



THE UNIVERSITY
of EDINBURGH

Methods for Causal Inference

Lecture 1: Introduction

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School of Informatics
2023-2024

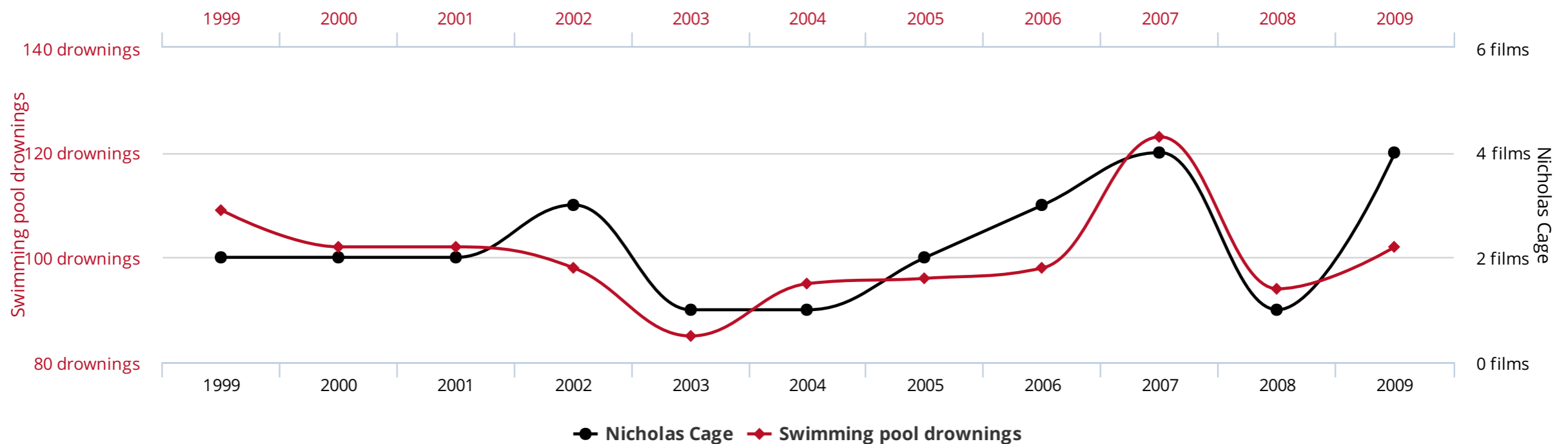
References

- Causal Inference in Statistics: A Primer (Pearl, Glymour, Jewell, 2016)
- What If (Hernán and Robins, 2023)
- Elements of Causal Inference: Foundations and Learning Algorithms (Peters, Janzing and Schölkopf, 2018)
- Causality (Pearl, 2009)
- Many other papers from the literature ... (will be referenced)

“Correlation does not imply causation”

Spurious correlation (random coincidence)

Number of people who drowned by falling into a pool
correlates with
Films Nicolas Cage appeared in

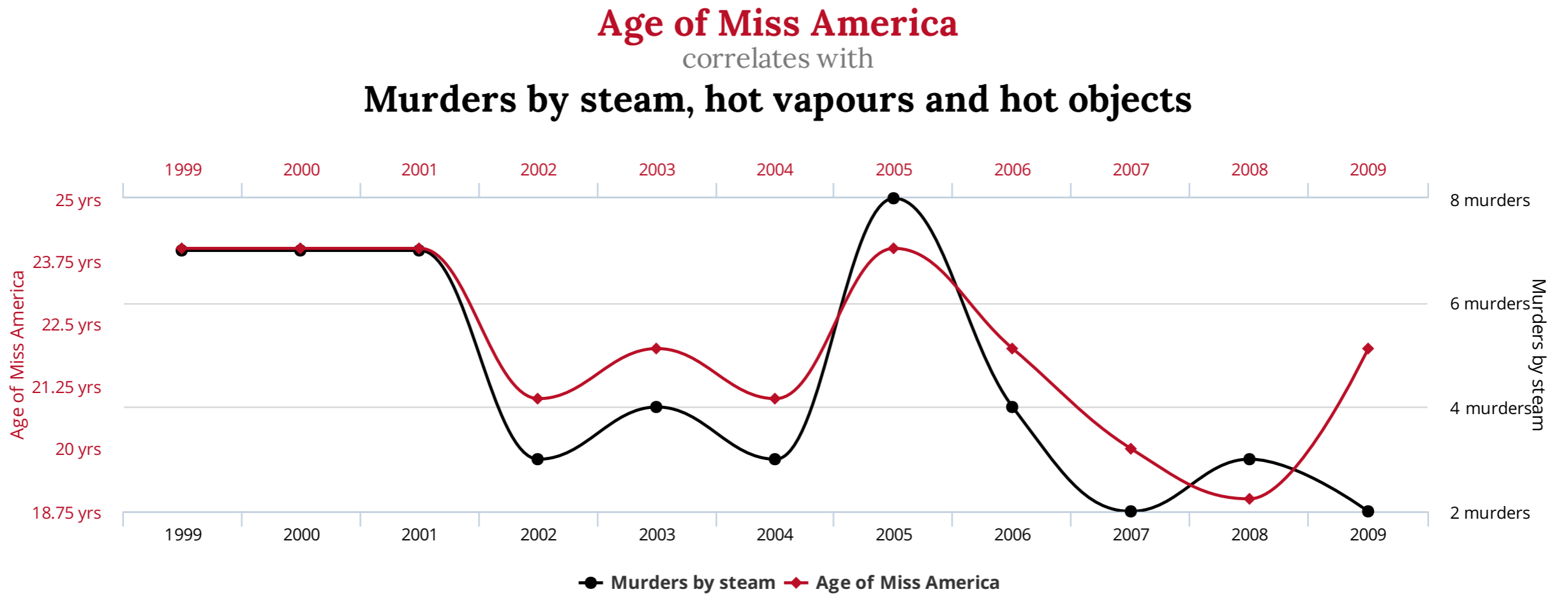


tylervigen.com

Correlation: 66.6% (r=0.666)

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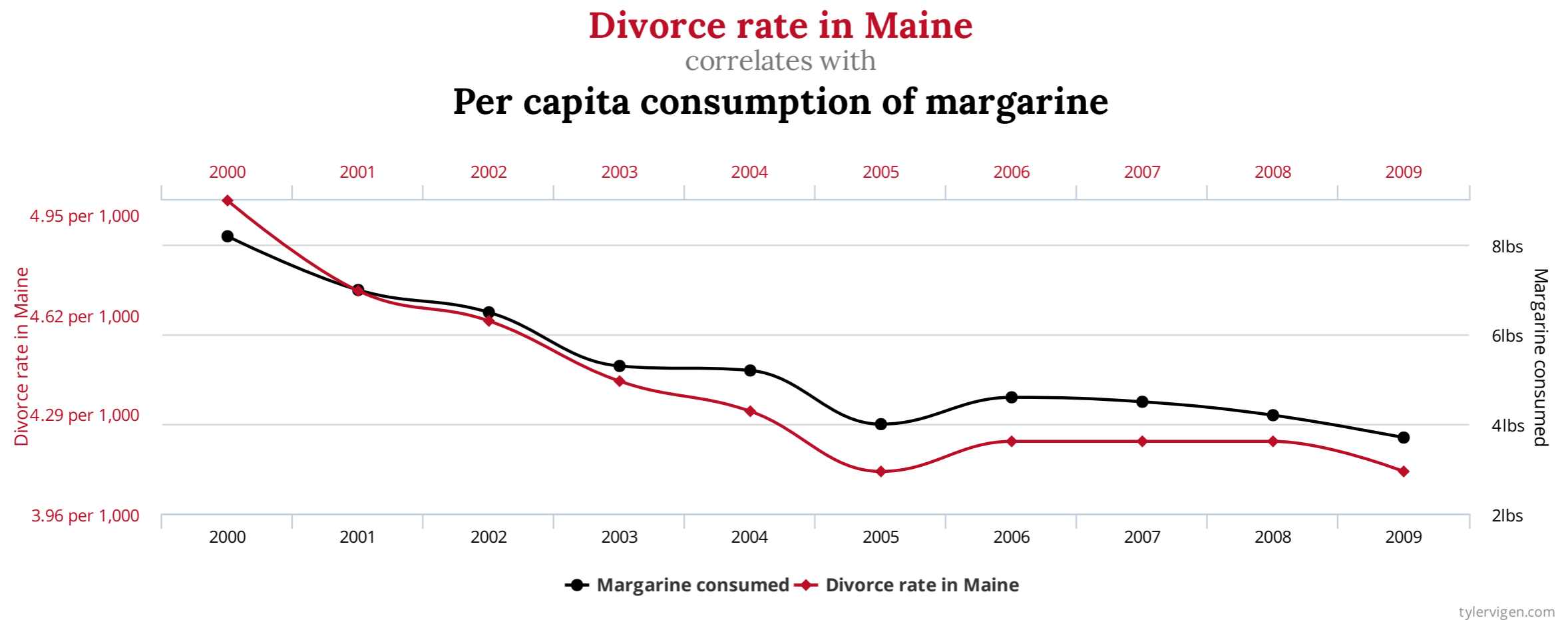


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Correlation: 87.01% (r=0.8701)

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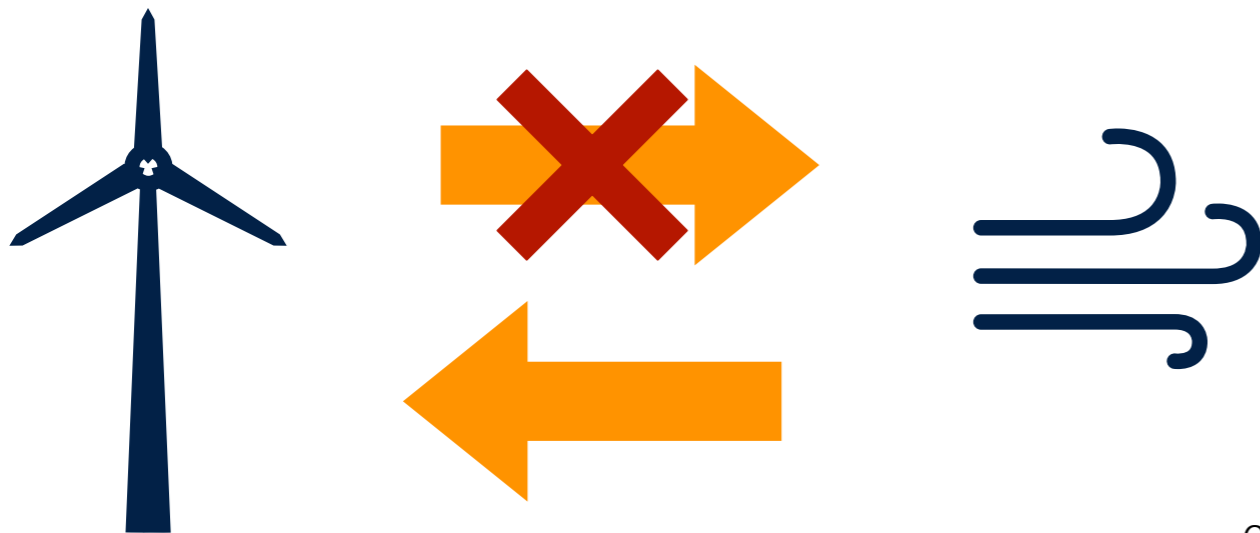


Correlation: 99.26% (r=0.9926)

“Correlation does not imply causation”

Reverse causation:

The faster the wind-turbine rotates, the more wind is observed.
Therefore, rotation of turbines is the cause for winds!



“Correlation does not imply causation”

Circular/bidirectional cause and consequence:

Hours spent on Netflix and weight gain

Scenario 1:

Hours spent on Netflix → Less activity → increase in weight

Scenario 2:

Weight gain → exercising gets harder → more time online as hobby

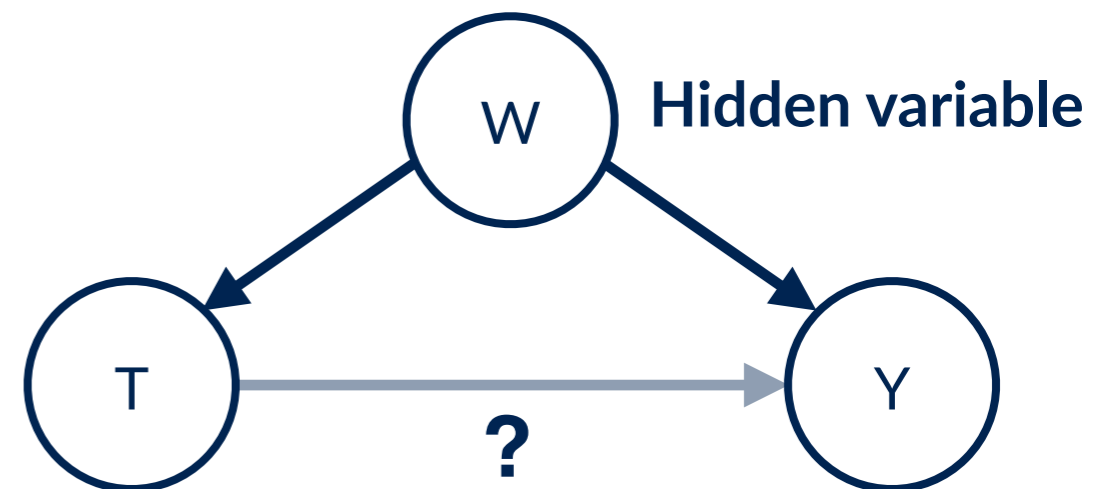


“Correlation does not imply causation”

Confounding factor:

Fever is not a cause of sneezing, they are both symptoms of flu
(no arrow)

Treatment & health outcome relationship confounded by age



Why should we care about causation?

- To guide **actions** and **policies**
- To understand *how* and *why* **interventions** affect outcomes
- **Predict** what would have happened under a different intervention:
“What if I were to act differently?”

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- **Political/Economical:** “increases minimum wage, increases unemployment (people become lazy)”

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Other general examples:

- **Biomedical:** What drug, what dose, when, how often, ... (see later)

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- **Environmental:** Is the constant energy consumption in region X due to the regions's energy efficiency standards or due to its mild climate
- **Education:** People with feature X are more likely to obtain an internship in tech

More examples: Personalised medicine

An individual is diagnosed with a particular disease

Baseline covariants ('features') are measured, e.g., age, sex, BMI, ...

Question: What treatment (A or B) is best for this individual?

What is the causal effect of A or B on the individual's health outcome?

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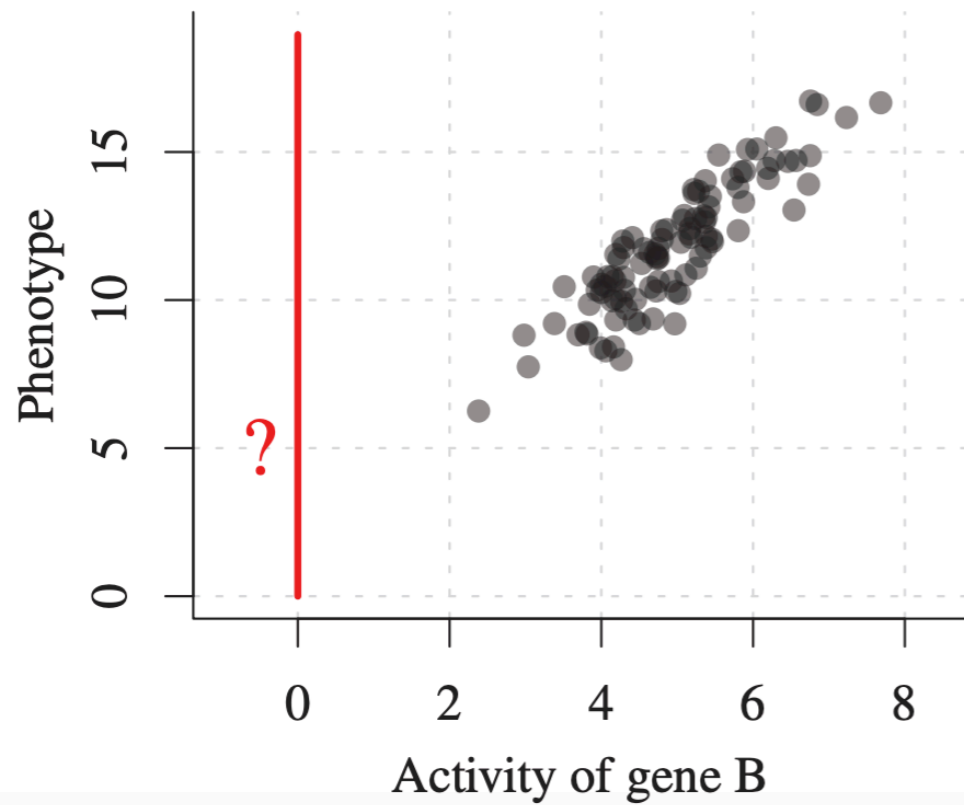
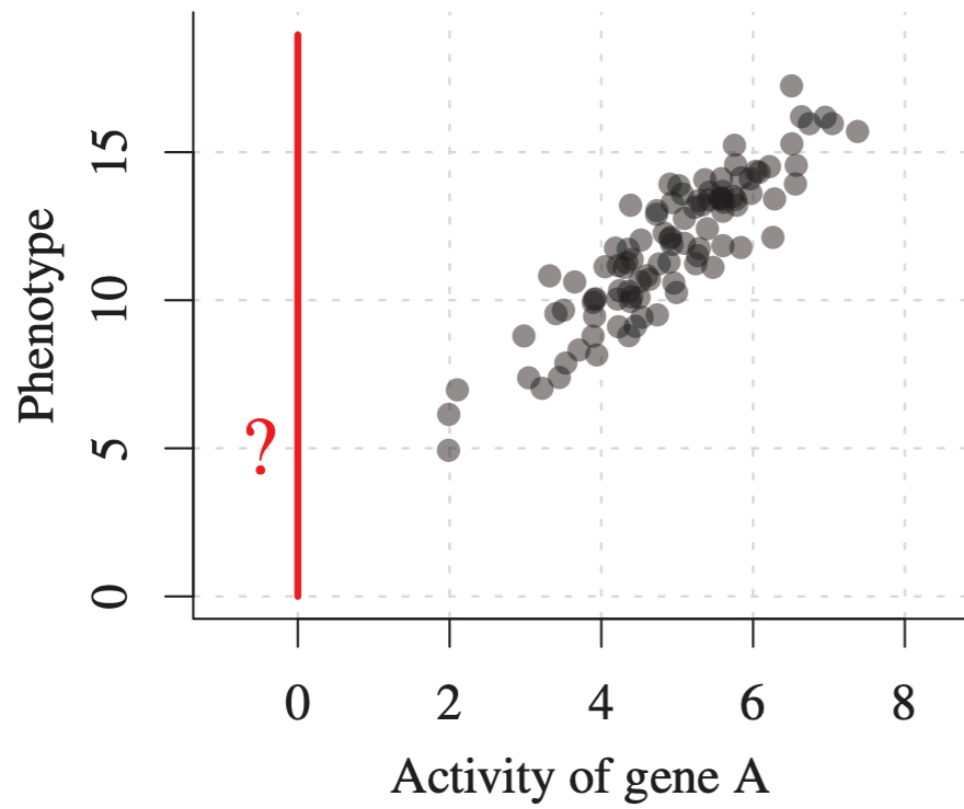
What is the causal effect of A or B on the individual's health outcome?

Ideally: We wish to design a policy that maps individual's:

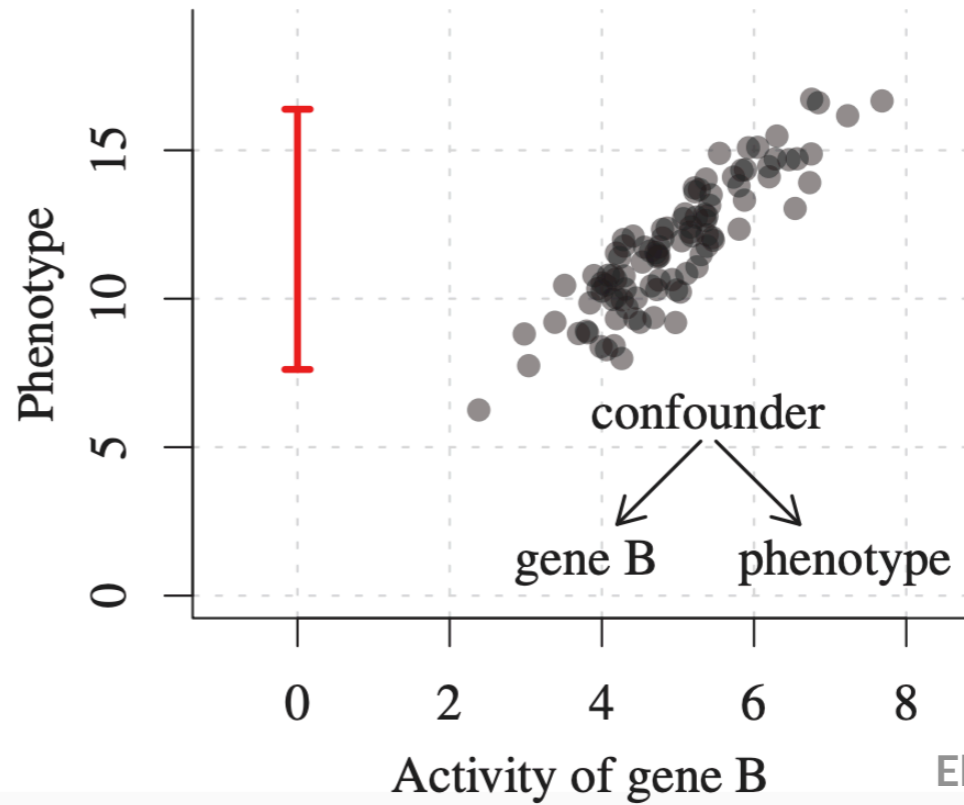
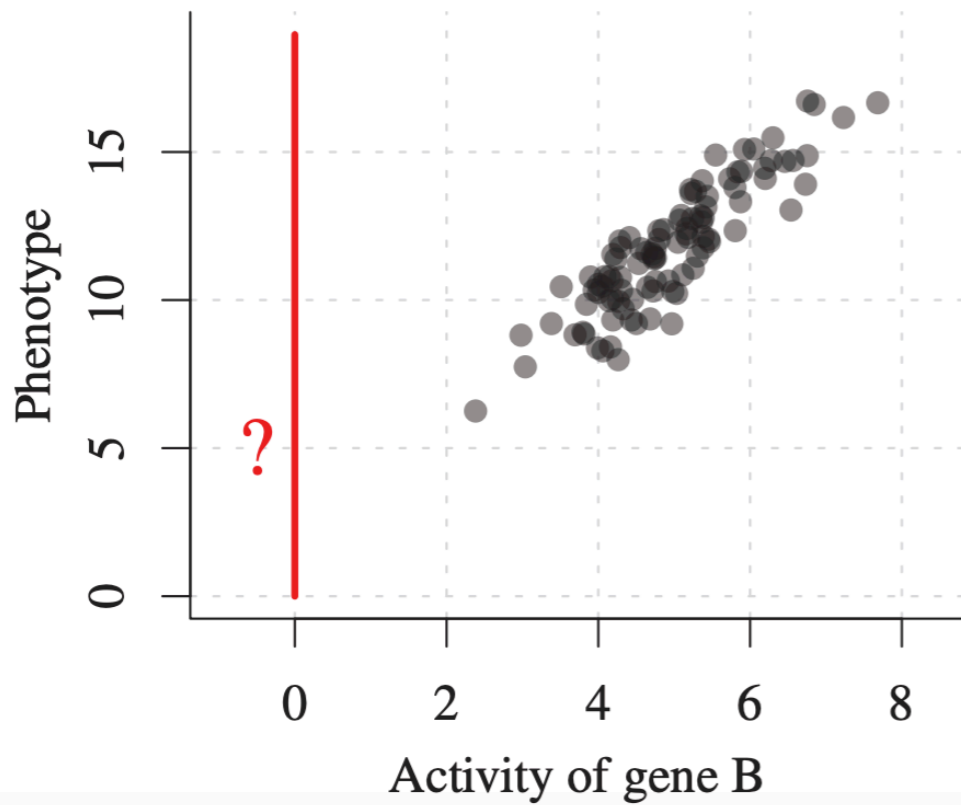
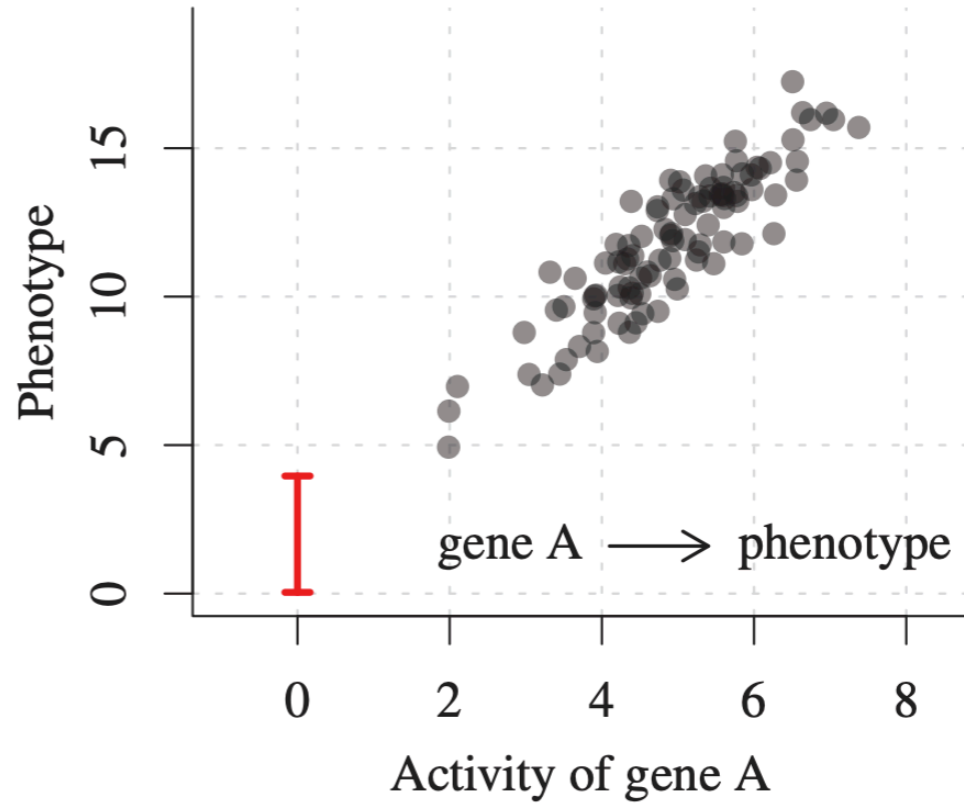
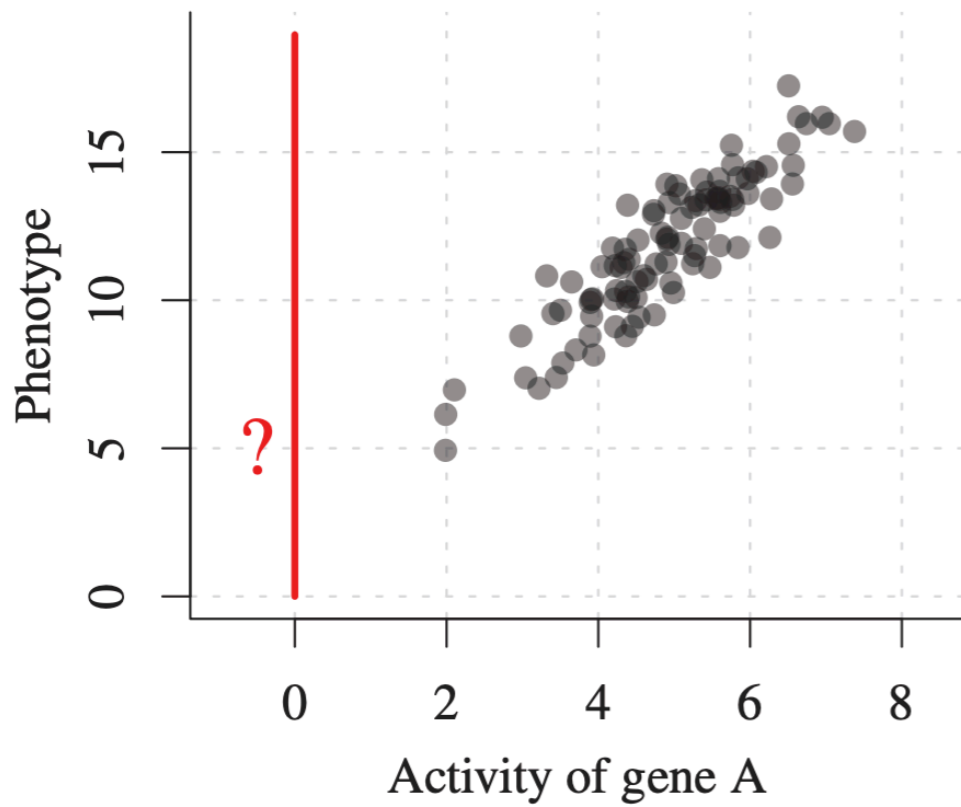


Source of data: Biobanks (e.g. UK's Biobank, US's All-of-US, ...) and electronic health records

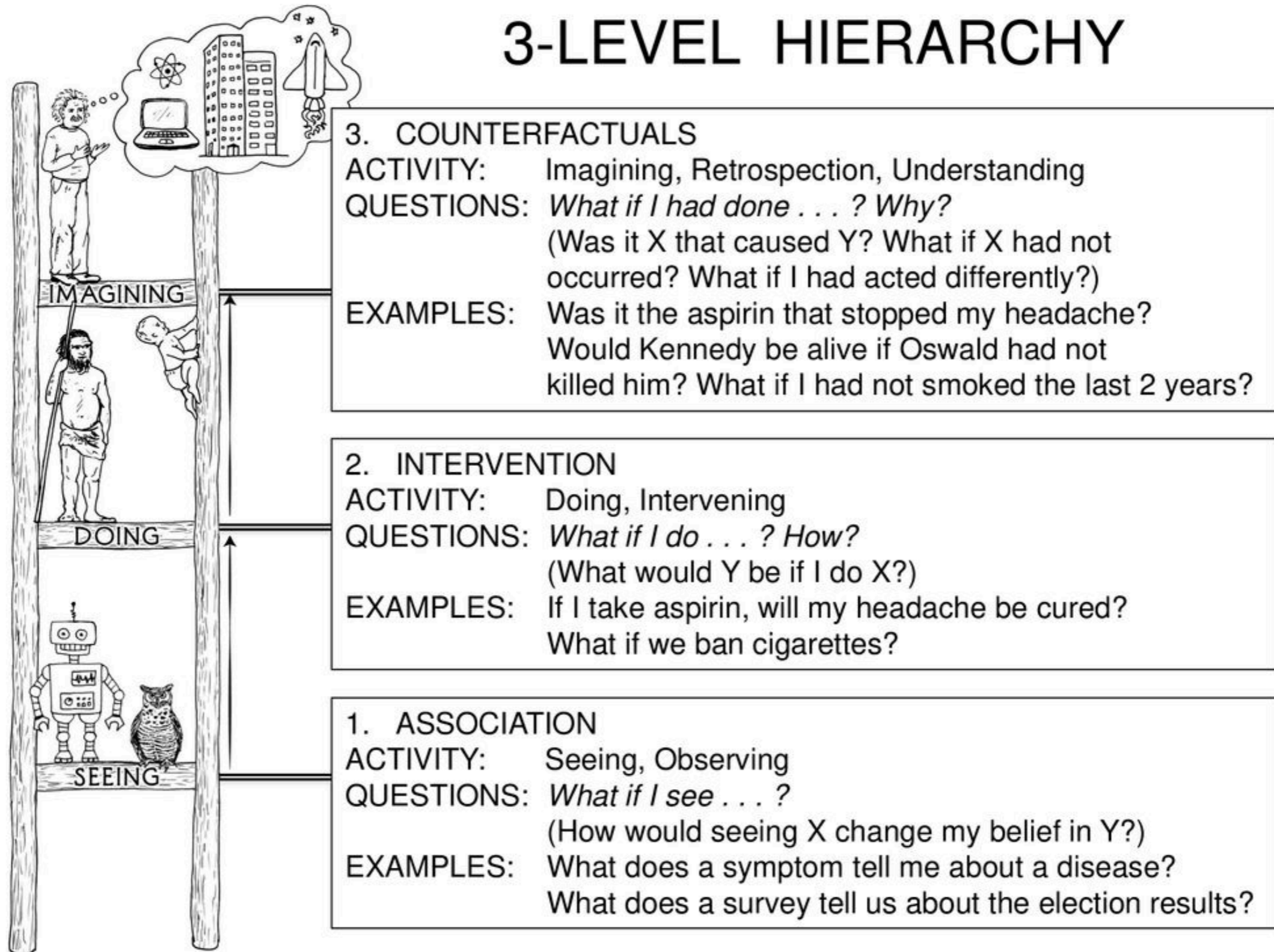
More examples: Gene perturbation



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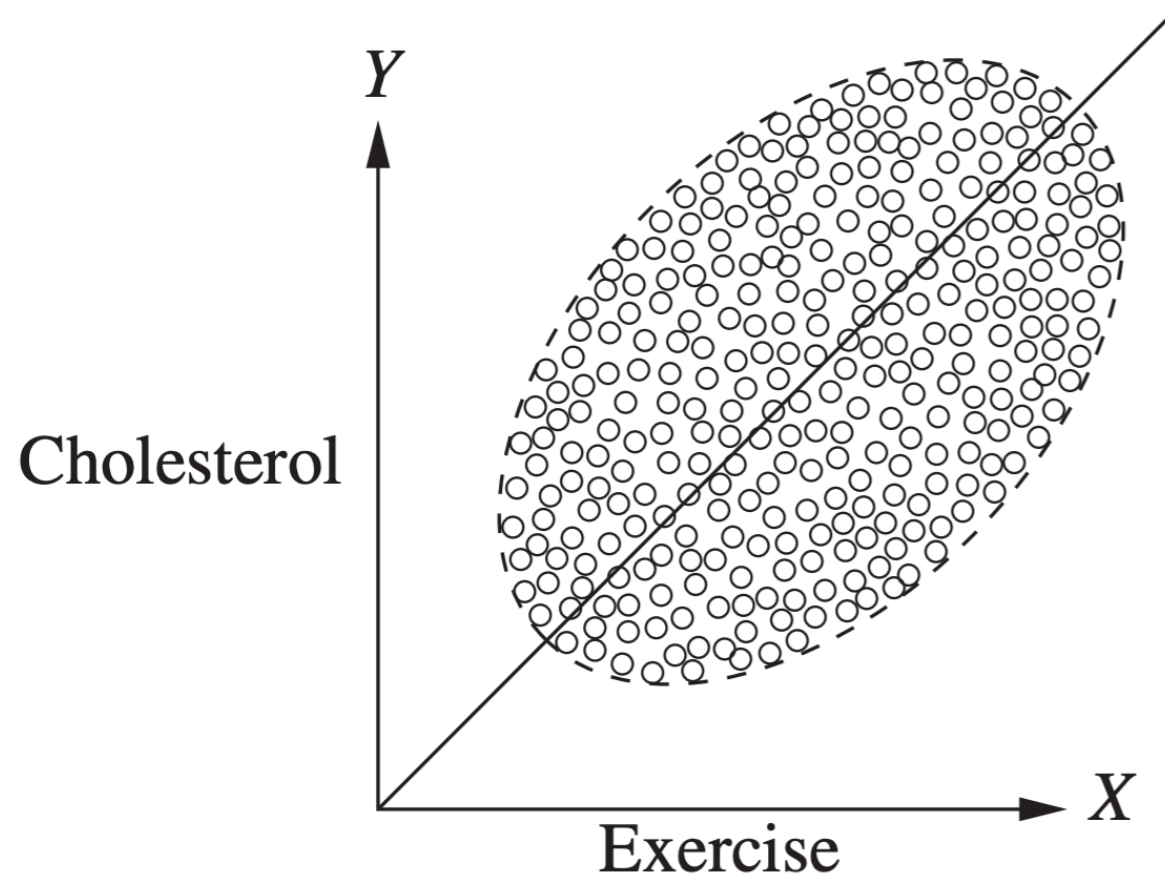
Pearl's ladder of causation



Simpson's paradox

Why concluding causality from purely associational measures, i.e. correlation, can be **very wrong** (not just neutral):

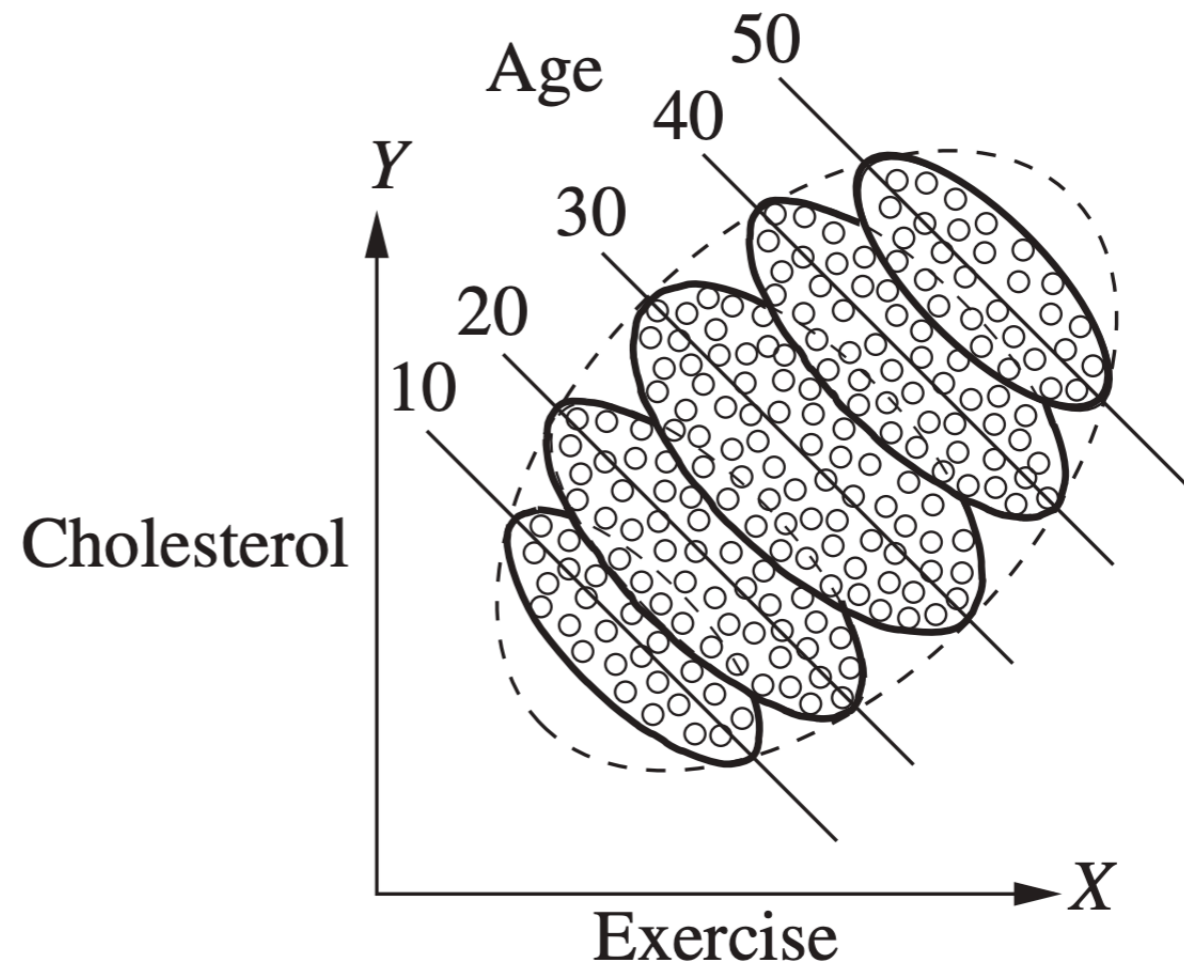
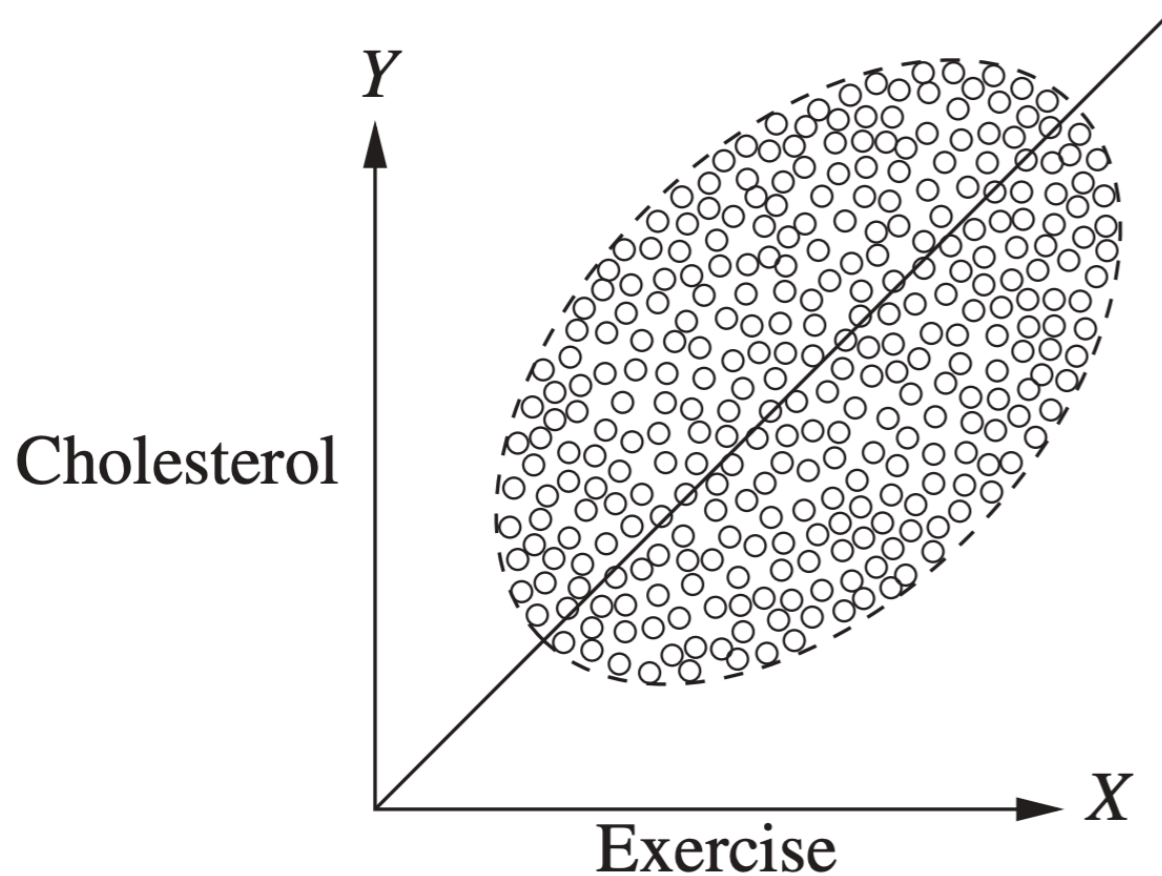
“It would have better not to make any statements!”



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Language of causality and the roles of variables

“What intervention”, “how much”, “when”, “how often”, “Control”, “effect of”, “why did”, “what if”, ...

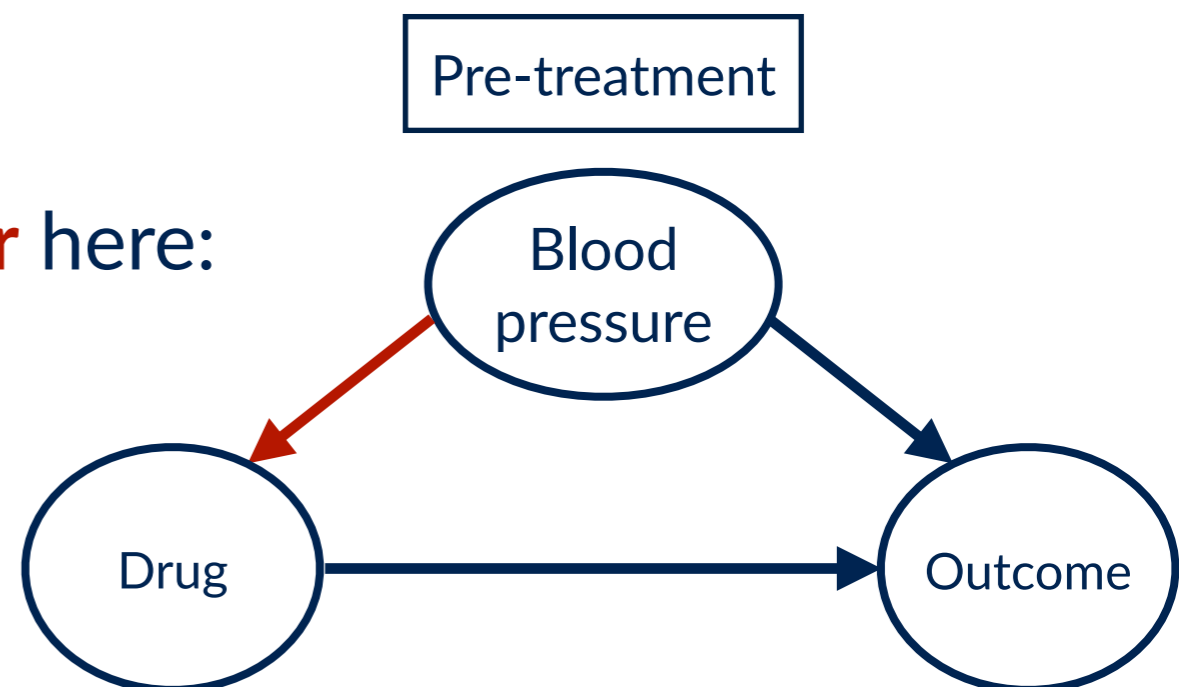
Causality language

Patient: Info on DNA variants and biomarkers, traits/disease, confounders

Clinician: Which medication, what dose, when, how often, ...

Consider all variables affecting the system of interest and
the role each plays.

Example, blood pressure is a **confounder** here:



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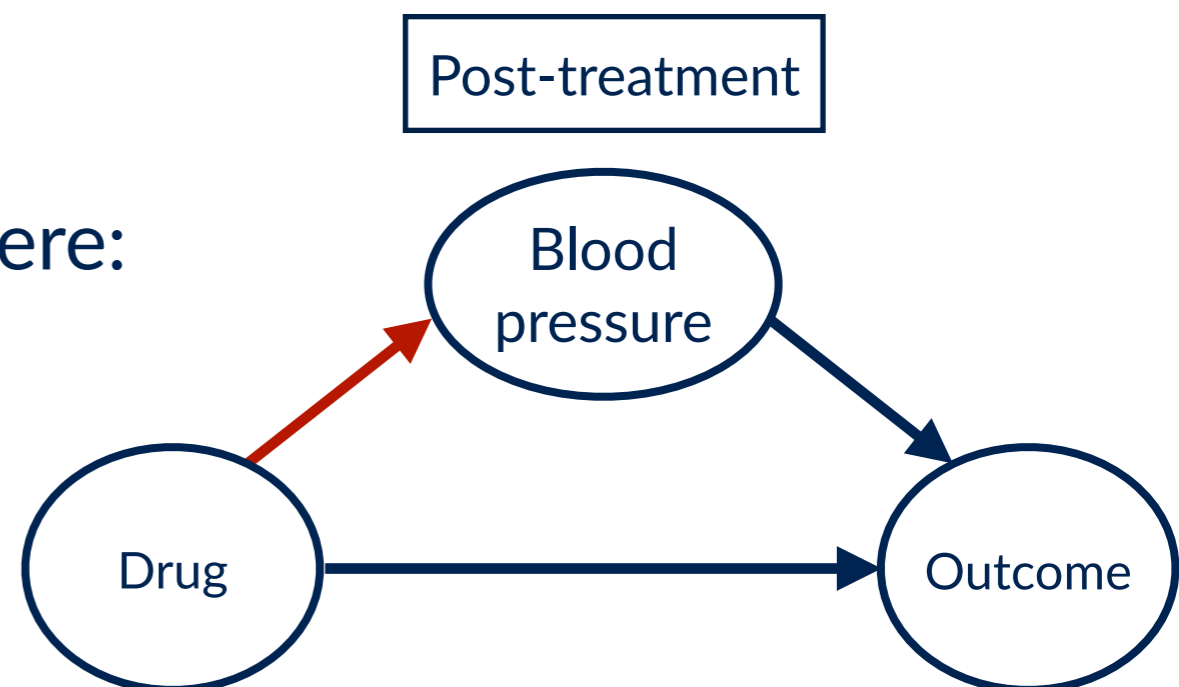
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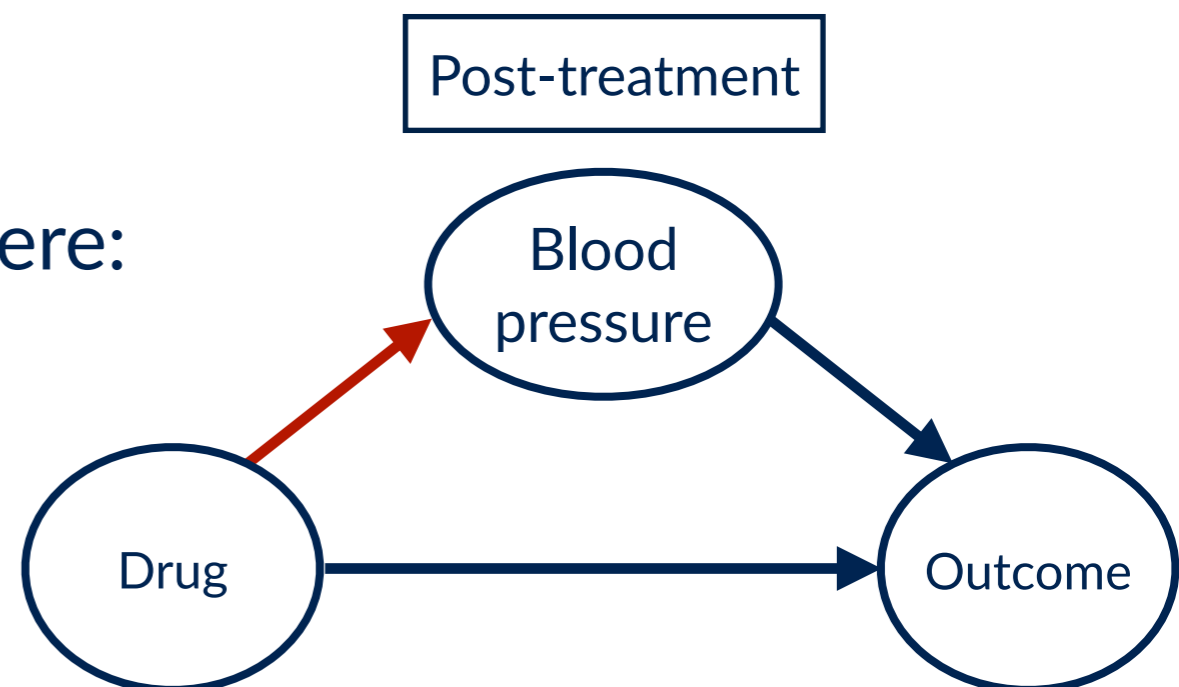
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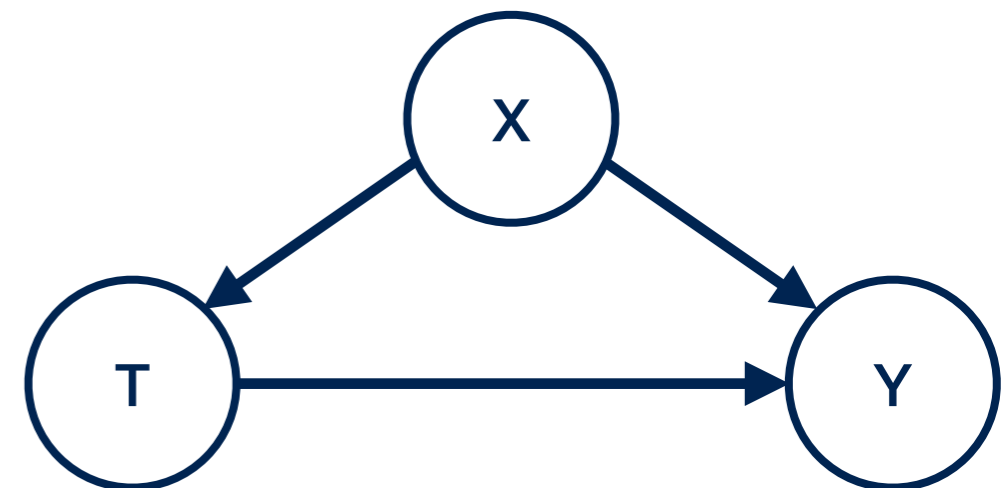
Example, blood pressure is a **mediator** here:

What happens when there are
lots of variables?



Conventions

- Variable to be manipulated: **treatment (T)**, e.g. medication
- Variable we observe as response: **outcome (Y)**, e.g. success/failure of medication
- Other observable variables that can affect treatment and outcome causally and we wish to correct for: **confounders (X)**, e.g. age, sex, socio-economic status, ...
- Unobservable confounder (**U**)



Causal effect estimation

Have a prior causal knowledge (may be incomplete) and know the treatment/outcome pair.

Counter example: weight gain, hours online

Interested in estimating the **effect size**:

$$\mathbb{E}[y_{t=1}(x) - y_{t=0}(x)] = \int (y_1(x) - y_0(x))p(x)dx$$

Note: The features/confounders x for both treatment and control groups are drawn from the same distribution $p(x)$

Goal: Find an **unbiased estimator**, e.g. signal/noise ratio

Randomised experiments: Already in causal framework

In a **randomised experiment**, the distribution of the confounders $p(x)$ is designed to be the same for both treatment groups ($t=0$ or $t=1$)

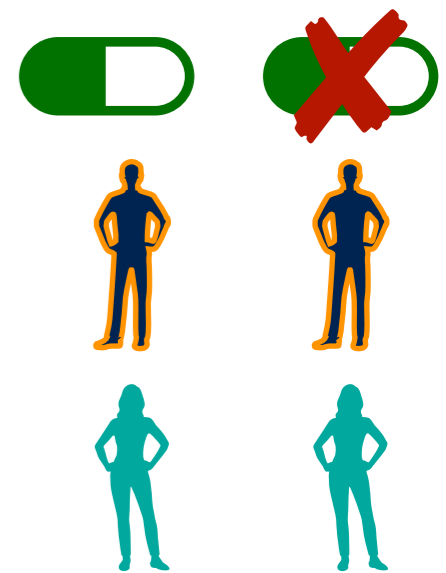
Paired '**clones**' in treatment and outcome groups

Simply take the difference of the averages:

$$\Delta \hat{\mu} = \hat{\mathbb{E}} [y_{t=1}(x) - y_{t=0}(x)] = \frac{1}{N} \sum_{i=1}^N (y_1^{(i)}(x) - y_0^{(i)}(x))$$

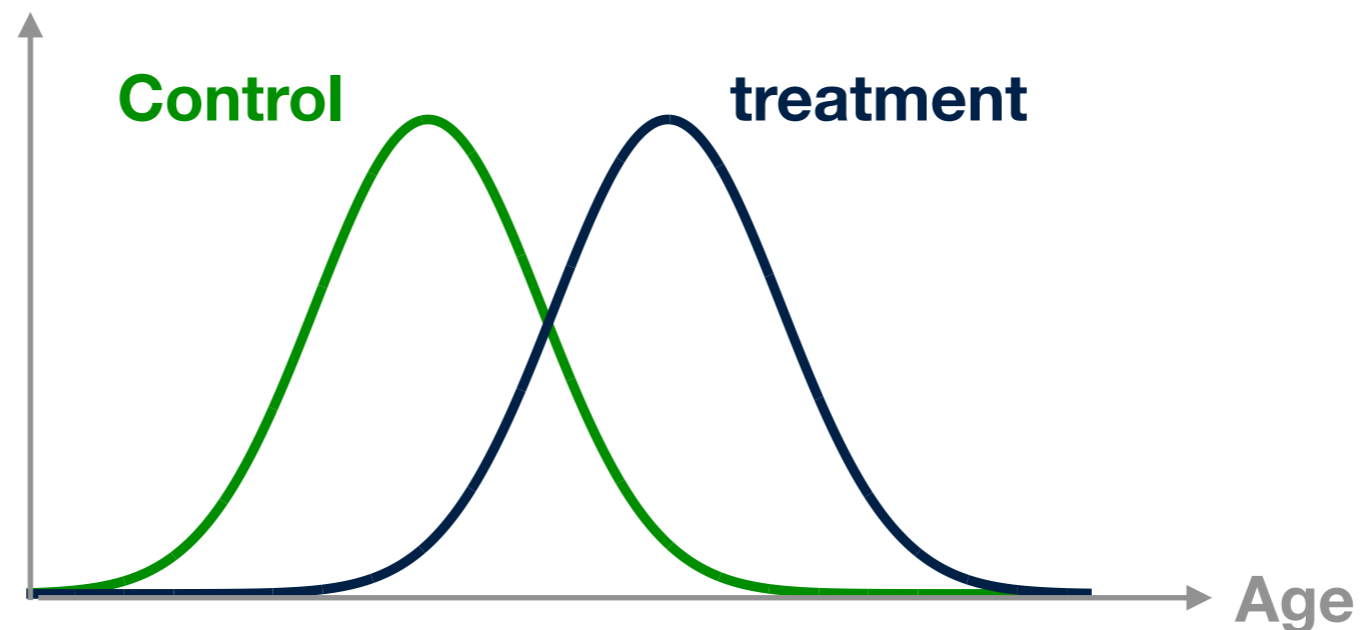
Perform statistical test: e.g. T-test and p-values ...

$$\frac{\Delta \hat{\mu}}{\sqrt{\frac{(\hat{\sigma}_{\Delta \mu})^2}{N}}} > t^*$$



Observational data: What goes wrong?

$$p(x|t = 1) \neq p(x|t = 0)$$



$$\left(\int y_1(x)p(x|t = 1)dx - \int y_0(x)p(x|t = 0)dx \right) \neq \int (y_1(x) - y_0(x))p(x)dx$$

Observational data: Stratification

- Measure outcome (success/failure), **within** each of the young/old groups **separately**
- Take weighted average by the probability of being young/old:

$$\mathbb{E}(\text{Healed}|t = 1) = \mathbb{E}(\text{Healed}|t = 1, \text{young})p(\text{young}) + \mathbb{E}(\text{Healed}|t = 1, \text{old})p(\text{old})$$

VS

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Issues: (i) All possible confounders need to be observed

(ii) Assume overlap between the two distributions (if there is no overlap, sample is not representative, e.g. performing the experiment only for old people),

(iii) Poor estimates as confounder dimensionality increases

	Age1	Age2	Age3	Age4
Female	●	●●● ●●●	● ●	●● ●●
Male		●●● ●●●	●● ●●	●



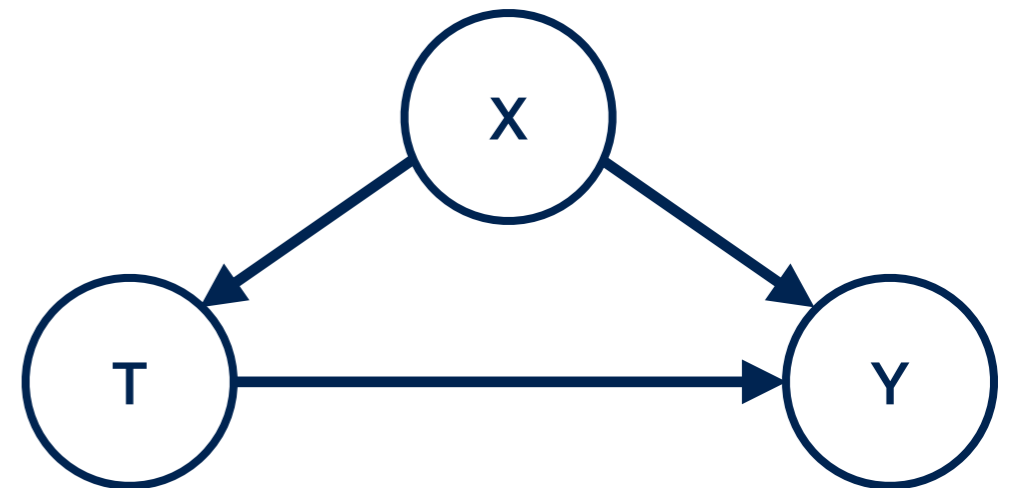
Need specific causal effect estimation techniques

Two main Frameworks for causal identifiability

- Potential outcomes framework (Neyman-Rubin):
 - Requires a given treatment-outcome pair (known directionality)
 - For causal estimation
 - More familiar to biomedical researchers (this is changing ...)

- Structural causal models (Pearl):

- Causal graphs
- Structural equations $x = f_x(\epsilon_x)$, $t = f_t(x, \epsilon_t)$, $y = f_y(x, t, \epsilon_y)$
- Algorithmic
- For causal estimation and discovery



Assumption: Independent noise terms: $\epsilon_x \perp\!\!\!\perp \epsilon_t \perp\!\!\!\perp \epsilon_y$

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Why deriving causality from observational data is non-trivial.

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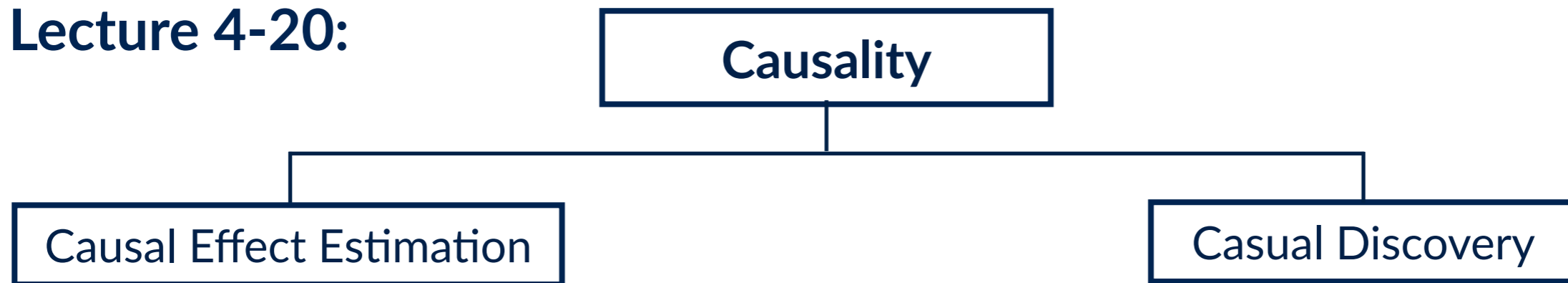
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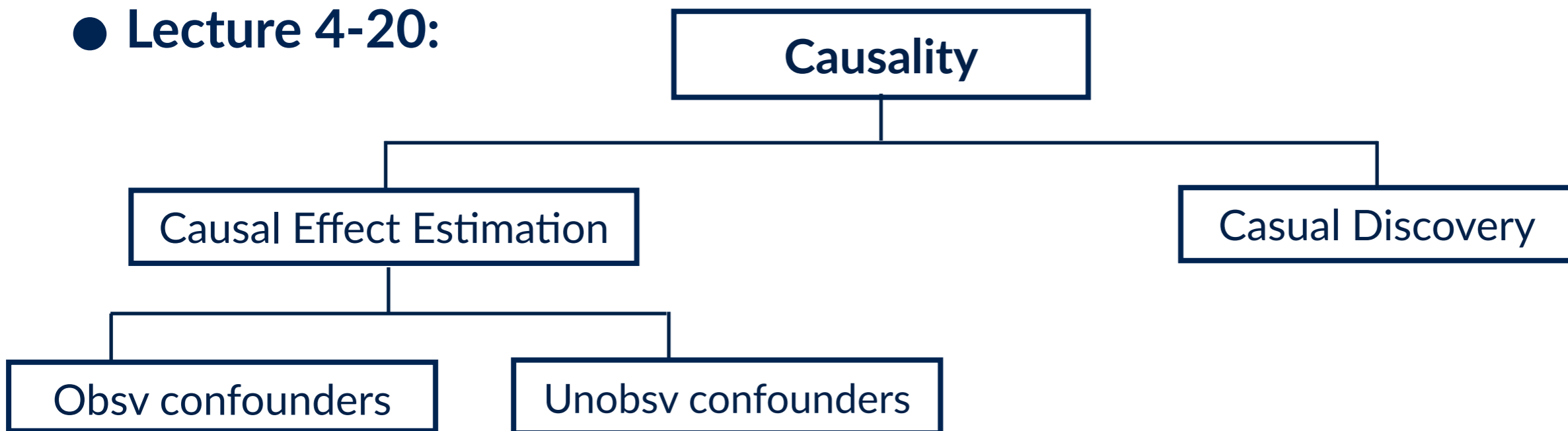
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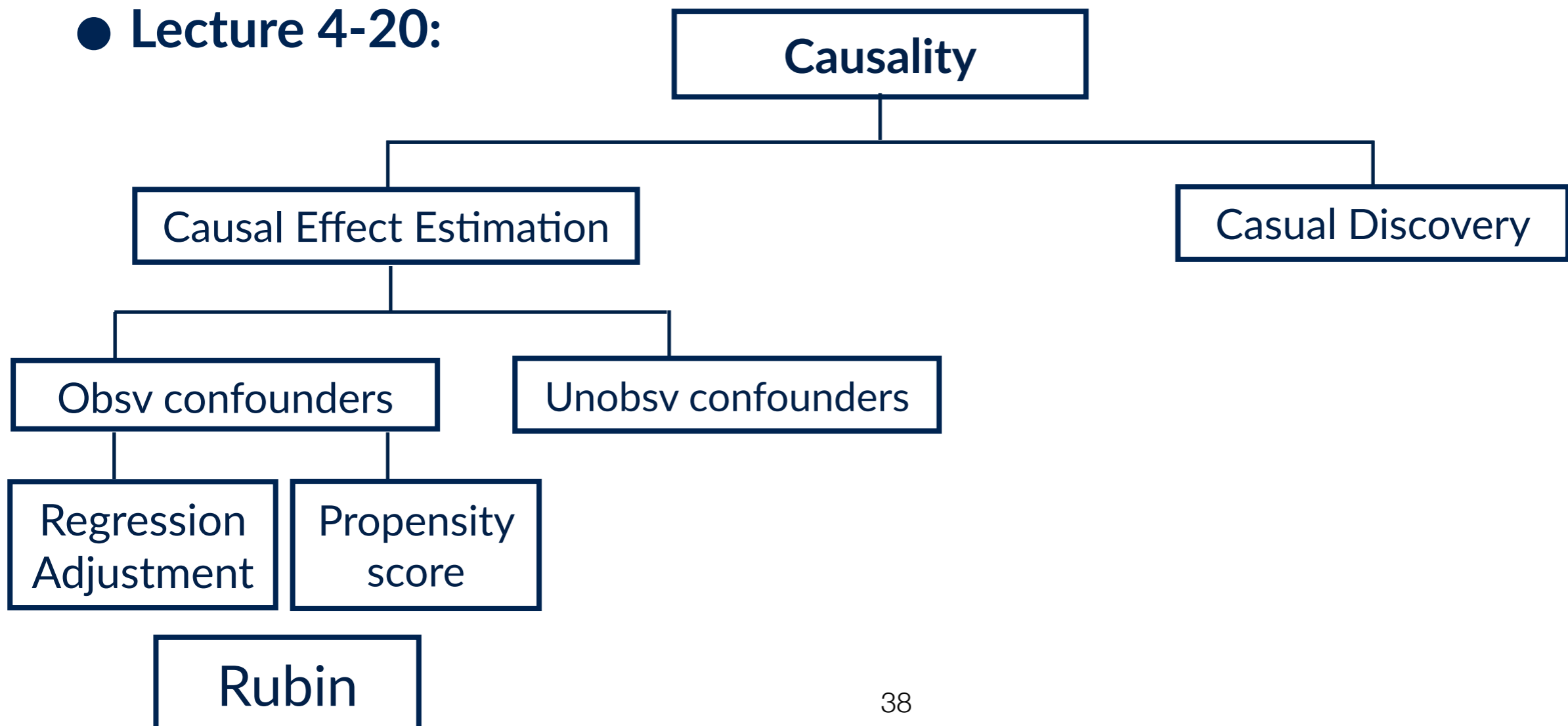
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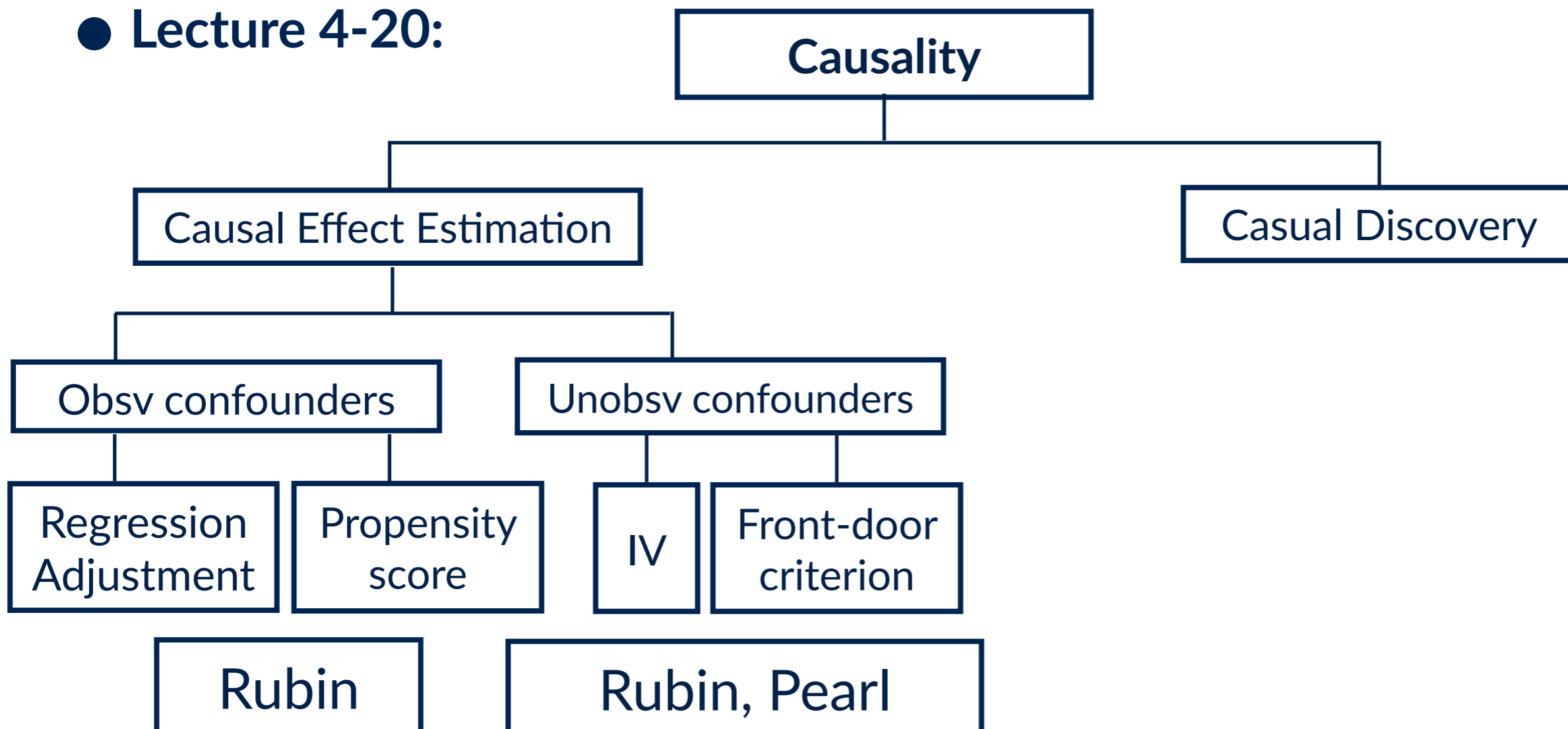
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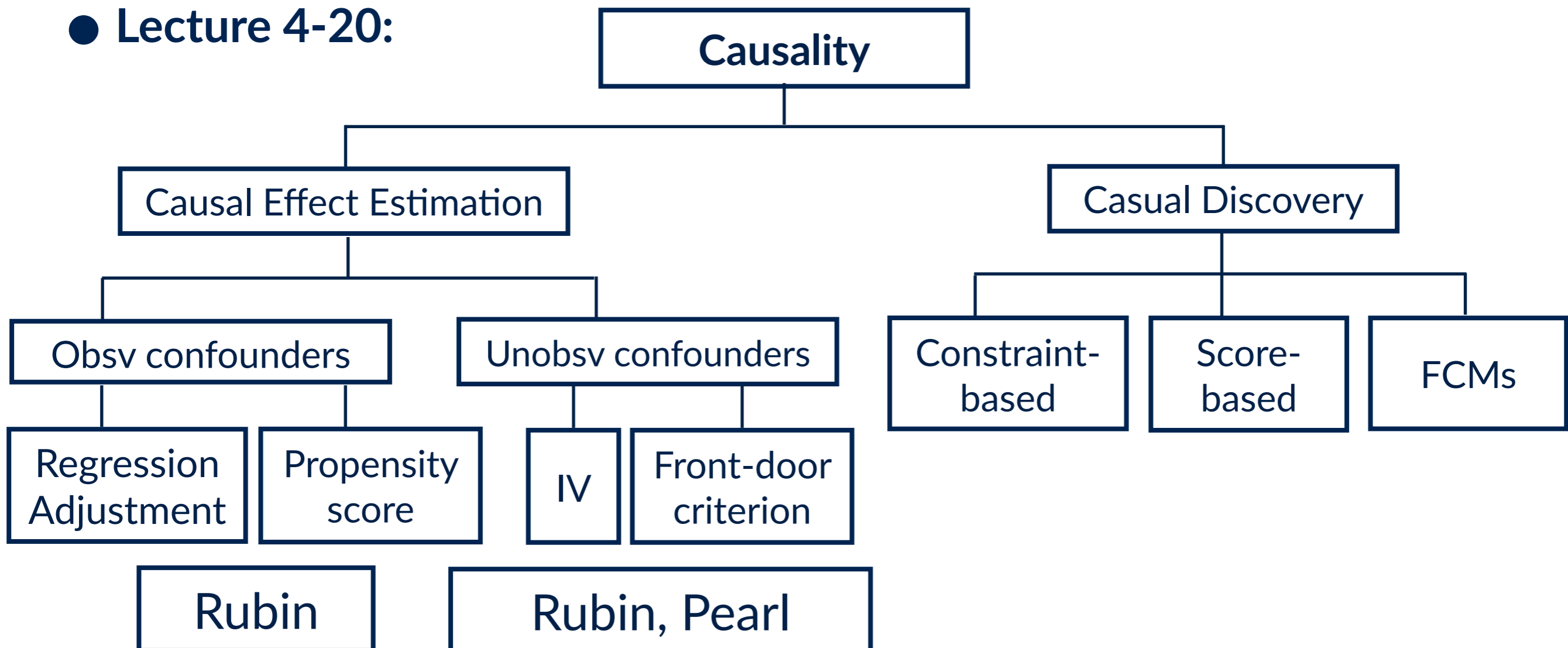
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Causal Effect Estimation vs Causal Discovery

- **How much would some variables change if we manipulate the value of another variable?**
 - Have a prior causal knowledge (may be incomplete)
 - Wish to estimate degrees of causal dependencies

- **By modifying the value of which variables could we change the value of another variable?**
 - Wish to discover the causal graph itself
 - Many assumptions ... difficult to get robust results that one can trust without perturbation data (even difficult with perturbation data!)