

# Informatics 2D: Reasoning and Agents

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Lecture 18b: Planning and acting in the real world:  
beliefs and sensorless planning

# Where are we?

Last time...

- We have impractical assumptions about planning
  - actions have deterministic outcomes
  - states are fully observable

that we now need to drop.

- General discussion of challenges and planning strategies to deal with more realistic planning problems.

Now: More formal detail.

# What's needed?

## When sensors aren't powerful enough

- Don't know the value of all relevant fluents
- So you must plan using your **beliefs**, not the representation of the actual state.
- How do we represent beliefs?

## When actions can have more than one outcome

- Need to represent **conditional effects** in action schemata.

# What's needed?

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# How to represent belief states

1. Sets of state representations, e.g.

$$\{(AtL \wedge CleanR \wedge CleanL), (AtL \wedge CleanL)\}$$

( $2^n$  states!)

2. Logical sentences can capture a belief state, e.g.  $AtL \wedge CleanL$  shows ignorance about  $CleanR$  by not mentioning it!
  - This often offers a more compact representation, but
  - Many equivalent sentences; need **canonical** representation to avoid general theorem proving; E.g:
    - All representations are ordered conjunctions of literals (under open-world assumption)
    - But this doesn't capture everything (e.g.  $AtL \vee CleanR$ )
3. Knowledge propositions, e.g.  $K(AtR) \wedge K(CleanR)$  (closed-world assumption)
  - Will use second method, but clearly loss of expressiveness

# Beliefs and Sensorless Planning

- When you have no sensors, you need:
  - to represent and track your (changing) **beliefs** as you perform actions ...
  - ... and so cope with **sensorless planning**

## Example

Table and chair, two cans of paint

*you know these objects exist, but you can't see them*

You can open cans, and paint furniture

Goal: table and chair to be same colour

## Sensorless Planning Example: The Belief States

- There are no *InView* fluents, because there are no sensors!
- There are unchanging facts:  
 $Object(Table) \wedge Object(Chair) \wedge Can(C_1) \wedge Can(C_2)$
- And we know that the objects and cans have colours:  
 $\forall x \exists c Color(x, c)$
- After skolemisation this gives an initial belief state:

$$b_0 = Color(x, C(x))$$

- A **belief state** corresponds exactly to the set of possible worlds that satisfy the formula—**open world assumption**.

# The Plan

$[RemoveLid(C_1), Paint(Chair, C_1), Paint(Table, C_1)]$

Rules:

- You can only apply actions whose preconditions are satisfied by your current belief state  $b$ .
- The **update of a belief state  $b$  given an action  $a$**  is the set of all states that result (in the physical transition model) from doing  $a$  in each possible state  $s$  that satisfies belief state  $b$ :

$$b' = \text{Result}(b, a) = \{s' : s' = \text{Result}_P(s, a) \wedge s \in b\}$$

Or, when a belief  $b$  is expressed as a formula:

- 1 If action adds  $l$ ,  $l$  becomes a conjunct of the formula  $b'$  (and the conjunct  $\neg l$  removed, if necessary); so  $b' \models l$
- 2 If action deletes  $l$ ,  $\neg l$  becomes a conjunct of  $b'$  (and  $l$  removed).
- 3 If action says nothing about  $l$ , it retains its  $b$ -value.



## Showing the Plan Works

$$\begin{aligned} b_0 &= \text{Color}(x, C(x)) \\ b_1 &= \text{Result}(b_0, \text{RemoveLid}(C_1)) \\ &= \text{Color}(x, C(x)) \wedge \text{Open}(C_1) \\ b_2 &= \text{Result}(b_1, \text{Paint}(\text{Chair}, C_1)) \\ &\quad (\text{binding } \{x/C_1, c/C(C_1)\} \text{ satisfies Precond}) \\ &= \text{Color}(x, C(x)) \wedge \text{Open}(C_1) \wedge \text{Color}(\text{Chair}, C(C_1)) \\ b_3 &= \text{Result}(b_2, \text{Paint}(\text{Table}, C_1)) \\ &= \text{Color}(x, C(x)) \wedge \text{Open}(C_1) \wedge \\ &\quad \text{Color}(\text{Chair}, C(C_1)) \wedge \text{Color}(\text{Table}, C(C_1)) \end{aligned}$$

# Summary

- When your sensors aren't powerful enough to fully observe the current state, you need to reason about your beliefs
- Various ways of representing beliefs
- Examined how you can keep track of beliefs as you act, and so cope with sensorless planning.