



The Chartered Institute for IT  
**BCSWomen Lovelace Colloquium**

*The national conference for undergraduate and MSc women in computing*

- 250 word abstract
- Deadline Feb 6<sup>th</sup>
- Women and non-binary students
- Best poster awards (for each year and for MSc)

The 19th annual BCSWomen Lovelace Colloquium will be held on Wednesday 8th and Thursday 9th April 2026, in-person, hosted by University of Bath.



Submission Form



Example Abstracts

# Introduction to Quantum Programming and Semantics

## Lecture 7: Copying and deleting

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# Overview

- Copying and deleting
- No-cloning and no-deleting
- Products
- Categories

**Copying and deleting**

# Copying machines

$$A \xrightarrow{d} A \otimes A$$

$$A \xrightarrow{e} \mathbb{C}^0 = \mathbb{C}$$

- commutative:  $\left. \begin{array}{l} -[d] \text{ with crossing} = -[d] \\ \triangleleft [d] \text{ with crossing} = \triangleleft \text{ with crossing} = \triangleleft = \triangleleft [d] \end{array} \right\}$
- associative:  $\left. \begin{array}{l} -[d][d] = -[d][d] \end{array} \right\}$
- unital:  $-[d] \xrightarrow{e} = \text{line}$

$$\Rightarrow \forall \psi: \triangleleft \psi \text{ with } [d] = \triangleleft \psi$$

$$\Rightarrow \text{loop with } [d] = -[d] = \text{loop with } [d]$$

$$\text{loop with } [d] \text{ ?}$$

Such a process we'll call a "copying machine", or "comonoid",

e.g.  $A = \mathbb{C}^n$

$$d|i\rangle = |ii\rangle = |i\rangle \otimes |i\rangle$$

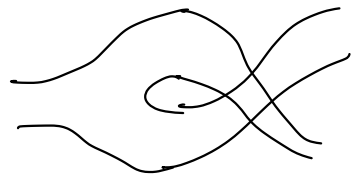
$$e|i\rangle = 1$$

$$d = \begin{pmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 1 \end{pmatrix}$$

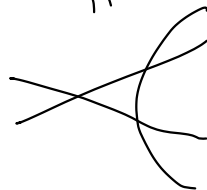
$$e = (1, 1)$$

and we'll draw it as

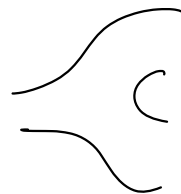
$$d = \text{diagonal line} \quad e = \text{horizontal line}$$



11

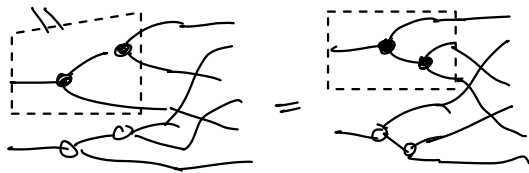
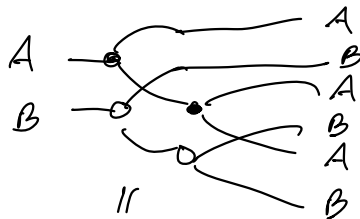
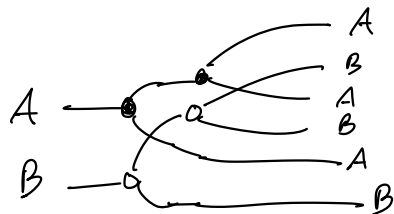
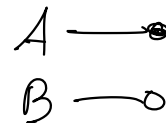
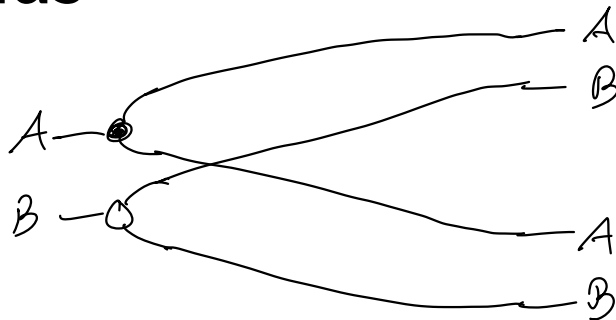
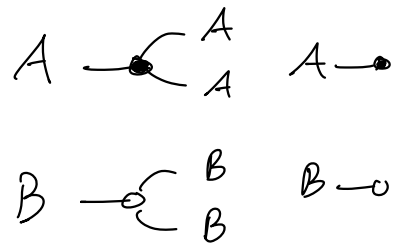


12

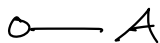
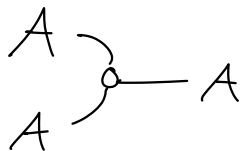


To distinguish different copying machines, we'll colour their pictures differently.

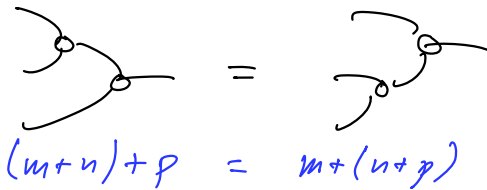
## Combining comonoids



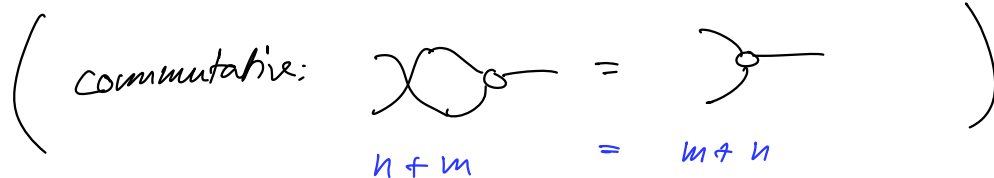
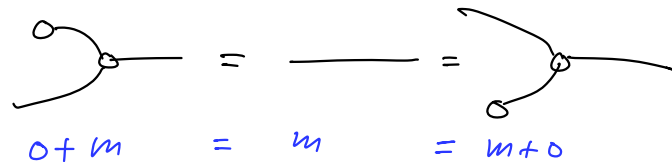
# Monoids



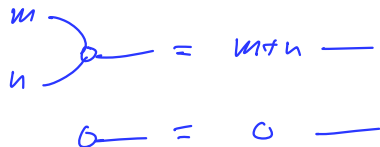
s.t. associative:



unital:

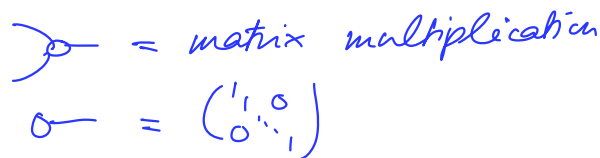


e.g.  $A = \mathbb{Z}$



or

$A = M_n = \{n\text{-by-}n \text{ complex matrices}\}$





# Pairs of pants

e.g.  $A = \{n \times n \text{ matrices}\}$

$$\cong \{f: \mathbb{C}^n \rightarrow \mathbb{C}^n \text{ linear}\}$$

$$\cong (\mathbb{C}^n)^* \otimes \mathbb{C}^n \ni x$$

$$x = \sum_{ij} x_{ij} |j\rangle \otimes |i\rangle$$

where  $A - = \begin{array}{c} \mathbb{C}^n - \\ \mathbb{C}^n - \end{array}$

$$\begin{array}{c} A \\ A \end{array} \circlearrowleft A = \begin{array}{c} \mathbb{C}^n \\ \mathbb{C}^n \\ \mathbb{C}^n \\ \mathbb{C}^n \end{array} \rightarrow \begin{array}{c} \mathbb{C}^n \\ \mathbb{C}^n \end{array}$$

$$0 - A = \begin{array}{c} \mathbb{C}^n \\ \mathbb{C}^n \end{array}$$

$$\begin{array}{c} \mathbb{C}^n \\ \boxed{f} \\ \mathbb{C}^n \end{array}$$

unital :  $\begin{array}{c} \circ \\ \swarrow \end{array} = \begin{array}{c} \text{S-shape} \end{array} = \begin{array}{c} \text{Z-shape} \end{array} = \begin{array}{c} \searrow \\ \circ \end{array}$

$$\begin{array}{c} \boxed{f} \\ \boxed{0} \end{array} = \begin{array}{c} \boxed{0} \boxed{f} \end{array} = \begin{array}{c} \boxed{0} \boxed{A} \end{array}$$

**No-cloning and no-deleting**

# Uniform deleting

systematic deleting: for each type  $A$ , have  $\overset{A}{\longrightarrow} \circ$

s.t. for any process  $f$ :  $A \longrightarrow \circ = A \longrightarrow \boxed{A} \overset{B}{\longrightarrow} \circ$

and:  $A \otimes B \longrightarrow \circ = \begin{matrix} A \longrightarrow \circ \\ B \longrightarrow \circ \end{matrix}$

no-deleting theorem: if systematic deleting  
and caps and cups ("entanglement") are available,  
then there is a unique process  $A \longrightarrow \square$ .

hence: unique scalar  $\text{tr}[\square] \dots$ , so no quantities

Uniform copying

# No-cloning theorem

**Products**

# Universal property

# Characterising products



# Categories

# Composition

# Summary:

- Comonoids are copying machines
- No-cloning theorem holds syntactically
- Can recognise when semantics is classical via products
- Can interpret string diagrams generally in monoidal categories