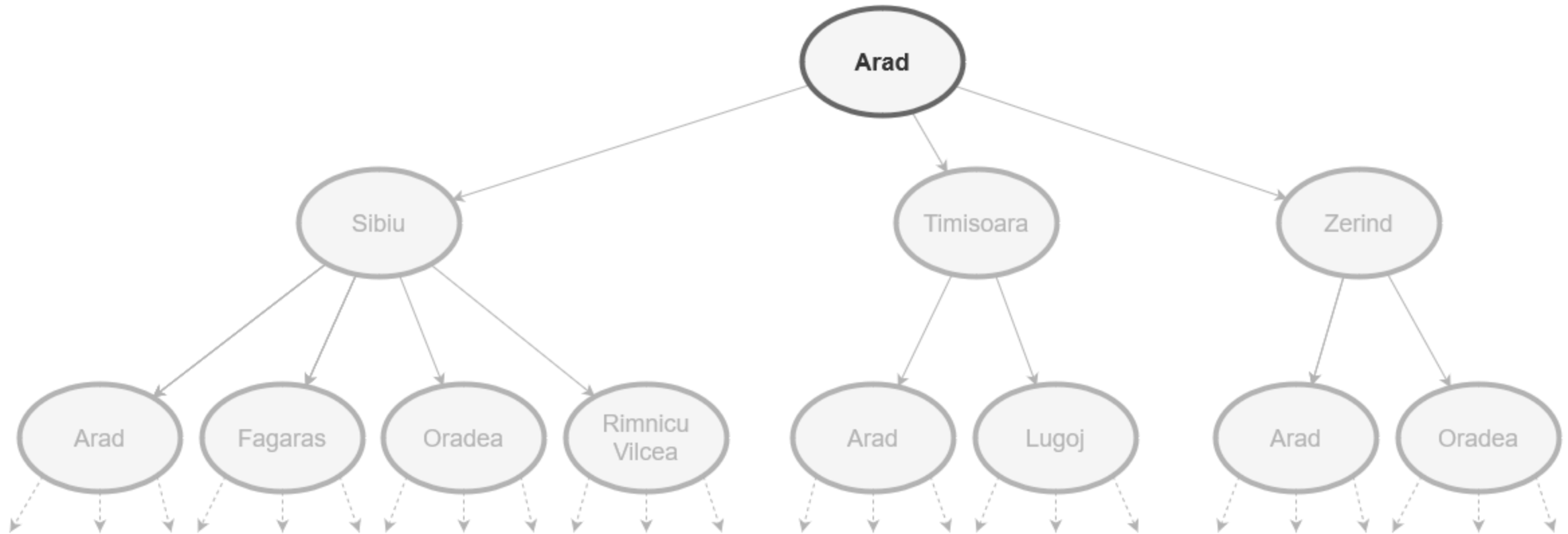
**if** the frontier is empty **then return** failure

    choose a leaf node and remove it from the frontier

**if** the node contains a goal state **then return** the corresponding solution

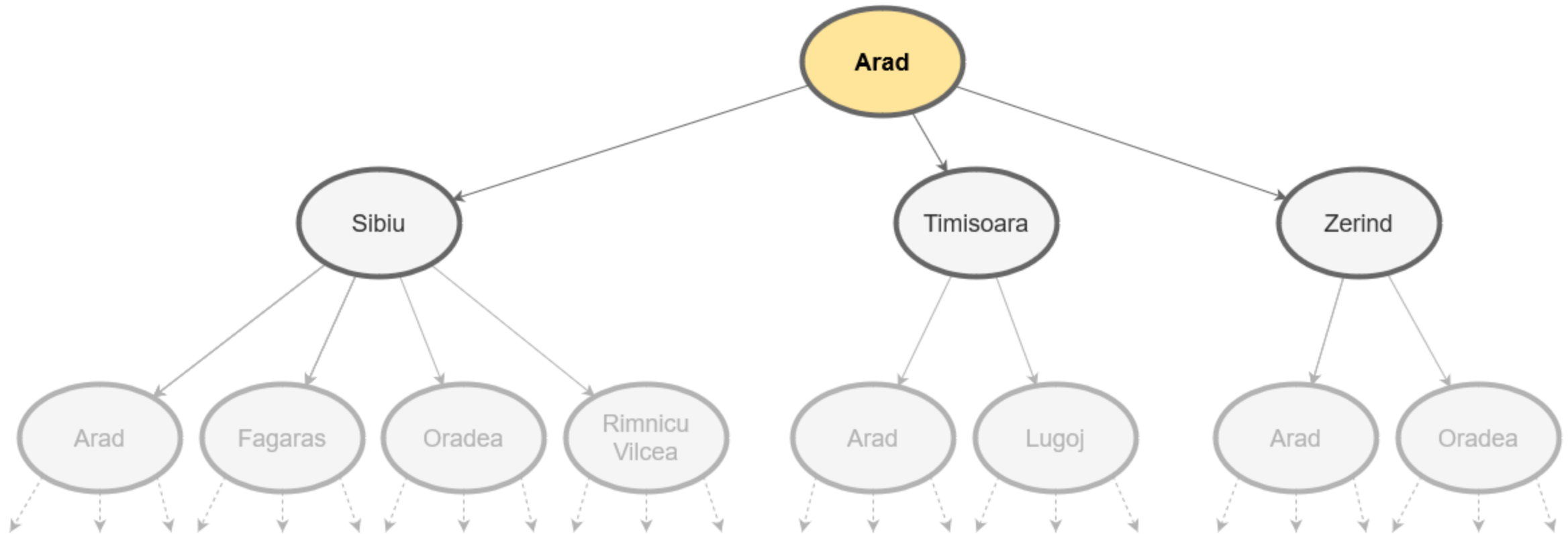
    expand the chosen node, adding the resulting nodes to the frontier





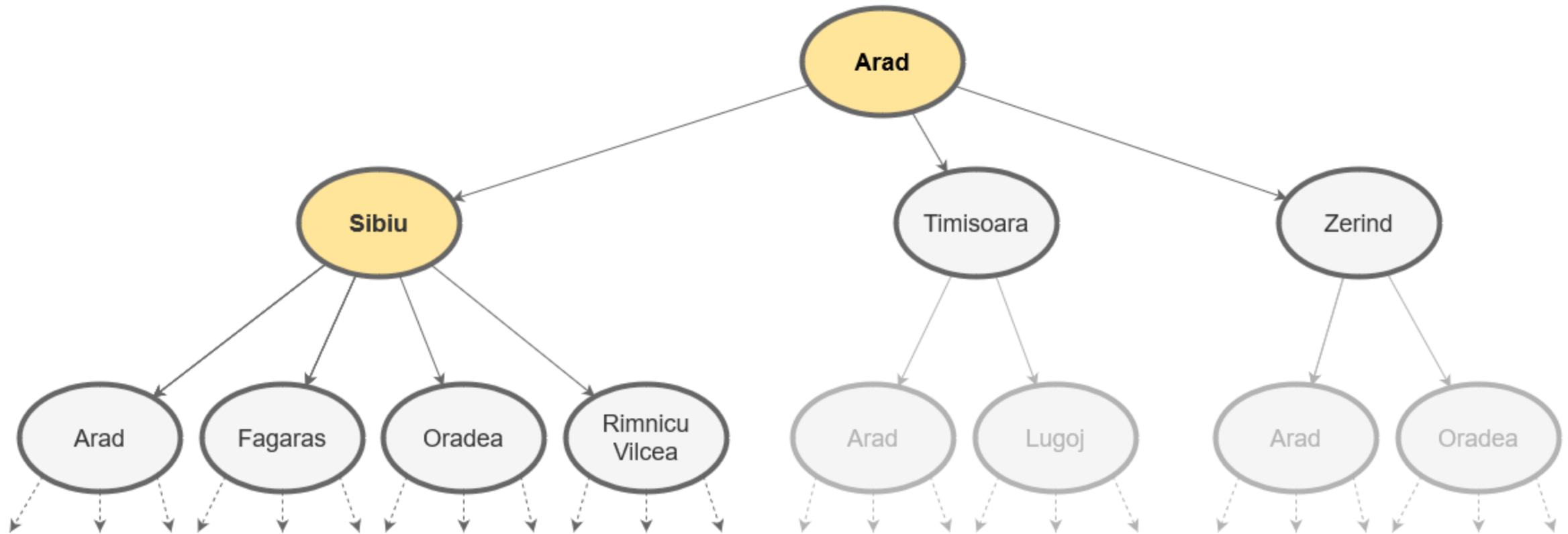
# Tree search example

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# Tree search example

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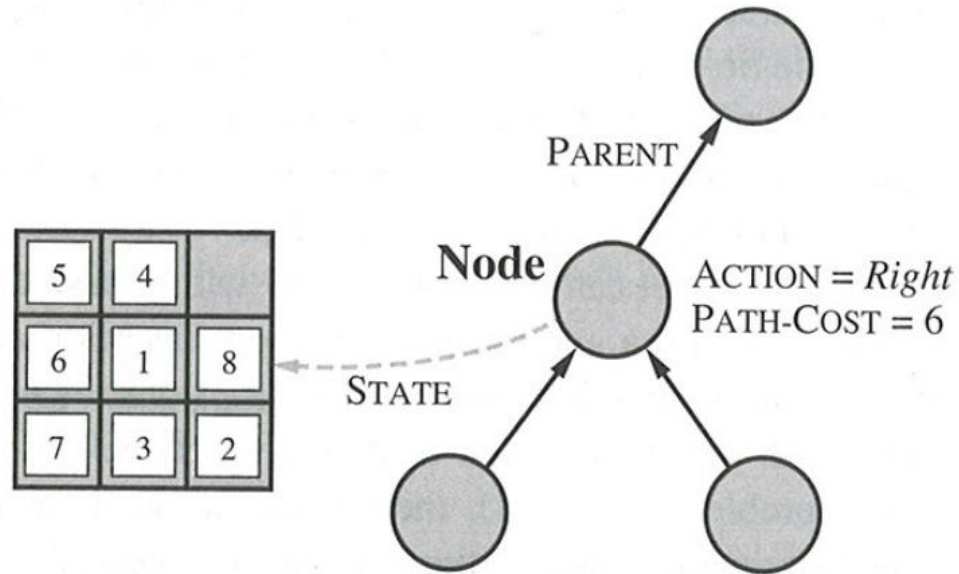


# Tree search example

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# Implementation: states vs. nodes

---



A **state** is a (representation of) a physical configuration

A **node** is a book-keeping data structure constituting part of a **search tree**; includes *state, parent node, action, path cost*

Using these it is easy to compute the components for a child node.  
(The `CHILD-NODE` function)

# Implementation: general tree search

---

```
function TREE-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    expand the chosen node, adding the resulting nodes to the frontier
```

```
function CHILD-NODE(problem, parent, action) returns a node
  return a node with
    STATE = problem.RESULT(parent.STATE, action),
    PARENT = parent, ACTION = action,
    PATH-COST = parent.PATH-COST + problem.STEP-COST(parent.STATE, action)
```

# Summary

---

Problem formulation usually requires abstracting away real-world details to define a state space that can feasibly be explored.

# Why?

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- Formulating problems in a way that a computer can understand.
- Breaking down the problem and its parameters.
- Clarifying the possible actions and assumptions about them.
- Creating structures where we can methodically and systematically search for solutions.