



- 250 word abstract
- Deadline Feb 6th
- Women and non-binary students
- Best poster awards (for each year and for MSc)

The 19th annual BCSWomen Lovelace Colloquium will be held on Wednesday 8th and Thursday 9th April 2026, in-person, hosted by University of Bath.



Submission Form



Example Abstracts

Introduction to Quantum Programming and Semantics

Lecture 7: Copying and deleting

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Overview

- Copying and deleting
- No-cloning and no-deleting
- Products
- Categories

Copying and deleting

Copying machines

$$\begin{array}{ccc} A & \xrightarrow{d} & A \otimes A \\ A & \xrightarrow{e} & \mathbb{C}^{\otimes} = \mathbb{C} \end{array}$$

- commutative:

$$\begin{array}{c} - \boxed{d} \times = - \boxed{d} \\ \triangleleft \boxed{d} \times = \triangleleft \times = \triangleleft \triangleleft = \triangleleft \boxed{d} \end{array} \quad \left. \begin{array}{c} \\ \\ \end{array} \right\}$$

$$\Rightarrow \forall: \triangleleft \boxed{d} \triangleleft = \triangleleft$$

- associative:

$$- \boxed{d} \boxed{d} = - \boxed{d} \boxed{d}$$

$$\Downarrow \quad \begin{array}{c} \\ \end{array} = - \boxed{d} = \begin{array}{c} \\ \end{array}$$

- unital:

$$- \boxed{d} \xrightarrow{e} = \begin{array}{c} \\ \end{array}$$

$$\begin{array}{c} \boxed{d} \\ \curvearrowleft \end{array} ?$$

Such a process we'll call a "copying machine", or "comonoid",

$$\text{e.g. } A = \mathbb{C}$$

$$d |i\rangle = |ii\rangle = |i\rangle \otimes |i\rangle$$

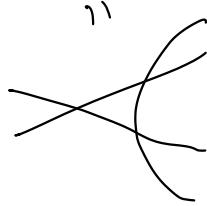
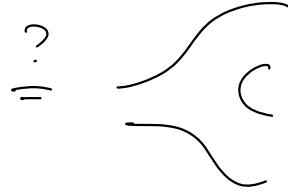
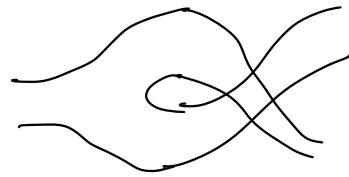
$$d = \begin{pmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 1 \end{pmatrix}$$

$$e |i\rangle = 1$$

$$e = \begin{pmatrix} 1 & 1 \end{pmatrix}$$

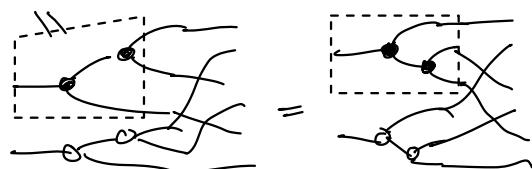
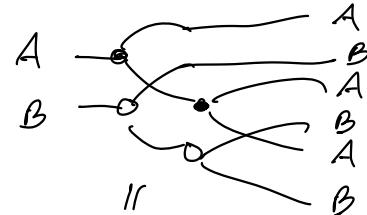
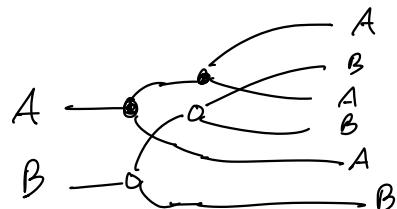
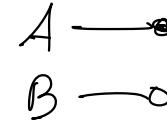
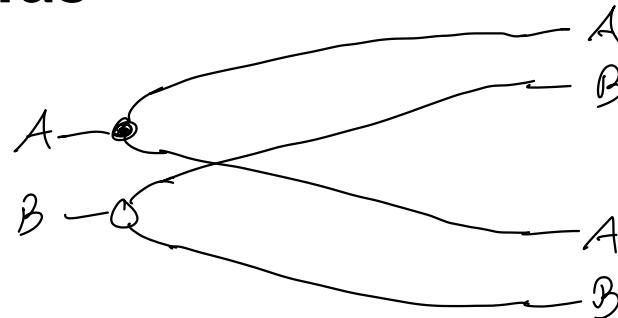
and we'll draw it as

$$d = \begin{array}{c} \boxed{d} \\ \curvearrowleft \end{array} \quad e = \begin{array}{c} \begin{array}{c} \\ \end{array} \end{array}$$



To distinguish different copying machines, we'll colour their pictures differently.

Combining comonoids



Monoids

$$\begin{array}{c} A \\ \circ \\ A \end{array}$$

$$\circ \longrightarrow A$$

s.t -

associative:

$$\begin{array}{c} \circ \\ \circ \\ \circ \end{array} = \begin{array}{c} \circ \\ \circ \\ \circ \end{array}$$

$$(m+n)+p = m+(n+p)$$

unital:

$$\begin{array}{c} \circ \\ \circ \end{array} = \begin{array}{c} \circ \\ \circ \end{array} = \begin{array}{c} \circ \\ \circ \end{array}$$

$$0+m = m = m+0$$

(commutative:

$$\begin{array}{c} \circ \\ \circ \end{array} = \begin{array}{c} \circ \\ \circ \end{array}$$

$$n+m = m+n$$

e.g. $A = \mathbb{Z}$

$$\begin{array}{c} m \\ \circ \\ n \end{array} = m+n \longrightarrow$$

$$\circ = 0 \longrightarrow$$

or

$A = M_n = \{n\text{-by-}n \text{ complex matrices}\}$

$\circ = \text{matrix multiplication}$

$$\circ = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

Pairs of pants

e.g. $A = \{n \times n \text{ matrices}\}$

$\approx \{f: \mathbb{C}^n \rightarrow \mathbb{C}^n \text{ linear}\}$

$\approx (\mathbb{C}^n)^* \otimes \mathbb{C}^n \ni x$

$$x = \sum_{ij} x_{ij} \langle j | \otimes | i \rangle$$

where $A = \begin{smallmatrix} \mathbb{C}^n & - \\ & \mathbb{C}^n - \end{smallmatrix}$

$$A \circ A = \begin{smallmatrix} \mathbb{C}^n & - \\ & \mathbb{C}^n - \\ \mathbb{C}^n & - \\ & \mathbb{C}^n - \end{smallmatrix}$$

$$0 \circ A = \begin{smallmatrix} \mathbb{C}^n & - \\ & \mathbb{C}^n - \end{smallmatrix}$$

$$\begin{smallmatrix} \mathbb{C}^n & - \\ & f \\ \mathbb{C}^n & - \end{smallmatrix}$$

unital : $\begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \end{smallmatrix}$

$$\begin{smallmatrix} \circ & - \\ & f \\ \circ & - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \\ \circ & - \\ & f \\ \circ & - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \\ \circ & - \\ & g \\ \circ & - \\ & \mathbb{C}^n - \end{smallmatrix} = \begin{smallmatrix} \circ & - \\ & \mathbb{C}^n - \\ \circ & - \\ & h \\ \circ & - \end{smallmatrix}$$

No-cloning and no-deleting

Uniform deleting

Systematic deleting: for each type A , have \xrightarrow{A}
s.t. for any process f : $A \xrightarrow{\circ} = A \xrightarrow{[A]} \xrightarrow{B}$

and: $A \otimes B \xrightarrow{\circ} = \begin{matrix} A \xrightarrow{\circ} \\ B \xrightarrow{\circ} \end{matrix}$

No-deleting theorem: if systematic deleting
and caps and caps ("entanglement") are available,
then there is a unique process $A \xrightarrow{[]}$.

hence: unique scalar $\circ \cdots \boxed{s} \cdots \circ$, so no quantities

Uniform copying

No-cloning theorem

Products

Universal property

Characterising products

Categories

Composition

Summary:

- Comonoids are copying machines
- No-cloning theorem holds syntactically
- Can recognise when semantics is classical via products
- Can interpret string diagrams generally in monoidal categories