

Simulation, Analysis, and Validation of Computational Models

— Multi-Agent Systems —



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- Schelling model
- Self-organisation and emergence
- Multi-agent systems (a.k.a. self-organised systems)
- Mesa

Multi-agent systems (MAS): Examples

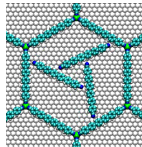
- Stock exchange
- Team games
- Work groups
- Animal behaviour
- Swarm intelligence
- Microbial intelligence
- Artificial chemistry
- Self-driving cars
- Warehousing
- Logistics
- Social modelling
- Epidemiology
- Sensor networks
- MARL



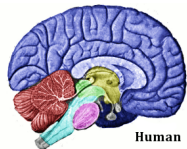
D. Dibenski: images.fws.gov



Serge Kernbach



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Much of the MAS literature has more restrictive (or just different) assumptions, but in order for simulations to be interesting, agent should have the following properties:

- **Autonomy:** Agents have some level of independence.
- **Local sensing:** Agents sense only some aspect of the environment the complexity of which surpasses the complexity the agent.
- **Decentralisation:** The behaviour of an agent can influence “nearby” agents, but no agent is in control of the system.

Panait & Luke (2005) Cooperative Multi-Agent Learning: The State of the Art.
Autonomous Agents and Multi-Agent Systems 11, 387–434.

Simulations can be useful for many other reasons: E.g. to find out about stability, robustness, efficiency, scaling of any complex systems, or to make sure that self-organisation is not an issue.

- Schelling model

T.C. Schelling (1971) Dynamic models of segregation. *J. Math. Sociology* 1, 143–186.

- Clustering by robots aimlessly pushing boxes
- Granular convection (“Brazil nuts effect”)

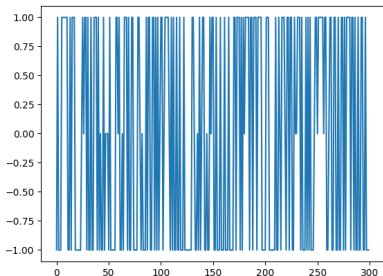
Rosato e.a. (1987) Why the Brazil Nuts are on Top. *Physical Review Letters* 58, 1038–41.

- Large scale structure of the universe

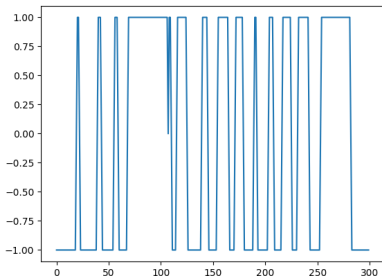
Schelling model

Original formulation: Consider city with people of group A and people of group B

If the fraction of neighbours of the same group is less than p , move to a more homogeneous place, until no more moves are possible.



1D case: Random initialisation



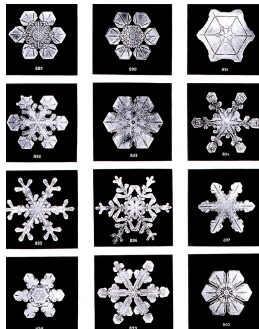
Segregated by Schelling model

Notebook from Li&Nakano: Consider different groups sizes, various p and fraction of free sites, and try to transfer to higher dimensions.

- Due to the activity and interaction of many agents, the order in the system can increase
- As the agents use energy from outside this is not in conflict with the *2nd law of thermodynamics*
- Energy import enables entropy export
- Often phenomena such as *self-organisation* or *emergence* occur, i.e. “qualitative changes by more of the same”.

A property of a systems is called emergent, if it is not present as a property of its elements.

- E.g. *kinetic energy* of a multi-particle systems “averages out”, and *temperature* because a meaningful description
- A single neuron (both biological or artificial) can perform a (linear) binary classification, while a neural network can recognise complex patterns.
- An ant can find food, but many ants are needed to start a colony.



Self-organisation

- The mechanism of order arising from local interactions between parts of an initially unstructured system

(One way to tell apart: Emergence is a phenomenon, self-organisation is a mechanism)

- Examples:
 - Waves forming driven by wind on a surface of water
 - Specific light frequencies are selected from wide spectrum to produce laser light
 - Convection patterns: Bénard effect, weather, cloud formation
 - Pattern formation, reaction-diffusion system
 - Traffic jams, stock-market crashes, rain, natural evolution, biological neural systems, cosmology etc.
- Simulations can serve various purposes, but most interesting are cases of self-organising processes, i.e. when system properties cannot be easily predicted from the elements.

'Since no system can correctly be said to be self-organizing, and since use of the phrase "self-organizing" tends to perpetuate a fundamentally confused and inconsistent way of looking at the subject, the phrase is probably better allowed to die out.' Ashby, 1962

- Generally (real or simulated agents)
 - Data: Sensing environment (e.g. neighbouring agents)
 - Model (Policy): mapping data (incl. internal states) → actions
 - Some form of actuator (critical for the agent being an agent)
 - Initialisation (e.g. for heterogeneous MAS)
 - Termination (or observation) of experiment
- In simulation:
 - Environment
 - Position in environment
 - Agent-ID (also for centrally controlled real agents)

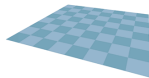
Agents can be

- moving in space e.g. articulated robot swarms
- stationary, e.g. agents on a grid interacting with their neighbors (see rock-paper-scissors example below)
- moving towards a position that is (at least temporarily) stationary, e.g. kilobots, modular robotics, coral polyps

Periodic boundary conditions

How to minimize effects of boundary corners, finite size of the simulation?

- Plain playing field becomes topologically a torus, while geometrically still being flat.
- No boundaries: Every point (or agent) is equally in the interior of the system.
- If spatial patterns play any other role in the dynamics, then Moiré-pattern-like interaction by that spreading either way can affect the dynamics.
- If spatial scales are small compared to the emerging patterns, usually no problem occurs, but for a large playing area any boundary conditions are likely to be fine.
- Magic numbers: For emerging patterns of size 20 for total size 50: destructive interference. For total size 60: constructive interference



Lucas Vieira (2012)

- Mesa is an open-source Python library for agent-based modeling for simulating complex systems and exploring emergent behaviors.
- Time-order: Both in discrete and (numerical) continuous systems all agents (rather: dimensions) are updated either
 - synchronously: Calculate all, then update all
 - sequentially: Calculate and update one by one
- How to implement parallel activity to run¹ asynchronously ensuring that each agent has a fair share of *compute*?

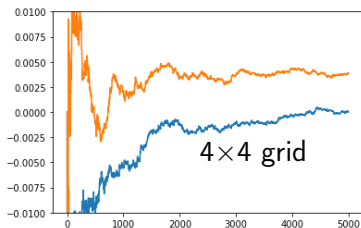
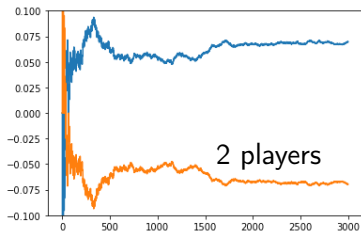
¹This is about simulation of causality rather than hardware or real-time.

Agents playing Rock, Paper, Scissors (see Li & Nakano, Ch. 7)

Agent A (“stubborn”): Stays with probability 80% with previous choice, and switches with probability 10% to one of the other two.

Agent B (“sneaky”): Use move that would have worked that previous time, or random after a draw

Points: “1” Not beaten by any neighbours, “-1” Not won against any of them, 0 otherwise (Teams A and B are arranged in checkerboard fashion with for neighbours from the opposing team).



In a 1-to-1 setting, sneaky can beat **stubborn** easily. On a square grid **sneaky** has to beat 4 neighbours, which is difficult when it is likely that at least one of them is changing its move randomly.

- Group behaviour is deviate strikingly from individual or pairwise behaviour
- Group behaviour be against the intention of each of the member even in a homogeneous group
- Simulations can show interesting system-level phenomena

- Coursework assignment
- Labs

- Case studies